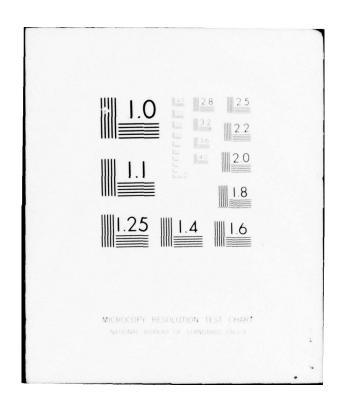
TOLEDO UNIV OH DEPT OF ELECTRICAL ENGINEERING F/6 9/5
UTILIZATION OF SOURCE IMPEDANCE TO DECREASE THE WEIGHT OF D.C. --ETC(U)
JUL 77 T A STUART

AFOSR-TR-77-0985
NL AD-A043 432 UNCLASSIFIED | OF 2 AD 43432





Final Report on AFOSR GRANT

AFOSR-76-2997

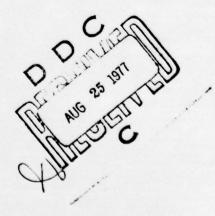
July 1977

"UTILIZATION OF SOURCE IMPEDANCE TO DECREASE THE WEIGHT OF D.C. POWER SUPPLY FILTERS"

by

Approved for public release; distribution unlimited.

T. A. Stuart
Department of Electrical Engineering
The University of Toledo



ODC FILE COPY

AIR FORCE OFFICE OF SCIENTIFIC RESEARCH (AFSC)
NOTICE OF TRANSMITTAL TO DDC
This technical report has been reviewed and is approved for public ralease IAW AFR 190-12 (7b).
A. D. BLOSE
Technical Information Officer

Final Report on AFOSR GRANT

AFOSR-76-2997

July 1977

"UTILIZATION OF SOURCE IMPEDANCE TO DECREASE THE WEIGHT OF D.C. POWER SUPPLY FILTERS"

by

T. A. Stuart
Department of Electrical Engineering
The University of Toledo

SECURITY CLASSIFICATION OF THIS PAGE (When Date Entered)	
REPORT DOCUMENTATION PAGE	READ INSTRUCTIONS BEFORE COMPLETING FORM
AFOSR-TR- 77-0985	. 3. RECIPIENT'S CATALOG NUMBER
UTILIZATION OF SOURCE IMPEDANCE TO DECREASE THE WEIGHT OF D.C. POWER	5. TYPE OF REPORT & PERIOD COVERED FINAL REPORT
SUPPLY FILTERS	6. PERFORMING ORG. REPORT NUMBER
7. AUTHOR(s)	8. CONTRACT OR GRANT NUMBER(s)
Stuart, Thomas A.	AFOSR-76-2997 mil
9. PERFORMING ORGANIZATION NAME AND ADDRESS	10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS
University of Toledo	61102F
Department of Electrical Engineering	011021
Toledo, Ohio 43606	2205 10
11. controlling office name and address AFOSR/NE	2305. D9
	18 July 1977
Bldg 410, Bolling AFB, DC 20332	18 July 1977 13. NUMBER OF PAGES 153
14. MONITORING AGENCY NAME & ADDRESS(il different from Controlling Office)	15. SECURITY CLASS. (of this report)
	UNCLAS
	15a. DECLASSIFICATION/DOWNGRADING SCHEDULE
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different fro	om Report)
18. SUPPLEMENTARY NOTES	
19. KEY WORDS (Continue on reverse side if necessary and identify by block number. Power Supply Superconducting)
Filter Alternator Source Impedance	
<u> </u>	
This report presents a study of how the source to reduce the weight of the output filter of a rectifical ternator power supply.	impedance can be used

SECURITY CLASSIFICATION OF THIS PAGE (When Date Entered)

REPORT DOCUMENTATION PAGE	READ INSTRUCTIONS BEFORE COMPLETING FORM
AFOSR TR-77-0985	3. RECIPIENT'S CATALOG NUMBER
4. TITLE (and Subtitle)	5 TYPE OF REPORT & PERIOD COVERED
Utilization of Source Impedance to Decrease	Final Repert.
the Weight of D.C. Power Supply Filters,	June 1976 — June 1977
	6) DERPORMING ORG. REPORT NUMBER
7. AUTHOR(e)	8. CONTRACT OR GRANT NUMBER(s)
Thomas A. Stuart	F-AFOSR 2997-76
9. PERFORMING ORGANIZATION NAME AND ADDRESS	10. PROGRAM ELEMENT, PROJECT, TASK
The University of Toledo	(19) (17) (03)
Toledo, Ohio 43606	9768 03 D9
3) Dept of Elec. Engry	(2303)
11. CONTROLLING OFFICE NAME AND ADDRESS	Jul 1977
AFOSR(PMD)	13. NUMBER OF PAGES
Bolling AFB, D.C. 20332	153 12 1616
14. MONITORING AGENCY NAME & ADDRESS(II different from Controlling Office)	15. SECURITY CLASS. (of this report)
	Unclassified
Same	
	15a. DECLASSIFICATION/DOWNGRADING SCHEDULE
16. DISTRIBUTION STATEMENT (of this Report)	
Approved for public release; distribution unlimi	ited.
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from	om Report)
18. SUPPLEMENTARY NOTES	
19. KEY WORDS (Continue on reverse side if necessary and identify by block number	7)
Power Supply Superconducting	g
Filter Alternator	
Source Impedance	
20. ABSTRACT (Continue on reverse side if necessary and identify by block number))
This report presents a study of how the sour used to reduce the weight of the output filter of conducting alternator power supply.	
	Anec

DD FORM 1473 EDITION OF 1 NOV 65 IS OBSOLETE 410 351
SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

CONTENTS

		Page
1.	ALTERNATOR WITH UNCONTROLLED RECTIFIER BRIDGE	1
1.1	Introduction	1
1.2	Steady State Alternator-Rectifier Model	3
1.3	Steady State Equations	6
1.4	Solution for I_f , β , μ , V and W	16
1.5	Numerical Results	18
2.	ALTERNATOR WITH CONTROLLED RECTIFIER BRIDGE	30
2.1	Introduction	30
2.2	Steady State Model	31
2.3	Steady State Equations	31
2.4	Numerical Results	33
3.	FAULT CURRENT CALCULATIONS	
3.1	Introduction	43 UNANNOUNCED
3.2	Circuit Model and Equations	45 JUSTI ICA 101
3.3	Numerical Results	51 BY DISTRIBUTION/AVAP ABILITY
4.	VARIATION OF THE ALTERNATOR PARAMETERS TO DECREASE OUTPUT RIPPLE VOLTAGE	55 0
4.1	Introduction	55
4.2	Effect of L_a on the Output Voltage Harmonics,	57
4.3	Numerical Results	58
5.	MINIMIZATION OF LOCO FILTER WEIGHT	63
5.1	Introduction	63
5.2	Calculation of L and C for Minimum Total Filter Weight	63

Buff Sect

						Page
5.3	L C Design Algorithm					67
5.4	Numerical Results					69
6.	SENSITIVITY ANALYSIS					74
6.1	Introduction					74
6.2	Differential Method					75
6.3	Deliberate Error Method					77
6.4	Numerical Results					78
7.	VOLTAGE REGULATOR AND CURRENT OVERLOAD PROTECTION (CIR	CU	IT	S	95
7.1	Introduction					95
7.2	Experimental Results					95
8.	CONCLUSIONS			•		102
9.	RECOMMENDATIONS					103
.0.	REFERENCES					104
1.	RESEARCH PUBLICATIONS		•			108
PPEN	NDIX I: GLOSSARY OF TERMS					109
PPEN	NDIX II: TRANSIENT MATRICES					112
PPEN	NDIX III: MAIN PROGRAMS					113
PPEN	NDIX IV: SUBROUTINES					132
PPENI	IDIX V: DISTRIBUTION LIST					154

SUMMARY

This report presents an analysis of a DC power supply consisting of a superconducting alternator, a rectifier bridge, and an LC output filter. The main purpose of this research was to determine if changes in the size of the alternator inductances would allow the use of a smaller filter. To perform this study it was necessary to examine the behavior of the filter and to determine how its operation was affected by the alternator parameters.

Basically, the filter performs two functions:

- 1. It attenuates the output ripple voltage.
- It limits the initial fault current when a short circuit occurs at the load.

Both of these functions also depend upon the values of the alternator inductances.

Since the first function refers to the steady state behavior, it was necessary to develop a model for this operating mode. This was done first for a system with an uncontrolled rectifier bridge and then these results were extended to a controlled rectifier bridge system. The second function is a transient phenomenon, so it was also necessary to develop a second model to describe the transient behavior.

Once the system models were complete, a study was performed where the unfiltered ripple voltage was calculated for various values of the alternator inductances. It was found that under certain conditions the ripple voltage can be decreased by increasing the armature self

inductance (L_a). A program was then written which calculated the weight of the LC filter that was required for a given set of specifications and alternator parameters. This program indicated that an increase in L_a could decrease the required filter weight by as much as 22%.

Other investigations included a sensitivity analysis of the alternator inductances and the design and testing of a phase controlled voltage regulator with current overload protection.

1. ALTERNATOR WITH UNCONTROLLED RECTIFIER BRIDGE

1.1 Introduction

Recent advancements in superconducting alternators have created a strong interest in using these machines for airborne electric power supplies. The predominant advantage of this power source is its relatively low weight for applications requiring multi-megawatt outputs at several kV. This low weight characteristic occurs because of two factors:

- Even with the required cryogenic equipment, the superconducting alternator system weighs much less than a conventional alternator.
- The higher armature voltages of the superconducting machine may eliminate the need for heavy output inverters and transformers.

These attributes are discussed in further detail in such references as [1] - [12], and a very recent example of such a machine is described by McCabria, et al. in [13,14]. This particular machine develops 10MVA at 5 kV and weighs approximately 1,000 pounds (alternator weight only). This same reference also includes projected estimates for a 25MVA machine weighing between 1882 and 2160 pounds, depending on rated output voltage (again, these figures only include the weight of the alternator).

The potential advantages of superconducting alternators have prompted extensive research in this area, most of which has concentrated on ac loads (again see [1] - [14]). Applications for these machines also exist in high power dc systems however, where the alternator is connected to a rectifier bridge followed by a large filter choke. This mode of operation

has been studied in detail for conventional alternators, (see [15] through [21]), but until now no such analysis has been presented for the superconducting machine.

One of the more rigorous analyses of conventional rectified alternators is that presented by Franklin [17,18] for salient pole machines.

By assuming constant flux linkages for the rotor windings, this study derives a set of nonlinear equations in terms of the electrical variables of interest. Certain approximations then lead to a linearization involving a constant K factor, and an explicit solution is obtained. The advantages of this approach are readily apparent since it provides a closed form expression for each of the variables, once the proper K factor has been found. The determination of K is somewhat distracting however, since it is load dependent and requires the use of numerical methods. In the following section it will be shown that this K factor can actually be eliminated from the final solution if a Newton-Raphson algorithm is used. This new approach appears to have certain advantages since it is somewhat less complicated and does not depend on any linearization factors.

The essence of the work presented here is:

- Franklin's basic analysis methods are extended to the superconducting machine.
- 2. The dependence on the previously mentioned K factor is eliminated. As stated above, this is accomplished by using a Newton-Raphson algorithm where a K=1 is used only to find a starting point.
- 3. A numerical example predicting the rectified characteristics of the machine described by McCabria, et al. in [13,14] is included.

The overall intent is to provide an analytical model of the steady state behavior of the superconducting alternator with a rectified output.

This analysis is regarded as a preliminary step to the eventual design and testing of these machines for D.C. loads.

1.2 Steady State Alternator-Rectifier Model

The armature of the superconducting machine is assumed to be Y connected as indicated for the basic two pole machine in Figure 1. The d and q windings shown in this figure are equivalent windings that account for the effect of the cylindrical damper shield located between the rotor and the stator (see [5], [13] or [14] for example). Output voltage and current waveforms are shown in Figure 2, where the indicated 0 corresponds to Figure 1. Formulation of this problem proceeds in much the same manner as in [17,18], but there are some important differences in the machine parameters. It also should be noted that the method of solution is quite different from these earlier references, and certain equations are employed in a different manner.

The following approximations are utilized:

- All winding and diode resistances are quite small and can be ignored.
- 2. All diode voltage drops are negligible.
- The load inductance, L_o, is sufficiently large to maintain a constant I_L, i.e., the effect of load current variations is ignored.
- 4. Each armature winding is assumed to have a perfect sinusoidal distribution about the stator.

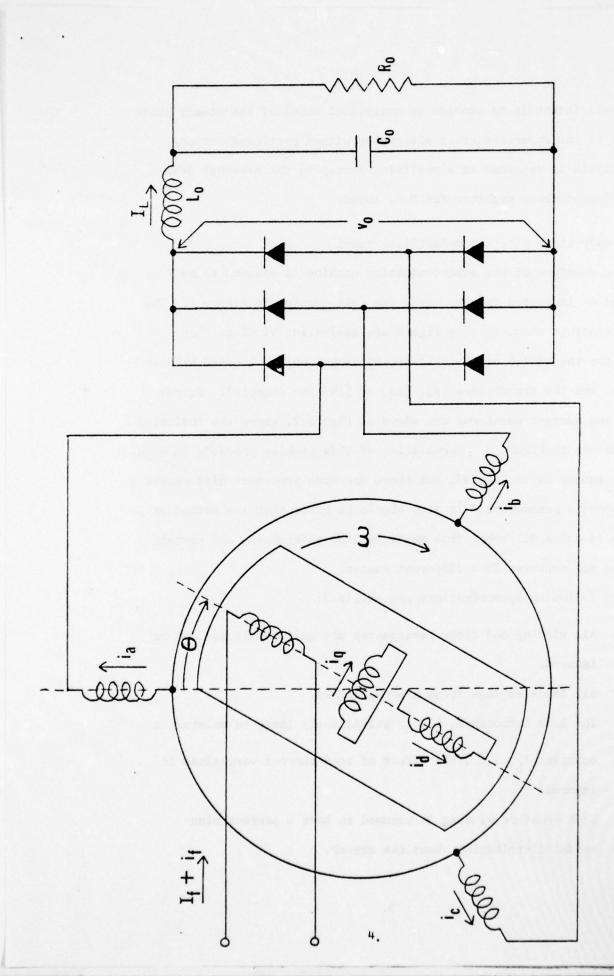


Figure 1. Equivalent Circuit for the Superconducting Alternator with Uncontrolled Rectifier Bridge.

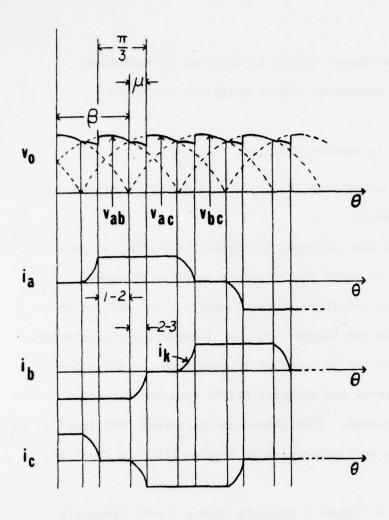


Figure 2. Output Voltage and Armature Currents with Uncontrolled Rectifier Bridge.

- 5. The effect of the damper shield is modelled by equivalent direct axis and quadrature axis windings on the rotor (d and q).
- 6. The rotor speed is assumed constant.

Since the superconducting alternator is an air core machine there are no saturation or saliency effects.

Although the line to line voltages in Figure 2 are shown as perfact sinusoids, it should be noted that they are actually distorted somewhat. Thus commutation actually starts at some $\beta > 90^{\circ}$ and not at $\theta = \beta = 90^{\circ}$ as indicated in the figure. Another interesting characteristic is the fact that the stator MMF is constant in magnitude and direction during the conduction interval and abruptly shifts to a new direction during the commutation interval. This phenomenon is termed "MMF jump" as is described further in such references as Stepina [16] and Franklin [17].

The waveforms shown in Figure 2 indicate that $\mu < \pi/3$. Franklin points out that it is also possible to reach a mode where $\mu = \frac{\pi}{3}$. Although a large number of simulations were conducted in this present study, the $\mu = \pi/3$ mode was never reached for the machine used in the numerical example. The conclusion drawn was that this appeared to be an unlikely operating mode for this application, so it was not included in the analysis.

1.3 Steady State Equations

The primary goal of this section is to derive five equations that are expressed in terms of the following variables:

 β = angle at which commutation starts

μ = commutation angle

I = average field current

W = variable defined by equation (20.)

V = variable defined by equation (21.)

These equations turn out to be nonlinear with respect to β and μ , but they can be solved by some numerical method such as the Newton-Raphson algorithm. Once these variables have been found it is possible to determine the time dependent expressions for the output voltage and the current in each winding.

It is assumed that the field current consists of the constant component, \mathbf{i}_{f} , and a time varying component, \mathbf{i}_{f} ,

$$i_{f(tot)} = I_f + i_f \tag{1.}$$

The winding currents during conduction and commutation are indicated as follows,

Conduction (Interval 1-2 in Figure 2), $\beta + \mu - \pi/3 \le \theta < \beta$

$$\frac{\mathbf{i}}{\mathbf{a}} = \mathbf{i}_{\mathbf{b}} = \mathbf{0} \\
\mathbf{i}_{\mathbf{b}} = \mathbf{0} \\
\mathbf{i}_{\mathbf{f}} = \mathbf{0} \\
\mathbf{i}_{\mathbf{f}} = \mathbf{0} \\
\mathbf{i}_{\mathbf{d}} = \mathbf{0} \\
\mathbf{i}_{\mathbf{d}}$$

Commutation (Interval 2-3 in Figure 2), β $\underline{<}$ θ < β + μ

$$\underline{i} = \begin{bmatrix}
I_L \\
(-I_L + i_k) \\
-i_k \\
(I_f + i_f) \\
i_d \\
i_q
\end{bmatrix}$$
(3.)

The flux linkages are given by the following expression,

$$\frac{\lambda}{a}$$

$$\frac{\lambda}{b}$$

$$\lambda_{c}$$

$$\frac{\lambda}{f}$$

$$\frac{\lambda}{d}$$

$$\lambda_{q}$$
(4.)

-M _d sin0	$-M_{\rm d}\sin\left(\theta-\frac{2\pi}{3}\right)$	$-M_{\rm d} \sin (\theta - \frac{4\pi}{3})$	0	0	Ld
W _{cos}	$M_{d}\cos (\theta - \frac{2\pi}{3})$	$M_{d}\cos (\theta - \frac{4\pi}{3})$	M _{fd}	$\Gamma_{\mathbf{d}}$	0
$_{\mathrm{f}}^{\mathrm{cos}_{\theta}}$	$M_{f}\cos (\theta - \frac{2\pi}{3})$	$M_{f}\cos (\theta - \frac{4\pi}{3})$		M _{fd}	0
E G	e F	n a		$M_{d}\cos (\theta - \frac{4\pi}{3})$	$-M_{\rm d}\sin (\theta - \frac{4\pi}{3})$
es M	L a	Σ. W	$M_{\rm f} \cos (\theta - \frac{2\pi}{3})$	$M_{\rm d}\cos (\theta - \frac{2\pi}{3})$	$-M_d \sin (\theta - \frac{2\pi}{3})$
n R	E G	E.	Mcose	Mdcose	$-M_{\rm d} \sin \theta$

[L] represents the inductance matrix for a superconducting alternator, as given by Kirtley in [5,6]. Note out in the above references, these equivalents account for the damper shield and are not actual windings). that L_d and M_d are the same for the equivalent direct and quadrature axis damper "windings" (as pointed

resistances are assumed to be negligible. Likewise, λf may be assumed constant if I_f is supplied by The d and q windings are short circuited, implying that Ad and Aq are constant since the winding a low impedance source. Therefore,

Figure 2 indicates that,

$$v_o = v_{ab} = -\omega \frac{d}{d\theta} \left[\lambda_a - \lambda_b \right], \beta + \mu - \pi/3 < \omega t < \beta + \mu$$
 (7.)

The average voltage, V_{L} , at the output of the rectifier bridge is,

$$V_{L} = \frac{3}{\pi} \left[\int_{\beta+\mu-\pi/3}^{\beta} d\theta + \int_{\beta}^{\beta+\mu} v_{023} d\theta \right]$$
 (8.)

where v_{012} and v_{023} represent the output voltage functions over 1-2 and 2-3 respectively.

$$V_{L} = -\frac{3\omega}{\pi} \left[\int_{\beta+\mu-\pi/3}^{\beta} \left[\frac{d\lambda}{d\theta} - \frac{d\lambda}{d\theta} \right]_{12} d\theta + \int_{\beta}^{\beta+\mu} \left[\frac{d\lambda}{d\theta} - \frac{d\lambda}{d\theta} \right]_{23} d\theta \right]$$
(9.)

Figure 2 indicates

$$v_{012} = v_{023} @ \theta = \beta$$
 (10.)

$$V_{L} = -\frac{3\omega}{\pi} \left[(\lambda_{a} - \lambda_{b})_{23} \Big|_{(\beta+\mu)} - (\lambda_{a} - \lambda_{b})_{12} \Big|_{(\beta+\mu-\pi/3)} \right]$$
 (11.)

(2.) and (3.) become the same when $i_k = 0$, therefore using (3.) and (5.),

$$\lambda_{q} = -\sqrt{3} I_{L}^{M} d^{\sin(\theta + \pi/6)} + \sqrt{3} i_{k}^{M} d^{\cos\theta} + i_{q}^{L} d$$
 (12.)

where $i_k = 0$ over the conduction interval.

 $\lambda_{\rm q}$ is assumed to be constant over 1-3. At θ = $\beta+\mu-\pi/3$ we have i $_{\rm q}$ = i $_{\rm qo}$, i $_{\rm k}$ = 0.

$$\lambda_{q} (\beta + \mu - \pi/3) = -\sqrt{3} I_{L}^{M} d^{\sin(\beta + \mu - \pi/6)} + i_{qo} L_{d}$$
 (13.)

$$i_{q} = -\sqrt{3} I_{L_{q}}^{K} [\sin(\beta + \mu - \pi/6) - \sin(\theta + \pi/6)] - \sqrt{3} i_{k_{q}}^{K} \cos\theta + i_{q_{0}}$$
 (14.)

where
$$K_q = M_d/L_d$$
 (15.)

Using a similar procedure, expressions for λ_f and λ_d may be determined. The two simultaneous equations for λ_f and λ_d may then be solved for i_f and i_d ,

$$i_d = \sqrt{3} I_L K_d [\cos (\beta + \mu - \pi/6) - \cos (\theta + \pi/6)] - \sqrt{3} i_k K_d \sin \theta + i_{do}$$
 (16.)

$$i_f = \sqrt{3} I_L K_f [\cos (\beta + \mu - \pi/6) - \cos (\theta + \pi/6)] - \sqrt{3} i_k K_f \sin \theta + i_{fo}$$
 (17.)

where
$$K_f = \frac{M_f L_d - M_d M_{fd}}{L_f L_d - (M_{fd})^2}$$
, $K_d = \frac{M_d L_f - M_f M_{fd}}{L_f L_d - (M_{fd})^2}$ (18.)

As pointed out by Shilling [15], the rotor currents are periodic with respect to the 6th harmonic; therefore,

$$\int_{\beta+\mu}^{\beta+\mu} \mathbf{i}_{\mathbf{f}} d\theta = \int_{\mathbf{d}}^{\beta+\mu} \mathbf{i}_{\mathbf{d}} d\theta = \int_{\mathbf{q}}^{\beta+\mu} \mathbf{i}_{\mathbf{q}} d\theta = 0$$

$$\beta+\mu-\pi/3 \qquad \beta+\mu-\pi/3 \qquad \beta+\mu-\pi/3$$
(19.)

Since $i_k = 0$ for $\beta + \mu - \frac{\pi}{3} < \theta \le \beta$, we may define the following constants

$$W = \int_{\beta}^{\beta+\mu} i_{k} \sin\theta \ d\theta \tag{20.}$$

$$V \equiv {}_{\beta} \int^{\beta+\mu} i_{k} \cos\theta d\theta \qquad (21.)$$

Integrating (14.), (16.) and (17.) over $\beta+\mu-\frac{\pi}{3} < \theta < \beta+\mu$ and solving

for i go, i do and i fo produces,

$$i_{qo} = \sqrt{3} I_{L} K_{q} \left[\sin (\beta + \mu - \pi/6) - \frac{3}{\pi} \sin (\beta + \mu) \right] + \frac{3\sqrt{3}}{\pi} K_{q} V$$
 (22.)

$$i_{do} = -\sqrt{3} I_{L}K_{d} \left[\cos \left(\beta + \mu - \pi/6\right) - \frac{3}{\pi} \cos \left(\beta + \mu\right)\right] + \frac{3\sqrt{3}}{\pi} K_{d} W$$
 (23.)

$$i_{fo} = i_{do} \left(\frac{K_f}{K_d}\right) \tag{24.}$$

Therefore, substituting into (14.), (16.) and (17.),

$$i_{q} = \sqrt{3} K_{q} \left\{ \frac{3}{\pi} \left[V - I_{L} \sin (\beta + \mu) \right] + \left[I_{L} \sin (\theta + \pi/6) - i_{k} \cos (\theta) \right] \right\}$$
 (25.)

$$i_{d} = \sqrt{3} K_{d} \left\{ \frac{3}{\pi} \left[W + I_{L} \cos (\beta + \mu) \right] - \left[I_{L} \cos (\theta + \pi/6) + i_{k} \sin (\theta) \right] \right\}$$
 (26.)

$$i_f = i_d \left(\frac{\kappa_f}{\kappa_d}\right) \tag{27.}$$

Drom (4.), we have,

$$\lambda_a = I_L (L_a + M_a) + [(I_f + i_f) M_f + i_d M_d] \cos\theta - i_q M_d \sin\theta$$
 (28.)

$$\lambda_{b} = -I_{L} (L_{a} + M_{a}) + i_{k} (L_{a} + M_{a}) + [(I_{f} + i_{f}) M_{f} + i_{d} M_{d}]$$

$$\cos (\theta - \frac{2\pi}{3}) - i_q M_d \sin (\theta - \frac{2\pi}{3})$$
 (29.)

$$\lambda_{c} = -i_{k} (L_{a} + M_{a}) + [(I_{f} + i_{f}) M_{f} + i_{d} M_{d}] \cos (\theta - \frac{4\pi}{3})$$

$$-i_{q}^{M} \sin \left(\theta - \frac{4\pi}{3}\right) \tag{30.}$$

Using the results of (25.) - (27.),

$$(I_{f} + i_{f}) M_{f} + i_{d}M_{d} = I_{f}M_{f} + \frac{3\sqrt{3}}{\pi} M_{o} W - \sqrt{3} I_{L} M_{o} [\cos (\theta + \pi/6)] - \frac{3}{\pi} \cos (\theta + \mu)] - \sqrt{3} i_{k} M_{o} \sin \theta$$
(31.)

$$i_{q}^{M} = \frac{3\sqrt{3}}{\pi} M_{oo} V + \sqrt{3} I_{L}^{M}_{oo} \left[\sin(\theta + \pi/6) - \frac{3}{\pi} \sin(\theta + \mu) \right]$$

$$- \sqrt{3} i_{k}^{M}_{oo} \cos \theta$$
(32.)

where,
$$M_o = (K_f M_f + K_d M_d) = \frac{M_f^2 L_d + M_d^2 L_f - 2M_d M_f M_{fd}}{L_d L_f - (M_{fd})^2}$$
 (33.)

$$M_{oo} = K_{q}M_{d} = \frac{M_{d}^{2}}{L_{d}}$$
 (34.)

(11.) can be used to find $V_{\underline{I}}$, by noting that

$$i_k = I_L @ \theta = \beta + \mu$$

 $i_k = 0 @ \theta = \beta + \mu - \pi/3$,

$$V_{L} = \frac{3\omega}{\pi} \left\{ \frac{3}{4} I_{L} \Delta_{o} + \frac{3}{2} I_{L} \Delta_{d} \cos (2\beta + 2\mu + \pi/3) + \sqrt{3} I_{f}^{M} \sin(\beta + \mu) + \frac{9}{2\pi} I_{L} \Delta_{d} \sin (2\beta + 2\mu) + \frac{9}{\pi} \left[M_{o}^{M} \sin(\beta + \mu) + M_{oo}^{M} V \cos(\beta + \mu) \right] \right\}$$
(35.)

where,
$$\Lambda_{f} = (M_{o} + M_{oo}), \Lambda_{d} = (M_{o} - M_{oo})$$

$$\Delta_{o} = \frac{4}{3}(L_{a} + M_{a}) - \Lambda_{f}$$
(36.)

The current i_k exists only during the commutation period where the "b" and "c" phases are shorted together, i.e.,

$$v_{bc} = 0, \beta - \theta - \beta + \mu$$

$$(\lambda_b - \lambda_c) = constant, \beta \le \theta \le \beta + \mu$$

For $\theta = \beta$, $i_k = 0$, therefore setting $(\lambda_b - \lambda_c)_{\theta} = (\lambda_b - \lambda_c)_{\beta}$ one obtains,

$$i_{k} = \frac{1}{\left[\Delta_{o} + \Lambda_{d}\cos(2\theta)\right]} \left[\frac{2MfI_{f}}{\sqrt{3}} \left(\sin\beta - \sin\theta\right) + \frac{6}{\pi} M_{o}W(\sin\beta - \sin\theta)\right]$$

$$+ \frac{6}{\pi} M_{OO} V (\cos\beta - \cos\theta) + \frac{3I_L \Lambda_d}{\pi} [\sin(2\beta + \mu) - \sin(\beta + \mu + \theta)]$$

$$- \frac{3I_L \Lambda_f}{\pi} [\sin\mu + \sin(\theta - \beta - \mu)] - I_L \Lambda_d [\cos(2\beta - \pi/3) - \cos(2\theta - \pi/3)]$$

$$(37.)$$

Again utilizing,

$$v_{bc} = 0, \beta - \theta - \beta + \mu$$

we have for $i_k = 0 @ \theta = \beta$,

$$(v_b - v_c)_{\beta} = -\omega \frac{d}{d\theta} (\lambda_b - \lambda_c)_{\beta} = 0$$
 (38.)

which leads to,

$$-\Lambda_{\rm d} \sin (2\beta - \pi/3) = \frac{1}{\sqrt{3}} \frac{I_{\rm f}}{I_{\rm L}} M_{\rm f} \cos \beta + \frac{3}{\pi I_{\rm L}} (M_{\rm o} W \cos \beta - M_{\rm oo} V \sin \beta) + \frac{3}{2\pi} [\Lambda_{\rm d} \cos (2\beta + \mu) + \Lambda_{\rm f} \cos \mu]$$
(39.)

Utilizing $i_k = I_L @ \theta = \beta + \mu \text{ in (37.) leads to,}$

$$\Delta_{o} + 2\Lambda_{d} \cos(2\beta + \mu) \cos(\mu + \pi/3) = -\frac{4}{\sqrt{3}} \frac{I_{f}}{I_{L}} M_{f} \left[\cos(\beta + \frac{\mu}{2}) \sin(\frac{\mu}{2})\right] + \frac{6}{\pi I_{L}} \left[M_{o}W(\sin\beta - \sin(\beta + \mu)) + M_{oo}V(\cos\beta - \cos(\beta + \mu))\right] - \frac{3}{\pi} \left[2\Lambda_{d} \cos(2\beta + \frac{3\mu}{2})\sin(\frac{\mu}{2}) + \Lambda_{f}\sin(\mu)\right]$$
(40.)

One could substitute (37.) into (20.) and (21.) and integrate to find two more equations, which along with (35.), (39.) and (40.) would yield five nonlinear equations for the five unknowns, I_f , β , μ , V and W. This process is simplified considerably by use of the following approximation,

$$\Lambda_{\rm d} \simeq 0$$
, (i.e., $M_{\rm o} \simeq M_{\rm oo}$) (41.)

Equations (35.), (37.), (39.) and (40.) indicate that $\Lambda_{\rm d}$ always appears in conjunction with $\Lambda_{\rm f}$ or $\Delta_{\rm o}$. Therefore, (41.) is acceptable if $\Lambda_{\rm d}$ is small in comparison to $\Lambda_{\rm f}$ and $\Delta_{\rm o}$.

The superconducting alternator considered in this study (the same machine described by McCabria, et al., in [13,14] has the following parameters:

$$L_f = 1.2 \text{ H.}$$
 $M_f = 7.9 \times 10^{-3} \text{H.}$ $L_d = 8.2 \times 10^{-8} \text{H.}$ $M_{fd} = 1.9 \times 10^{-4} \text{H.}$ $M_{a} = 3.8 \times 10^{-6} \text{H.}$ $M_{a} = 1.5 \times 10^{-4} \text{H.}$

$$\Lambda_{d} = 0.01 \times 10^{-4} \text{ H.}, \Lambda_{f} = 3.5 \times 10^{-4} \text{ H.}, \Lambda_{o} = 2.5 \times 10^{-4} \text{ H.}$$
 (43.)

Therefore the approximation given by (41.) appears to be acceptable, at least for this particular example.

Using (41.), equations (20.), (21.), (35.), (39.) and (40.) reduce to,

$$0 = \Delta_{O}W + A (\cos (\beta + \mu) - \cos \beta) + \frac{B}{4} (2\mu - \sin(2\beta + 2\mu) + \sin 2\beta) + \frac{C}{2} (\sin^{2}(\beta + \mu) - \sin^{2}\beta)$$
(44.)

$$0 = \Delta_{O}V + A(\sin\beta - \sin(\beta + \mu)) + \frac{B}{2}(\sin^{2}(\beta + \mu) - \sin^{2}\beta) + \frac{C}{4}(2\mu + \sin(2\beta + 2\mu) - \sin(2\beta))$$
(45.)

$$0 = -V_{L} + \frac{3\omega}{\pi} \left[\frac{3}{4} I_{L} \Delta_{o} + \sqrt{3} I_{f}^{M} \sin (\beta + \mu) + \frac{9M_{oo}}{\pi} (W \sin (\beta + \mu) + V \cos (\beta + \mu)) \right]$$
(46.)

These parameters were supplied by H. Southall of the U.S. Air Force Aero Propulsion Laboratory.

$$0 = \frac{I_{f}}{\sqrt{3} I_{L}} M_{f} \cos \beta + \frac{3M_{OO}}{\pi I_{L}} (W \cos \beta - V \sin \beta) + \frac{3}{\pi} M_{OO} \cos \mu$$
 (47.)

$$0 = -\Delta_{o} - \frac{4 I_{f}}{\sqrt{3} I_{L}} M_{f} \cos (\beta + \frac{\mu}{2}) \sin (\frac{\mu}{2}) - \frac{6 M_{oo}}{\pi} \sin \mu + \frac{6 M_{oo}}{\pi I_{L}}.$$

$$[W (\sin \beta - \sin (\beta + \mu)) + V (\cos \beta - \cos (\beta + \mu))]$$
 (48.)

where

$$A = \frac{2}{\sqrt{3}} I_f M_f \sin \beta + \frac{6 M_{OO}}{\pi} (W \sin \beta + V \cos \beta - I_L \sin \mu)$$
 (49.)

$$B = \frac{2}{\sqrt{3}} I_{f}^{M} f + \frac{6}{\pi} M_{OO} (W + I_{L} \cos (\beta + \mu))$$
 (50.)

$$C = \frac{6 \text{ M}}{\pi} \left(V - I_{L} \sin \left(\beta + \mu \right) \right) \tag{51.}$$

(44.) - (48.) provide five nonlinear equations which are functions of the variables I_f , β , μ , V and W. Actually, these equations are linear with respect to I_f , V and W so it would be possible to eliminate these variables and have a set of two equations which are functions of β and μ . The equations involved in this reduction are quite cumbersome however, so one might as well work directly with (44.) - (48.).

1.4 Solution for I_f , β , μ , V and W

Rewriting the variables and equations in matrix form,

$$\underline{\mathbf{x}} \qquad \equiv \qquad \begin{bmatrix} \beta \\ \mu \\ \mathbf{I_f} \\ \mathbf{V} \\ \mathbf{W} \end{bmatrix} \tag{52.}$$

$$f(x) \equiv R.H.S. \text{ of}$$

$$(44.)$$

$$(45.)$$

$$(46.)$$

$$(47.)$$

$$(48.)$$

Jacobian matrix
$$\equiv F(\underline{x}) \equiv \frac{\partial \underline{f}(\underline{x})}{\partial \underline{x}}$$
 (54.)

(52.) - (54.) can be used to form the standard Newton-Raphson equation,

$$F\left(\underline{x}_{0}\right)\left(\underline{x}-\underline{x}_{0}\right)=\underline{f}\left(\underline{x}\right)-\underline{f}\left(\underline{x}_{0}\right) \tag{55.}$$

where \underline{x}_{0} is some initial starting point which must be reasonably close to the desired \underline{x} . In this case $\underline{f}(\underline{x}) = \underline{0}$, so we have,

$$F\left(\underline{x}_{0}\right)\left(\underline{x}-\underline{x}_{0}\right)=-\underline{f}\left(\underline{x}_{0}\right) \tag{56.}$$

It remains to find a satisfactory value for \underline{x}_0 . This is accomplished by making use of the linearization suggested by Franklin¹,

$$i_k \simeq (\theta - \beta) \frac{I_L}{\mu}$$
 (57.)

Substituting (57.) into (20.) and (21.) gives the result,

$$W = -I_{L} \cos (\beta + \mu) + \frac{2 I_{L} \sin (\mu/2) \cos (\beta + \mu/2)}{\mu}$$
 (58.)

Actually, Franklin uses a "K factor" as mentioned in the Introduction, where 0.5 $\stackrel{<}{-}$ K $\stackrel{<}{-}$ 0.9. This produces the approximation, $i_k \simeq K(\theta-\beta) \frac{I_L}{\mu}$. Since (57.) is only used to find a starting point for the Newton-Raphson algorithm, K is not critical, and K = 1.0 is used.

$$V = I_{L} \sin (\beta + \mu) - \frac{2 I_{L} \sin (\mu/2) \cos (\beta + \mu/2)}{\mu}$$
 (59.)

After substituting (57.) - (59.) into (35.), (39.) and (40.) and performing some rather laborious calculations, one obtains,

$$\mu = \cos^{-1} \left[\frac{4\pi V_L - 9\omega I_L^{\Delta}}{4\pi V_L + 9\omega I_L^{\Delta}} \right]$$
 (60.)

$$\beta = \tan^{-1} \left[\frac{\pi \Delta_0 \mu + 12 M_{00} (\sin \frac{\mu}{2})^2 (1 - \cos \mu)}{12 M_{00} \sin (\mu/2) \cos (\frac{\mu}{2}) (1 - \cos \mu)} \right]$$
(61.)

$$I_{f} = \frac{1}{\sqrt{3} M_{f} \sin (\beta + \mu)} \left[\frac{\pi V_{L}}{3\omega} - \frac{3}{4} I_{L} \Delta_{O} - \frac{18 I_{L} M_{OO}}{\pi \mu} (\sin \frac{\mu}{2})^{2} \right]$$
(62.)

(58.) - (62.) provide a value of \underline{x}_0 which produces convergence within three or four iterations, depending on the convergence tolerance.

1.5 Numerical Results

This example is based on the same 4 pole, 400 Hz, 10 MVA/5kV superconducting alternator described by McCabria, et al. in [13,14]. When operating into a bridge rectifier at full load with a large filter inductance, this system will have the output values (see [24]),

$$V_{L} = 6760 \text{ V. dc}$$

$$I_{L} = 1420 \text{ A. dc}$$
(64.)

The following results assume that the system is operating with a closed loop controller, i.e., $\mathbf{I}_{\mathbf{f}}$ is varied to maintain a constant $\mathbf{V}_{\mathbf{L}}$.

The inductance parameters for this machine are indicated in (42.). All data is presented in terms of the actual magnitudes, but a per unit system would serve just as well.

If vs. II:

Figure 3. shows I_f vs. I_L , where I_f is varied to maintain a constant V_L . As seen from the curve, the variation in I_f is approximately linear up to 200% of the full load value of I_L .

 β and μ vs. I_L :

Figures 4. and 5. indicate the variation in β and μ respectively with respect to $I_{\rm L}.$ Figure 5. indicates that μ remains less than 60^{o} as mentioned earlier.

Harmonic Content of v_o vs. I_L :

One of the more important problems in this type of power system is the weight of the output filter (L_{o} and C_{o} as shown in Figure 1.). In order to minimize the combined weight of these components it is necessary to know the harmonic content of v_{o} under all load conditions. The output voltage is obtained from (7.) by substitution:

Conduction period (i_k = 0), β + μ - $\pi/3$ < θ \leq β ,

$$v_{012} = \omega (\sqrt{3} I_{f} M_{f} + \frac{9}{\pi} M_{oo} W) \sin (\theta + \pi/6) + \frac{9\omega}{\pi} M_{oo} V \cos (\theta + \pi/6) + \frac{9\omega I_{L} M_{oo}}{\pi} \sin (\theta + \pi/6 - \beta - \mu)$$
(65.)

Commutation period (i_k \neq 0), β < θ \leq β + μ ,

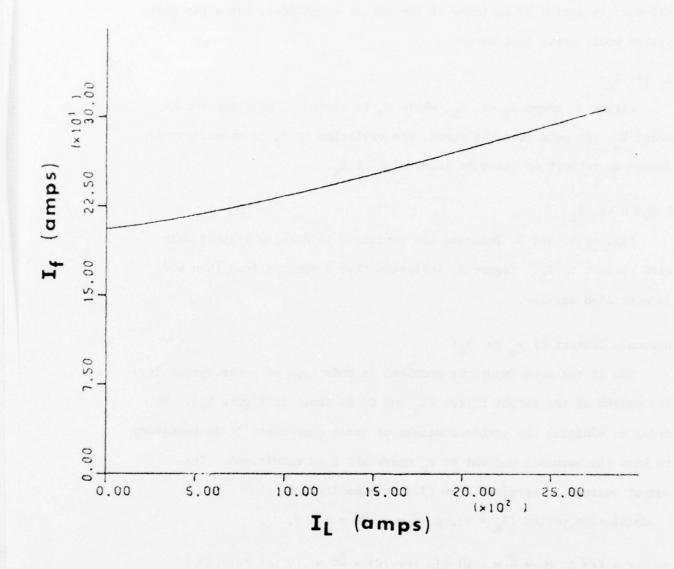


Figure 3. I_f versus I_L with Uncontrolled Rectifier Bridge.

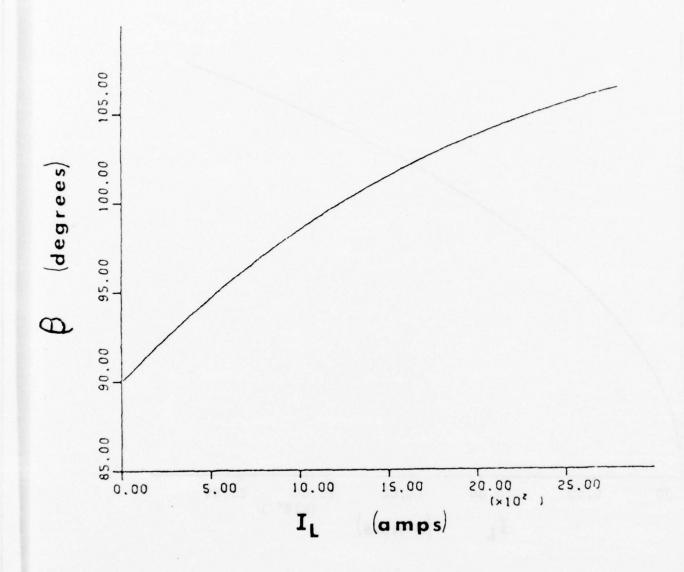


Figure 4. β versus I_L with Uncontrolled Rectifier Bridge.

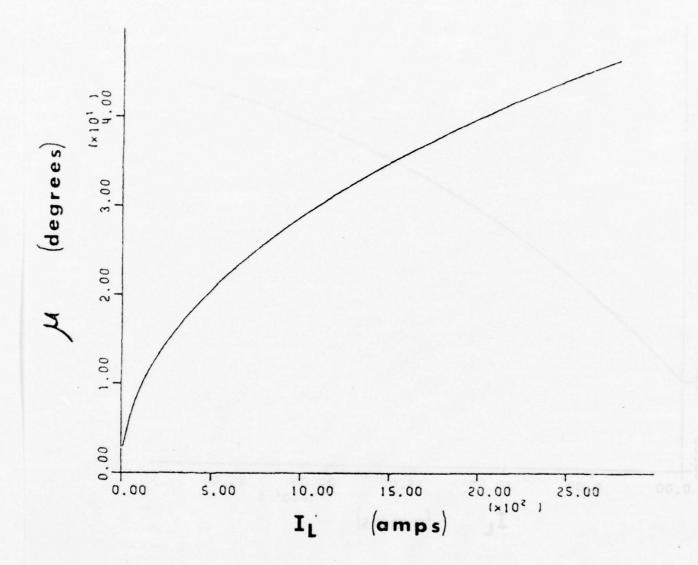


Figure 5. μ versus I_L with Uncontrolled Rectifier Bridge.

$$v_{o23} = v_{o12} + \frac{\omega}{\Delta_o} \left(\frac{3M_{o0}}{2} - L_a - M_a \right) \left[\left(\frac{2M_f I_f}{\sqrt{3}} + \frac{6M_o W}{\pi} \right) \cos \theta \right]$$
$$- \frac{6M_o V}{\pi} \sin\theta + \frac{6I_c M_o}{\pi} \cos (\theta - \beta - \mu) \right]$$
(66.)

The Fourier series for v_0 is given by,

$$v_0 = V_L + \sum_{n=6}^{\infty} a_n \cos(n\omega t) + \sum_{n=6}^{\infty} b_n \sin(n\omega t) \quad n = 6,12,18,...$$
 (67.)

where
$$V_{L} = \frac{6}{\pi} \int_{\beta+\mu-\pi/3}^{\beta} v_{012} d\theta + \frac{6}{\pi} \int_{\beta}^{\beta+\mu} v_{023} d\theta$$
 (68.)

$$a_n = \frac{6}{\pi} \int_{\beta+\mu-\pi/3}^{\beta} v_{012} \cos(n\theta) d\theta + \frac{6}{\pi} \int_{\beta}^{\beta+\mu} v_{023} \cos(n\theta) d\theta$$
 (69.)

$$b_{n} = \frac{6}{\pi} \int_{\beta+\mu-\pi/3}^{\beta} v_{012} \sin(n\theta) d\theta + \frac{6}{\pi} \int_{\beta}^{\beta+\mu} v_{023} \sin(n\theta) d\theta$$
 (70.)

The peak value of the nth harmonic is given by,

$$c_n = (a_n^2 + b_n^2)^{1/2}$$
 (71.)

Although tedious, the evaluation of these coefficients is straightforward and will not be included here.

The peak value of the first three ac harmonics of $\mathbf{v}_{_{\mathrm{O}}}$ vs. $\mathbf{I}_{_{\mathrm{L}}}$ are indicated in Figure 6. As would be expected, the ac content is dominated by the 6th harmonic.

Variation in i_f, i_d, and i_q:

As pointed out in various references ([8] through [11], for example), one of the more critical problems in a superconducting machine is heating due to induced currents in the field winding since this may cause the field to depart from the superconducting mode. The thermal analysis

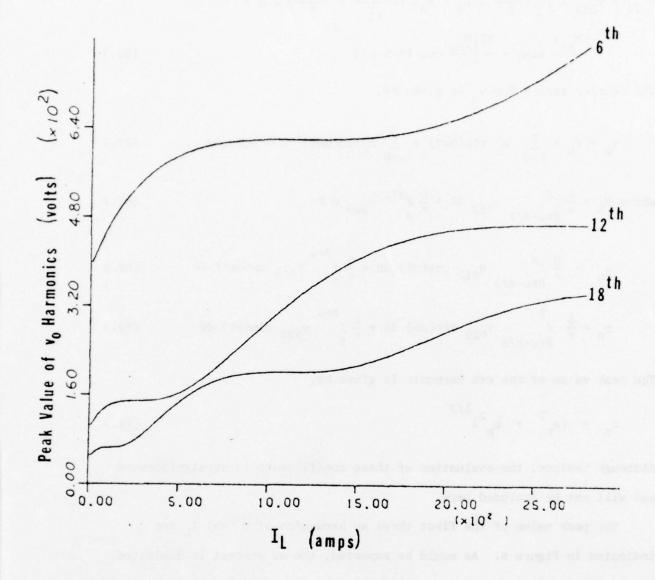


Figure 6. First Three Harmonics of $\mathbf{v}_{_{\mathrm{O}}}$ versus $\mathbf{I}_{_{\mathbf{L}}}$ with Uncontrolled Rectifier Bridge

of this winding is beyond the scope of this report, but it is certainly related to the variations in i_f . The instantaneous value of i_f is given by (27.) and plotted as a function of θ in Figure 7. The rms value of i_f was obtained by numerical integration and is shown as a function of I_L in Figure 8.

Since laboratory data on an actual rectified superconducting alternator was not available at the time of this report, it is difficult to say how these calculated variables will eventually compare with experimental results. However, an analytical review of the $i_{\rm f}$ calculations does indicate that the $i_{\rm f}$'s shown in Figures 7 and 8 may be higher than the actual values. It is believed that the reason for this is that the inductance matrix in (5.) does not fully account for the high frequency attenuation provided by the damper shield. This effect is still under investigation.

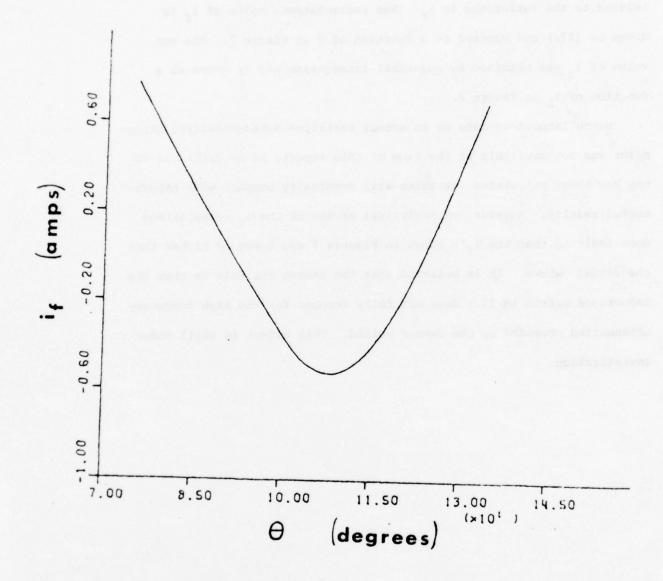


Figure 7. i_f versus θ at Full Load with Uncontrolled Rectifier Bridge. (See text for discussion of i_f calculations.)

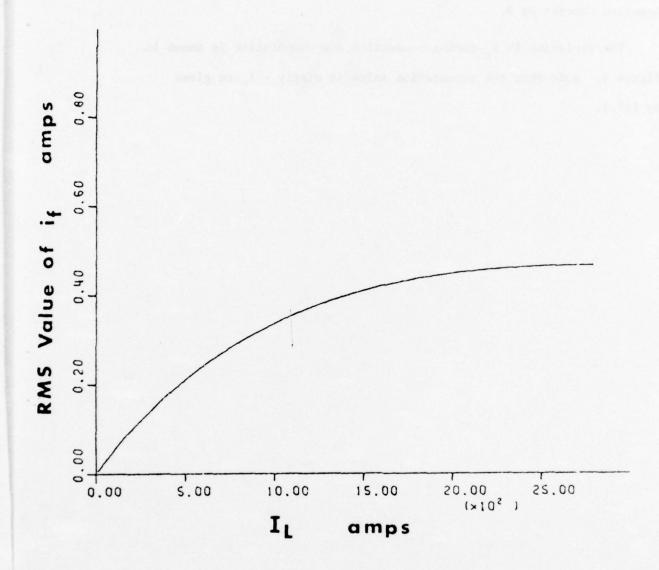


Figure 8. RMS value of i_f versus I_L with uncontrolled Rectifier Bridge. (See text for discussion of i_f calculations.)

Armature Current vs θ :

The variation in i_c during conduction and commutation is shown in Figure 9. Note that the commutation value is simply - i_k as given by (37.).

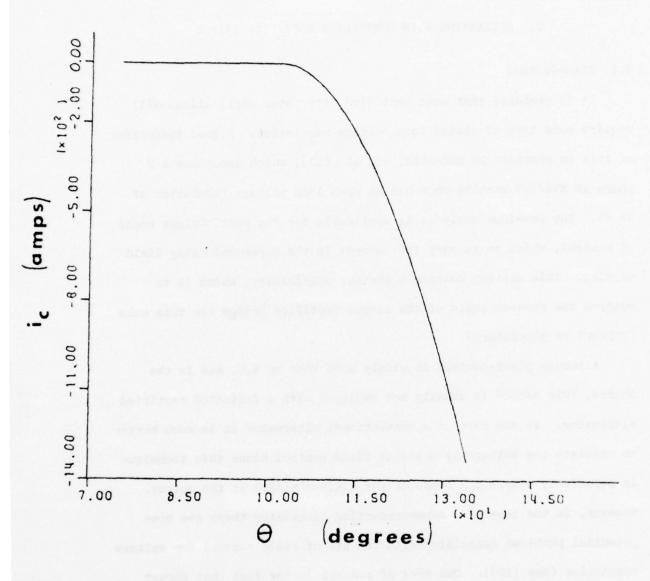


Figure 9. i_c versus θ at Full Load.

2. ALTERNATOR WITH CONTROLLED RECTIFIER BRIDGE

2.1 Introduction

It is probable that most rectified alternator applications will require some type of closed loop voltage regulation. A good indication of this is provided by McCabria, et. al. [13], which describes a 3 phase 10 MVA/5kV machine that has an open loop voltage regulation of 26.5%. The previous analysis is applicable for the most obvious means of control, which is to vary the current in the superconducting field winding. This section considers another possibility, which is to control the turn-on angle of the output rectifier bridge (in this case composed of thyristors).

Although phase-control is widely used when an A.C. bus is the source, this method is usually not employed with a dedicated rectified alternator. In the case of a conventional alternator it is much better to regulate the voltage by means of field control since this technique is relatively simple and produces the minimum ripple at the output. However, in the case of a superconducting alternator there are some potential problems associated with the use of field control for voltage regulation (see [10]). One area of concern is the fact that abrupt variations in field current may cause this winding to leave the superconducting mode. Another problem is the long time constant of the field circuit which produces a very slow step response.

The use of a phase controlled rectifier bridge on the output should provide relatively lower field current variations and a faster step re-

sponse. It also should be noted that gated devices may be required for the rectifier bridge in order to provide short circuit protection. Thus these same devices can be used to provide voltage regulation.

2.2 Steady State Model

The schematic diagram for the alternator with a controlled rectifier bridge is shown in Figure 10, and the output voltage and current waveforms are shown in Figure 11. The approximations used in this section are identical to those used for the analysis of the uncontrolled rectifier bridge.

2.3 Steady State Equations

Equations (44.) - (48.) of the previous section provide five expressions which can be solved numerically to find the variables I_f , β , μ , V and W. However, with the thyristor bridge, commutation does not start when $v_c = v_b$ but at some later time when $v_c \geq v_b$, i.e., β is controlled externally to produce the desired V_L . This means that (47.) no longer applies since it is based on $v_c = v_b$ at $\theta = \beta$.

Therefore, there are only four equations to work with, (44.), (45.), (46.) and (48.), and I_f is held constant slightly above the minimum value required for maximum I_L .

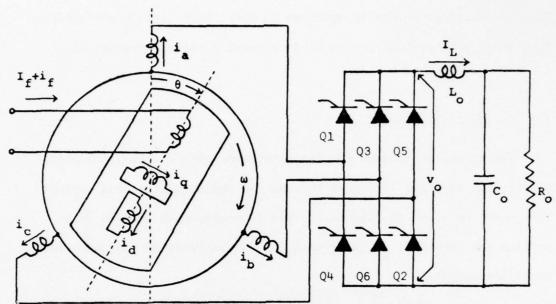


Figure 10. Equivalent Circuit for the Superconducting Alternator with Controlled Rectifier Bridge.

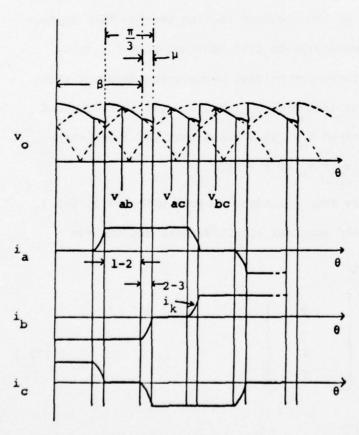


Figure 11. Output voltage and armature currents for the alternator with controlled rectifier bridge.

$$\underline{f'}(\underline{x'}) \equiv R.H.S. \text{ of}$$

$$(44.)$$

$$(45.)$$

$$(46.)$$

$$(48.)$$

A solution for \underline{x}' can be obtained from the standard Newton-Raphson equation,

$$F(\underline{x}') (\underline{x}' - x') = \underline{f}' (\underline{x}') - \underline{f}' (\underline{x}')$$
 (74.)

where \underline{x}_0' is some initial starting point sufficiently close to \underline{x}' and,

$$F(\underline{x'}) = \text{the Jacobian matrix} = \frac{\partial \underline{f'(\underline{x'})}}{\partial \underline{x'}} \Big|_{\underline{x'} = \underline{x'}}$$
(75.)

A satisfactory value for \underline{x}'_0 is obtained by using the previous diode bridge solution, \underline{x} , where I_f is a variable, or by using the approximate method reported by Franklin in [17,18].

2.4 Numerical Results

This numerical example is based on the same 4 pole, 400 Hz., 10 MVA/5kV superconducting machine used in the previous example. The same full load conditions are assumed,

$$V_{L} = 6760 \text{ V.D.C.}$$

$$I_{L} = 1420 \text{ A.D.C.}$$
(76.)

The minimum value of I_f that will produce I_L = 1420A corresponds to the solution for the uncontrolled rectifier bridge (i.e., minimum β). This current is found from the first section,

$$I_{f(min.)} = 250A.$$
 (77.)

In an actual system it will be desirable to set I_f at some value above that given by (77.). This will insure against low voltage if I_f decreases for any reason. For this example, the high value, $I_{f(max.)}$, was arbitrarily taken to be,

$$I_{f(max.)} = 1.1 I_{f(min.)}$$
 (78.)

A plot of I_f vs. I_L for both the controlled and uncontrolled rectifier bridge is shown in Figure 12.

 β , μ , the first three harmonics of v_o , and the rms value of i_f are plotted vs. I_L in Figures 13 through 18 respectively. Note that the corresponding values for the diode bridge case are included for reference purposes.

As would be expected, Figure 13 indicates that the thyristor bridge β must exceed the diode bridge β to compensate for the higher I_f . The thyristor bridge β also drops as I_L increases in order to compensate for the higher voltage drop across the armature windings.

Figure 14 reveals an interesting characteristic in that the μ for the thyristor bridge is considerably less than the μ for the diode bridge. This is not too surprising when Figures 10 and 11 are considered. Referring to these figures, it is observed that because of the delayed β_1 commutation from b to c does not start until $\mathbf{v}_{bc} > 0$. Therefore, more voltage is present to force the commutation process than in the diode case where commutation begins at $\mathbf{v}_{bc} = 0$. Because of this higher \mathbf{v}_{bc} , \mathbf{i}_b will be driven to zero in less time, thus producing a smaller μ for the thyristor case.

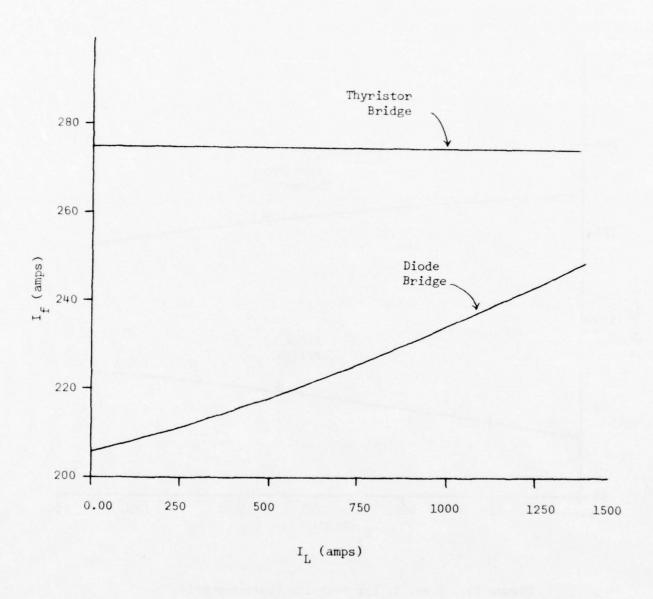


Figure 12. I_f vs. I_L for both the thyristor bridge and the diode bridge.

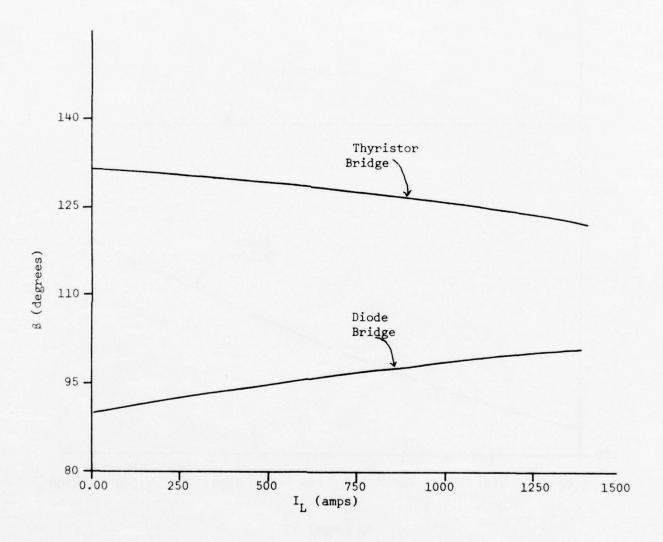


Figure 13. β vs. I_L for both the thyristor bridge and the diode bridge.

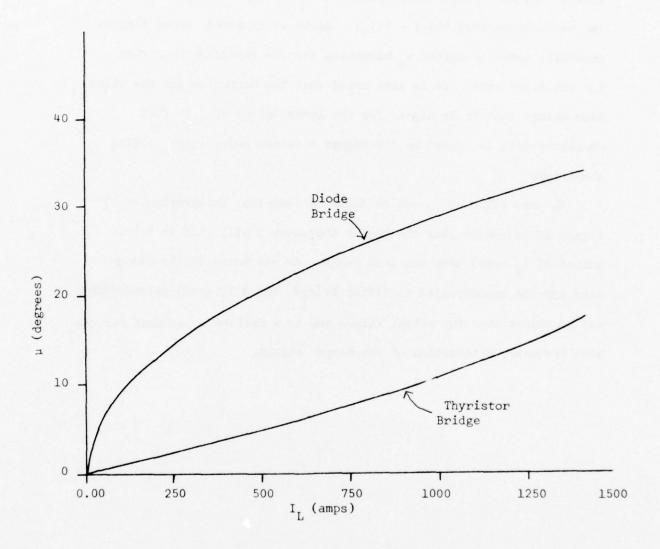


Figure 14. μ vs. I for both the thyristor bridge and the diode bridge.

The voltage harmonics shown in Figure 15 to 17 are obtained by calculating the Fourier coefficients of the output voltage, v_o , which can be obtained from (65.) - (71.). Again as expected, those figures generally indicate higher v_o harmonics for the thyristor case than for the diode case. It is also noted that the harmonics for the thyristor bridge tend to be higher for the lower values of I_L . This characteristic is caused by the higher β values under light loading conditions.

The rms value of i_f can be found by numerical integration of (27.). Figure 18 indicates that the higher thyristor β will lead to higher values of i_f (rms) over the load range. As was noted in the discussion for the uncontrolled rectifier bridge, these i_f (rms) calculations may be higher than the actual values due to a failure to account for the high frequency attenuation of the damper shield.

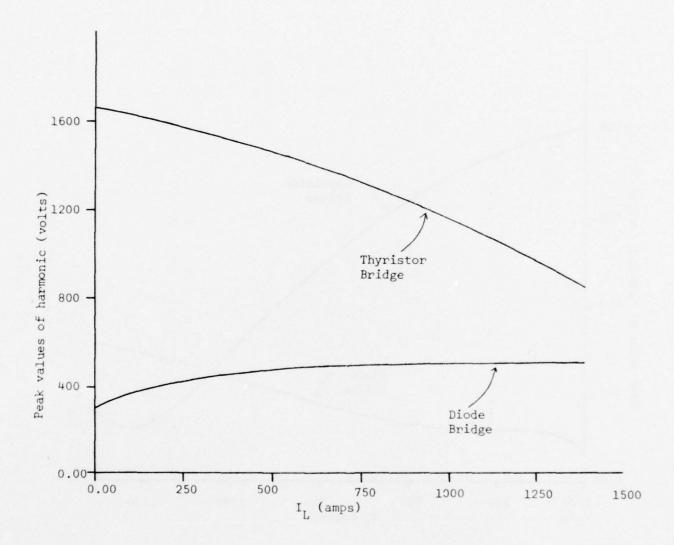


Figure 15. 6th harmonic of \mathbf{v}_{o} vs. \mathbf{I}_{L} for both the thyristor bridge and the diode bridge.

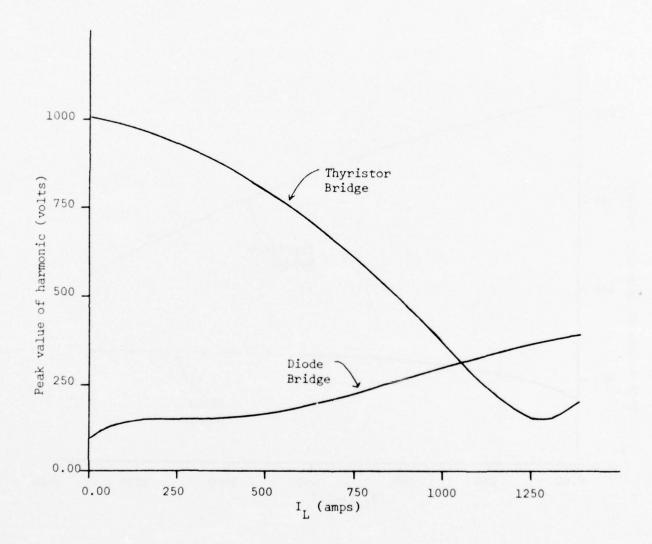


Figure 16. 12th harmonic of ${\bf v}_{\rm o}$ vs. ${\bf I}_{\rm L}$ for both the thyristor bridge and the diode bridge.

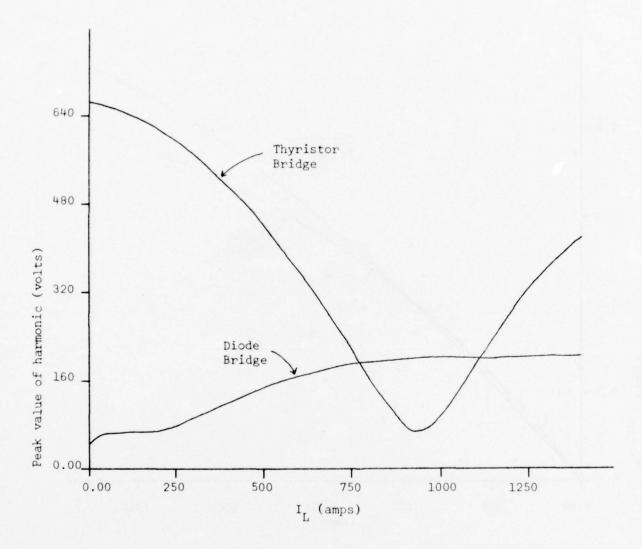


Figure 17. 18th harmonic of ${\rm v}_{\rm o}$ vs. ${\rm I}_{\rm L}$ for both the thyristor bridge and the diode bridge.

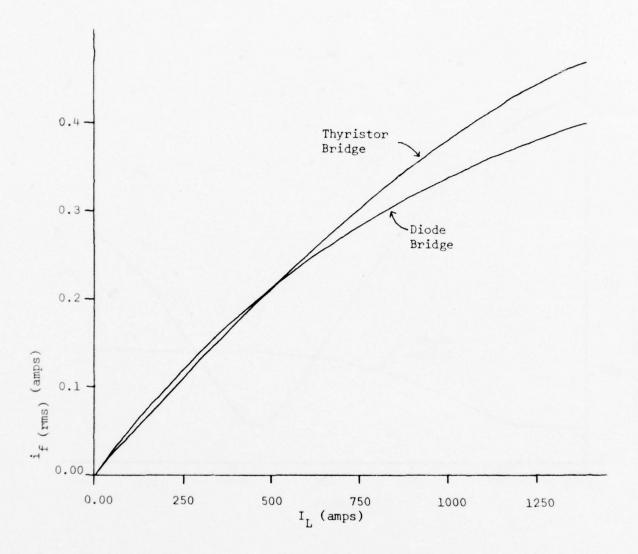


Figure 18. i_{f} (rms) vs. I_{L} for both the thyristor bridge and the diode bridge.

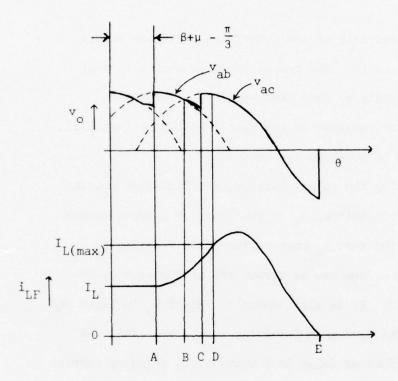
3. FAULT CURRENT CALCULATIONS

3.1 Introduction

This discussion is based only on the controlled rectifier bridge configuration shown in Figure 10. The reason for this choice is that this circuit has the capability of fast turn off in the event of a fault. Fast turn off can be achieved by the system in Figure 1 only if some type of series switch is added to the circuit.

In addition to filtering the output voltage, the inductor, $L_{_{\scriptsize O}}$, in Figure 10 must be capable of limiting $I_{_{\scriptsize L}}$ in the event of a short across the load. The length of time that $L_{_{\scriptsize O}}$ must perform this function is limited however, since the bridge can be turned off on the next cycle after the fault is detected. It is also common to select $L_{_{\scriptsize O}}$ to limit the $C_{_{\scriptsize O}}$ charging current when the system is initially turned on. This can also be accomplished by a further delay in β however, so charging current will not be used as a constraint in this analysis.

To determine if L_o is of adequate size, it will be necessary to calculate the transient load current, i_{LF} , that occurs after the fault. Since the differential equations involved have time varying coefficients, a numerical solution will be required. In this particular study it is assumed that the fault occurs at the beginning of a conduction period and that the bridge will not be turned off until this conduction period, the next commutation period, and a final conduction period are complete. This corresponds to the interval, AE, shown in Figure 19. The rationale behind this choice is that some time is required for i_{LF} to exceed $I_{L(max.)}$, at which time a current overload sensing circuit is enabled to



- A: Fault occurs at the start of a conduction period B: On-coming thyristors fire and commutation begins C: Commutation interval ends D: $I_{L(max)}$ is exceeded, next trigger signal is blanked E: i_{LF} decays to 0

Figure 19. Transient Behavior for the Controlled Rectifier Bridge.

blank all the thyristor gate signals. Other choices are certainly possible, such as assuming that the fault occurs at the start of a commutation period and that the thyristor gates are blanked before the next firing pulse.

3.2 Circuit Model and Equations

Figure 20 represents the equivalent circuit with phase "a" conducting and a short across the load. Note that the armature resistance $R_{\rm a}$ and the parasitic resistance of the filter choke, $R_{\rm p}$, have been included since they aid in limiting the fault current. The periods AB, BC, etc. in Figure 19 will correspond to the following thyristors being on:

Period	Th	nyristors (Conductin
AB, conduction BC, commutation CE, conduction		Q1, Q1, O1.	Q6, Q2

The steady state analysis has assumed that the winding resistances are negligible. That practice will be continued here for all windings except those on the armature; as before, it implies that λf , λd and λq are approximately constant over the relatively short transient period, AE, and that the voltages across the closed f, d and q windings are approximately zero.

The equations for the commutation period, BC, are found to be,

$$[A] \frac{d\underline{i}}{dt} = [B] \underline{i}$$
 (79.)

where

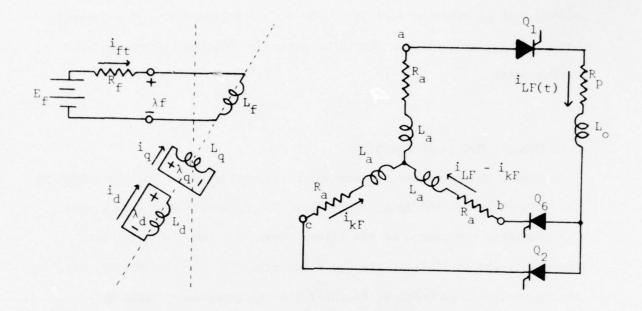


Figure 20. Equivalent circuit for conduction and commutation periods while fault is present.

$$\frac{i}{i}_{LF}$$

$$\frac{i}{f(tot)}$$

$$\frac{i}{d}$$

$$\frac{i}{q}$$

$$\frac{i}{kF}$$
(80.)

and the [A] and [B] matrices are defined in Appendix II.

The equations for the conduction period, AB, (Q2 off) can be expressed in a similar manner,

$$[A_{11}] \frac{d\underline{i}'}{dt} = [B_{11}] \underline{i}'$$
 (81.)

where $[A_{11}]$, $[B_{11}]$ and \underline{i} ' are submatrices of [A], [B] and \underline{i} . These submatrices are also defined in Appendix II.

Since the fault is assumed to occur at A in Figure 19, (81.) will be solved first, then (79.). It is unnecessary to formulate equations specifically for the second conduction period, CE, since this period can be analyzed by using (81.).

As predicted earlier, [A] and [B] have time dependent elements. This implies that <u>i</u> must be found by some numerical integration technique. The modified Euler method was chosen for this particular study, but other techniques could also be employed.

Starting with the conduction period, AB, (81.) can be solved for $\frac{d\underline{i}'}{dt}$ at each time increment, Δt , and the next value of \underline{i}' can then be found by using the standard modified Euler equations (see [27.]). This process is simplified however, if the approximation of constant λf , λd , and λq is again utilized. Writing the flux linkage equations for the most general case (the commutation period, BC), one obtains,

$$\begin{bmatrix} \lambda f \\ \lambda d \\ \lambda q \end{bmatrix} = \begin{bmatrix} \sqrt{3} & M_f & \cos (\omega t + \pi/6) \\ \sqrt{3} & M_d & \cos (\omega t + \pi/6) \\ \sqrt{3} & M_d & \sin (\omega t) \end{bmatrix}$$

$$i_{LF} + \begin{bmatrix} \sqrt{3} & M_f & \sin (\omega t) \\ \sqrt{3} & M_d & \sin (\omega t) \\ \sqrt{3} & M_d & \cos (\omega t) \end{bmatrix}$$

$$i_{kF}$$

$$(cont.)$$

$$\begin{bmatrix} L_{f} & M_{fd} & 0 \\ M_{fd} & L_{d} & 0 \\ 0 & 0 & L_{d} \end{bmatrix} \begin{bmatrix} i_{f(tot)} \\ i_{d} \\ i_{q} \end{bmatrix}$$

$$(82.)$$

or in vector notation, $\underline{\lambda}_{fdq} = \underline{x}\underline{i}_{LF} + \underline{y}\underline{i}_{kF} + [C]\underline{i}_{fdq}$. (83.) $\underline{\lambda}_{fdq}$ can be found initially by substituting the steady state values for \underline{i}_{fdq} , i_{LF} and i_{kF} at $\omega t = \beta + \mu - \pi/3$ (i.e., \underline{i}_{fdq} is found from (25.), (26.), (27.) and $i_{LF} = I_L$, $i_{kF} = 0$). At each time increment i_{LF} and i_{kF} can be found from the modified Euler equations while \underline{i}_{fdq} can be found from (83.) (using the constant value of $\underline{\lambda}_{fdq}$).

Figure 19 indicates that the firing angle is delayed before the fault, but not afterwards (point B). The reason for this is that once the output is shorted the voltage regulator will call for the minimum firing angle, and the oncoming thyristors will conduct as soon as possible. Since the load current is no longer constant, the steady state equations that yield $\beta(\min.)$ (i.e., the firing angle for an uncontrolled rectifier bridge) do not apply, and the firing angle (point B) must be found by determining the first point at which $v_{bc} \stackrel{>}{=} 0$. As v_{bc} becomes positive Q2 will start to conduct and the commutation of Q6 will commence. v_{bc} for the AB conduction state can be readily found from the bc loop,

$$v_{bc} = R_{a} i_{LF} + (L_{a} + M_{a}) \frac{di_{LF}}{dt} - \sqrt{3} \sin(\omega t) \left(M_{f} \frac{di_{f}(tot)}{dt} + M_{d} \frac{di_{d}}{dt}\right)$$

$$- \sqrt{3} M_{d} \cos(\omega t) \frac{di_{q}}{dt} - \sqrt{3} \omega \cos(\omega t) \left(M_{f} i_{f}(tot) + M_{d} i_{d}\right)$$

$$+ \sqrt{3} \omega M_{d} \sin(\omega t) i_{q}$$
(84.)

 ${
m v}_{
m bc}$ is tested at each time increment of the AB interval; at the first point where ${
m v}_{
m bc} \ge 0$ the computer program branches to the equations for the BC commutation interval. It will also be necessary to perform some test to determine when the commutation period ends at point C. This is done by comparing $i_{
m LF}$ and $i_{
m kF}$ at each time increment of the BC interval; the commutation period ends at the first point where $i_{
m kF} \ge i_{
m LF}$.

It should be noted that it may take several machine cycles to commutate the thyristors after the firing signals have been blanked. This can be illustrated conceptually by the simplified model shown in Figure 21 (this model is of little quantitative use however, since it does not account for the winding resistances and inductances of the machine). If $e_{s(t)} = v_{ab}$ and the thyristors start to conduct at $\omega t = \pi/3$ (approximate), $i_{(t)}$ will have the form,

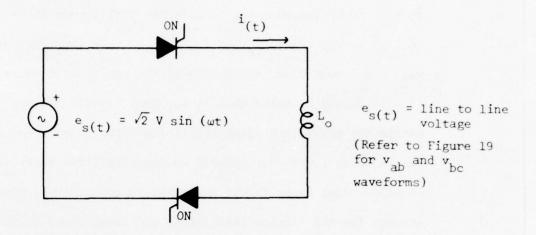
$$i_{(t)} = I_L + \frac{\sqrt{2}V}{\omega L_o} (1/2 - \cos(\omega t))$$
 (85.)

where I $_{L}$ = load current at ωt = $\pi/3.$

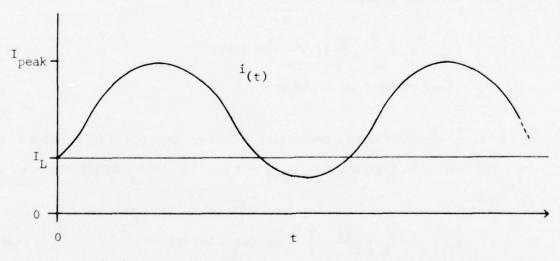
At $\omega t = \frac{2\pi}{3}$ (approximate), conduction switches from phase b to phase c so the source voltage becomes $e_{s(t)} = v_{ac}$. The load current now has the form,

$$i_{(t)} = I_L + \frac{\sqrt{2}V}{\omega L_o} (\frac{3}{2} - \cos(\omega t - 2\pi/3))$$
 (86.)

Even if the bridge is blanked during the v_{ac} cycle (to prevent the next commutation) (86.) never goes negative, meaning that the conducting thyristors will not turn off.



(a.) Simplified equivalent circuit during fault.



(b.) Fault current.

 $\frac{\text{Note:}}{\text{of } 2R_{\text{a}} + R_{\text{p}}}$ Actual waveform will be damped due to presence

Figure 21. Effect of L_{\odot} in limiting fault current.

A similar phenomenon can occur in the actual physical circuit, except that $i_{(t)}$ will eventually decay to zero due to resistive damping. This may require several cycles however, and more cycles will be required for larger values of L_o . Thus if L_o is large, several cycles may be required to complete turn off; however, if it is too small the peak fault current will be excessive.

3.3 Numerical Results

The transient analysis algorithm can be used to plot post fault current waveforms for various values of $L_{_{\rm O}}$ and $R_{_{\rm P}}$. Two parametric studies of $i_{_{\rm LF}}$ for variations in $L_{_{\rm O}}$ and $R_{_{\rm P}}$ are shown in Figures 22 and 23 respectively. Figure 24 shows a plot of $i_{_{\rm LF}}$ that requires three cycles for $i_{_{\rm LF}}$ to reach zero. Presumably commutation would occur on the fourth cycle where $i_{_{\rm LF}}$ would attempt to go negative.

This algorithm could also be used to plot $i_{f(tot)}$, i_{d} and i_{q} during a fault condition. However, as stated earlier for the steady state calculations, the $i_{f(tot)}$ values may be too high since the model does not include the high frequency attenuation of the damper shield.

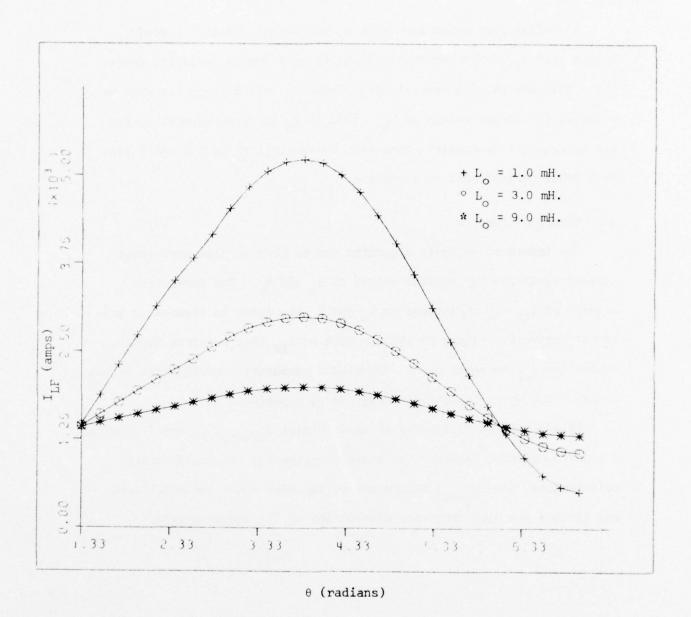


Figure 22. Fault current vs. θ for different values of L $_{o}$. R $_{p}$ = 0.05 $\!\Omega$

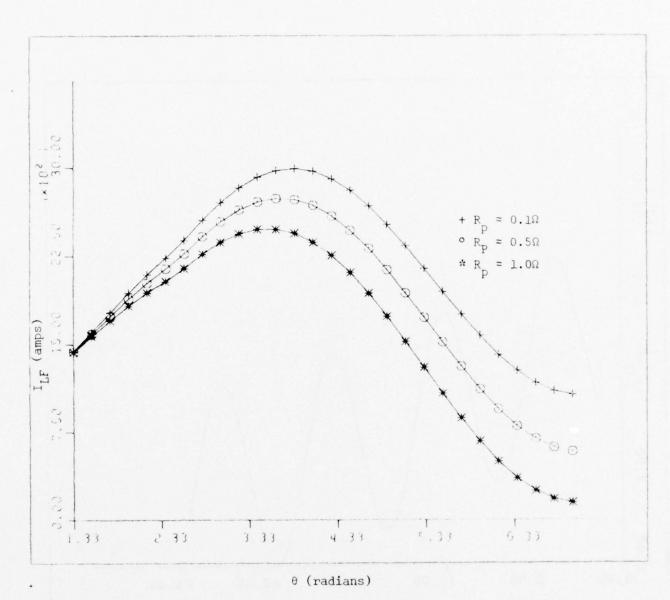
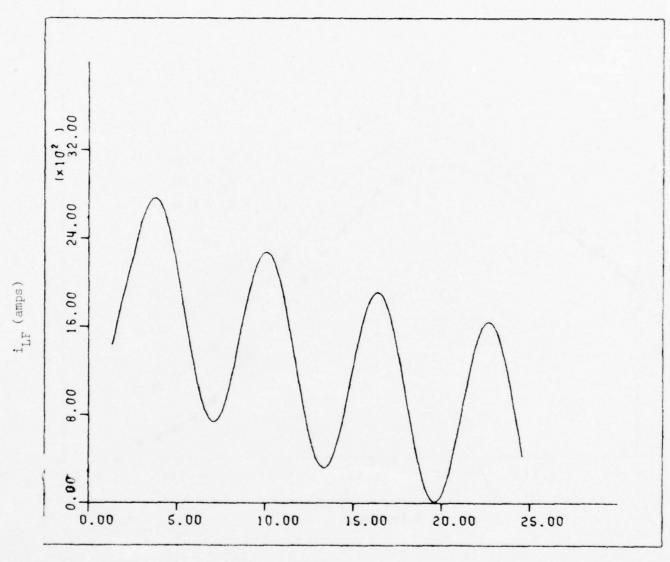


Figure 23. Fault current vs. θ for different values of R $_{\rm p}.$ L $_{\rm o}$ = 3.0 mH.



θ (radians)

Figure 24. Exponential decay of $i_{\mbox{LF}}$

4. VARIATION OF THE ALTERNATOR PARAMETERS TO DECREASE OUTPUT RIPPLE VOLTAGE

4.1 Introduction

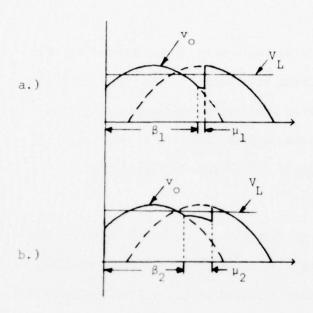
As noted previously, there are two basic methods for regulating the dc output voltage, $V_{_{\rm I}}$, of the rectified alternator:

- 1. Use an uncontrolled rectifier bridge, and regulate ${\bf V}_{\bf L}$ by controlling the average field current, ${\bf I}_{\bf f}.$
- 2. Hold I_f constant, and regulate the voltage by means of a controlled rectifier bridge.

The first method provides the minimum ripple voltage, but it tends to have a slow response time due to the long time constant of the field winding.

Therefore the analysis of this section is based on the controlled rectifier bridge.

If the alternator is modeled by an ideal ac voltage in series with an inductor, it is well known that an increase in this inductance will increase the commutation angle, μ , shown in Figure 11. For constant V_L and I_L this effect can also lead to a reduction in output ripple voltage, as illustrated in Figure 25. Comparing parts (a.) and (b.) of the figure it is seen that the same average output voltage, V_L , is achieved by different combinations of the angle, β and μ . However, the deviation of V_0 is less in part (b.). This indicates than an increase in μ requires the bridge firing angle to decrease, resulting in a more level V_0 . Therefore, the β_2 , μ_2 combination in (b.) produces a lower ripple voltage than the β_1 , μ_1 combination in (a.). This implies that at least over a limited range of μ values it is possible to decrease the ripple voltage by increasing μ . Thus for a fixed load, it is possible to decrease



 $V_{\rm L}$ = average output voltage (source inductance for (b.) is higher than that for (a.))

Figure 25. Effect of μ upon output ripple voltage for fixed $\textbf{V}_{\underline{\textbf{L}}}$ and $\textbf{I}_{\underline{\textbf{L}}}.$

the ripple by increasing the source inductance since this causes an increase in $\boldsymbol{\mu}$.

The model used in this study was considerably more complicated than the one just described, but it was found that for a constant load the ripple could be decreased if the armature inductance, L_a , was increased beyond its specified value of 0.3 mH. This implies that a lighter weight filter could be used if L_a were increased. A word of caution is in order however, since these gains may be offset by an increase in alternator weight (due to the larger L_a). Ultimately, it would be desirable to develop a procedure that would minimize the combined weight of the alternator and filter. This would require a detailed weight analysis of the superconducting alternator however, and such an effort would be beyond the scope of this present study.

4.2 Effect of L on the Output Voltage Harmonics

As discussed in the previous section, it is possible to reduce the full load ripple voltage by changing the output impedance of the alternator. The model used in this study cannot be reduced to a single ac source in series with such an impedance, but a similar effect will occur if the armature self inductance, L_a, is varied. Changes in L_a will, of course, change the armature mutual inductances. To account for this, it is assumed that the coefficient of coupling between L_a and each of the other windings, remains constant while L_a is varied, i.e.,

$$k_{af} = \frac{M_f}{\sqrt{L_a L_f}} = constant$$
 (87.)

$$k_{aa} = \frac{M_a}{L_a} = constant$$
 (88.)

$$k_{ad} = \frac{M_d}{\sqrt{L_a L_d}} = constant$$
 (89.)

(L $_{\rm f}$ and L $_{\rm d}$ also remain constant.)

4.3 Numerical Results

Since k_{af} and L_{f} are assumed constant, (87.) indicates that an increase in L_{a} will also increase M_{f} . Thus an increase in L_{a} implies that the same magnetic flux linkage from field to armature, $M_{f}I_{f}$, can be achieved with a lower I_{f} (since a thyristor bridge is used for voltage regulation it is assumed that I_{f} will be held constant at 110% of the minimum allowable value for a given L_{a} , as discussed in the section on controlled rectifiers). Figure 26 indicates the decrease in the required I_{f} as L_{a} is increased for I_{L} = 1420 A. dc. This decrease in I_{f} might allow the use of smaller superconducting wire for the rotor winding, thus decreasing the rotor size. An alternate approach would be to hold M_{f} constant and allow L_{f} to decrease as L_{a} increased; thus the field winding would have fewer turns (both effects appear small).

Figure 27 indicates that the 6th harmonic of \mathbf{v}_{o} reaches a minimum at \mathbf{L}_{a} = 0.72 mH. This leads to a decrease in the size of the output filter, \mathbf{L}_{o}^{C} , since less attenuation is required.

Break frequency =
$$f_b = \frac{1}{\sqrt{L_{00}^{C}}}$$
 (90.)

Figure 27 also indicates that the 12th and 18th harmonics generally continue to increase with $L_{\rm a}$, but their effect is less important since

filter attenuation is much greater at these frequencies. Figure 28 shows that the 6th harmonic continues to decrease as L_a increases, indicating that the optimum L_a at 40% of full load lies somewhere above 0.9 mH. Thus the optimum L_a is different for different values of I_L .

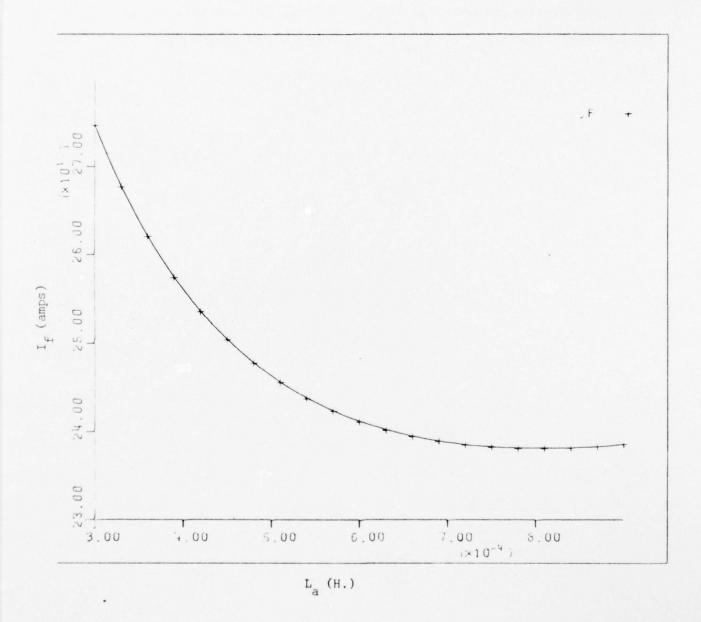
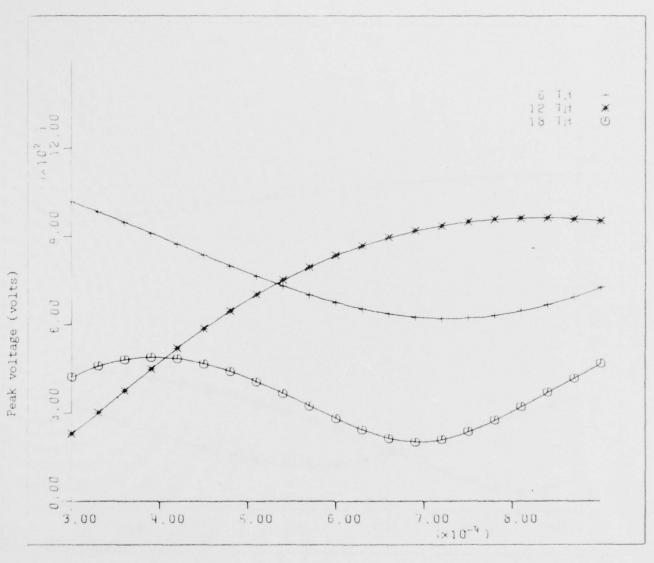


Figure 26. I_f vs. L_a for the controlled rectifier bridge. I_L = 1420 A.d.c.



L_a (H.)

Figure 27. 6th, 12th and 18th harmonics of v_o vs. L_a for the controlled rectifier bridge. I_L = 1420 A.d.c.

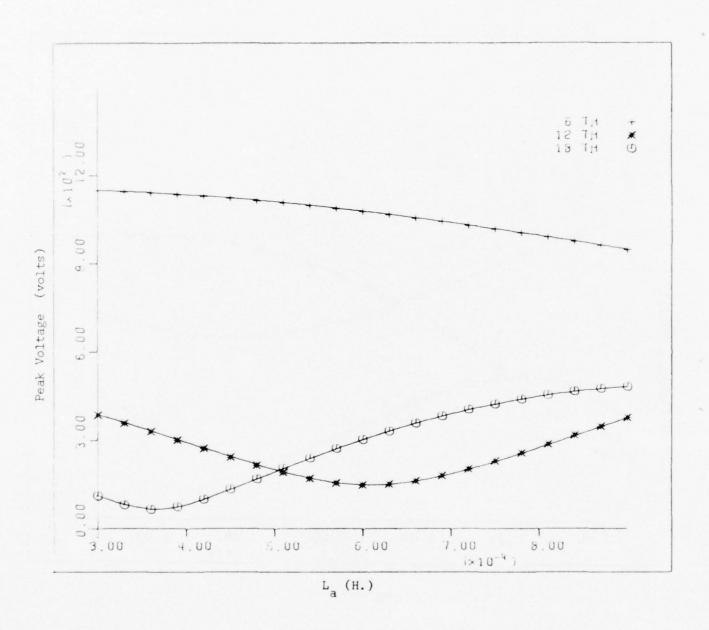


Figure 28. 6th, 12th and 18th harmonics of $\rm v_o$ vs. $\rm L_a$ for the controlled rectifier bridge. $\rm I_L$ = 568 A.d.c.

5. MINIMIZATION OF L.C. FILTER WEIGHT

5.1 Introduction

The previous sections have considered the following topics:

- 1. Steady state behavior with an uncontrolled rectifier bridge.
- 2. Steady state behavior with a controlled rectifier bridge.
- Transient currents that occur when a short circuit is placed across the output.
- 4. Reducing the full load output ripple voltage by increasing L_a .

The results of these studies can now be used in designing an L_{O}^{C} output filter for minimum weight. This analysis assumes the use of a controlled rectifier bridge for voltage regulation. The maximum allowable ripple voltage will be based on the size of the sixth harmonic that is present at full load. It should be noted that this harmonic will actually be greater at minimum load since the firing angle of the thyristors will be greater. This study assumes that the load will be fairly constant however, and that the presence of ripple voltage will be more important at full load than at lighter loads. Hence the filter optimization is based on full load conditions.

5.2 Calculation of L $_{\odot}$ and C $_{\odot}$ for Minimum Total Filter Weight

In the weight minimization algorithm, $L_{_{\rm O}}$ and $C_{_{\rm O}}$ are calculated to provide a given amount of ripple attenuation at full load. This calculation is based only on the sixth harmonic and ignores the harmonic attenuation provided by the load in conjunction with $L_{_{\rm O}}$. Therefore,

$$\left| \frac{1}{1 - L_{0} C_{0} \omega_{6}^{2}} \right| \leq k_{1} \tag{91.}$$

where k_1 = specified magnitude of the 6th harmonic attenuation

and $\omega_6 = 15079.64 \text{ radians/sec.}$

$$\therefore \qquad \qquad L_{\circ} C_{\circ} \geq \frac{k_{1}+1}{k_{1}\omega_{6}}$$
 (92.)

Due to the high value of the magnetic field and the low weight requirement, it is assumed that L_o will be an air core reactor.

Aluminum was chosen for the conductor due to its low weight/conductance ratio. The physical configuration of the inductor is shown in Figure 29. This particular design is chosen to produce the minimum loss for a given amount of material (see [25,26]). The inductance is,

$$L_0 = (24.5 \times 10^{-7}) \text{ N}^2 \text{ a}$$
 H. (93.)

and the weight of L is given by

$$L_{o}$$
 wt. = 3 π f D_{w} a 1bs. (94.)

where

N = number of turns

a = thickness of the coil (m.)

D, = density of Al (5837.8 lbs/m.3)

f = filling factor of the conductors (assumed to
 be 0.7)

The filling factor can be expressed,

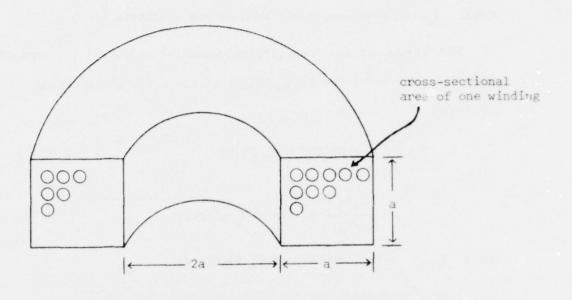


Figure 29. $L_{\rm o}$ dimensions.

$$f = \frac{NF_w}{a^2} \tag{95.}$$

where $F_{w} = cross sectional area of one winding(m.²)$

The common method of specifying capacitor weight is in terms of jouls/lb. Therefore the total weight of the L C filter can be expressed,

$$T_{\text{wt}} = C_{\text{o}} \text{ weight} + L_{\text{o}} \text{ weight}$$

$$= \frac{C_{\text{o}} V_{\text{L}}^{2}}{2D_{\text{c}}} + 3 \pi f D_{\text{w}} a^{3} \text{ lbs.}$$
(96.)

where D_{C} = energy density of C_{O} (joules/lb.).

Therefore substituting (92.), (93.) and (95.) into (96.)

$$T_{wt} = k_2/a^5 + k_3 a^3$$
 (97.)

where
$$k_2 = \left(\frac{1}{51.1 \times 10^{-7}}\right) \left(\frac{F_w V_L}{f}\right)^2 \left(\frac{k_1 + 1}{D_c k_1 \omega_6^2}\right)$$

$$k_3 = 3 \pi f D_w$$

To find the minimum value of T_{wt} , set

$$\frac{dT_{wt}}{da} = \frac{-5k_2}{a^6} + 3k_3 a^2 = 0 {(98.)}$$

$$a = \left(\frac{5k_2}{3k_3}\right)^{1/8} \tag{99.}$$

Once a is determined, N can be found from (95.) , $L_{_{\rm O}}$ from (93.) and $C_{_{\rm O}}$ from (92.) .

5.3 L C Design Algorithm

The flow chart for the L C filter design program is shown in Figure 30. The following discussion refers to the seven blocks indicated in the figure.

1. Read input data. This includes the following information: $^{\text{C}}_{\text{O}}$ energy density ($^{\text{D}}_{\text{C}}$), $^{\text{L}}_{\text{O}}$ current density, maximum 6th harmonic ripple voltage at full load, and maximum short circuit current, $^{\text{I}}_{\text{L(max.)}}$. This particular program assumes that the following quantities are constant:

 $V_{L} = 6760 \text{ V.dc}$

 $I_{T} = 1420 \text{ A.dc}$

 ω_6 = 15079.6 rad./sec. (line frequency = 400 Hz.)

 $\mathbf{V_L},~\mathbf{I_L}$ and $\boldsymbol{\omega_6}$ could be varied if desired, by making a few minor changes in the program.

- Set L_a = 0.3 mH, the normal design value specified in [13,14].
- 3. Assuming that a controlled rectifier bridge is used, the minimum weight $L_{_{\hbox{\scriptsize O}}}$ and $C_{_{\hbox{\scriptsize O}}}$ that will meet the 6th harmonic ripple specification are calculated.
- 4. A transient analysis subroutine to called to determine if the peak short circuit current will exceed the specified value of $I_{L(max.)}$. The details of this analysis are given in section 3.
- 5. If $I_{L(max.)}$ is exceeded, L_o is increased by 10%, and step 3 is repeated (C_o is simultaneously decreased to maintain a constant L_o product.) If $I_{L(max)}$ is not exceeded, the L_o and C_o design data is printed.
- 6. The program calculates L_o and C_o , first for the normal and then for the optimum values of L_a . If the calculation for the optimum L_a has

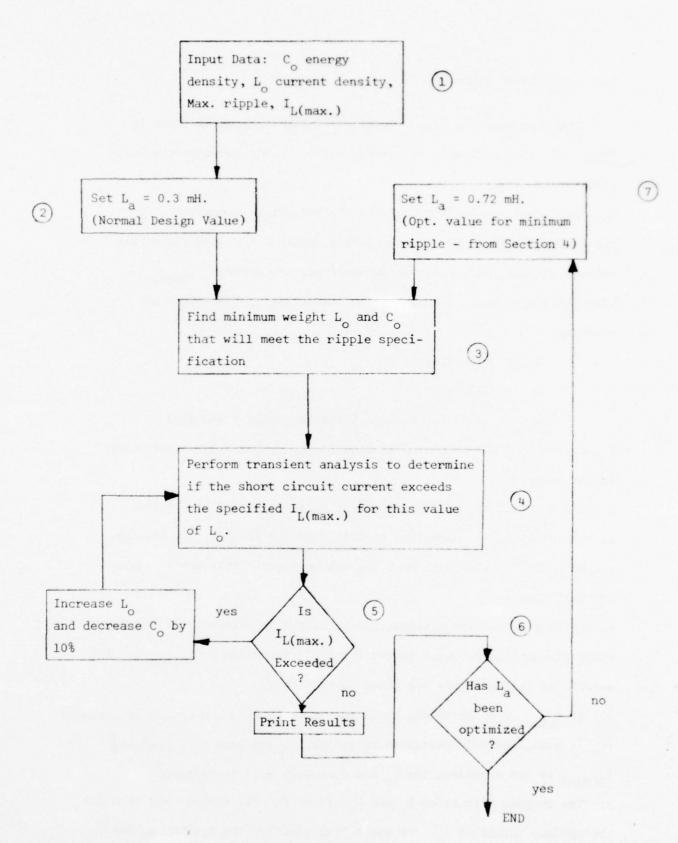


Figure 30. L_{\circ}° weight minimization flow chart.

been completed the program ends. If not, the program branches to step 7.
7. Set L_a = 0.72 mH., the optimum value for minimum ripple at full load calculated in Section 4. Steps 3 through 6 are then repeated.

5.4 Numerical Results

A sample of the computer results for the optimization program are shown in the following example. Note that use of the optimum $\mathbf{L}_{\mathbf{a}}$ decreases the total filter weight by approximately 22%.

The total filter weight will obviously decrease if a higher energy density (D_c) is used for C_o and/or a higher current density is used for L_o . Plots of filter weight vs. energy density and current density are shown in Figures 31 and 32 respectively. The filter weight will also be affected if the allowable $I_{L(max.)}$ is changed. A plot of this is shown in Figure 33.

WRITE THE FOLLOWING PARAMETERS FOR THE FILTER

ALL INPUTS HAVE FORMAT = F7.2 UNLESS ØTHERWISE SPECIFIED

CAP. EMERGY DEWSITY (JULLES/LB.) = 50.0

CURRENT DENSITY FOR L WIRE (CIR MIL/AMPI =

MAX. RMS VALUE OF 6TH HAR4. OF VO (VOLTS) = 20.0

ALLOWABLE PEAK FAULT CURRENT (AMPS) = 2500.0

THE FOLLOWING VALUES ARE BASED ON NORMAL LA = 0.300E-03 H.

IF= 0.275E+03 BETA= 0.212E+01 MU= 0.307E+00

ØPT.VALUES BEFØRE FAULT TEST ARE LO= 0.422E-02 H., CO= 0.636E-04 FD. R ES= 0.547E-01

MAX LØAD CURRENT FRØM FAULT = 0.250E+04

FAULT CURRENT TOO LARGE, LO INCREASED

MAX LØAD CURRENT FRØM FAULT = 0.250E+04

MAX LØAD CURRENT FRØM FAULT = 0.245E+04

LO= 0.511E-02. CO= 0.525E-04 ILF= 0.245E+04 RES= 0.615E-01

NJ. TURNS = 134 L RADIUS = 0.223E+00M L LENGTH = 0.111E+00M

THE FØLLØWING VALUES ARE BASED ØNØPTIMUM LA = 0.720E-03 ::-

IF= 0.239E+03 BETA= 0.223E+01 MU= 0.604E+00

VL= 0.676E+04 V1= 0.620E+03

@PT.VALUES BEFORE FAULT TEST ARE LO= 0.282E-02 H., CO= 0.499E-04 FD. R ES= 0.428E-01

MAX LUAD CURREIT FROM FAULT = 0.250E+04

FAULT CURRENT TOO LARGE, LO INCREASED

MAX LØAD CURRENT FROM FAULT = 0.250E+04

MAX LØAD CURRENT FRØM FAULT = 0.250E+04

NO. TURNS = 114 L RADIUS = 0.206E+00N L LENGTH = 0.103E+00M

WRITE "O" TO END, OR "I" FOR ANOTHER RUN

FURMAT= 12

IL= 0.142E+04

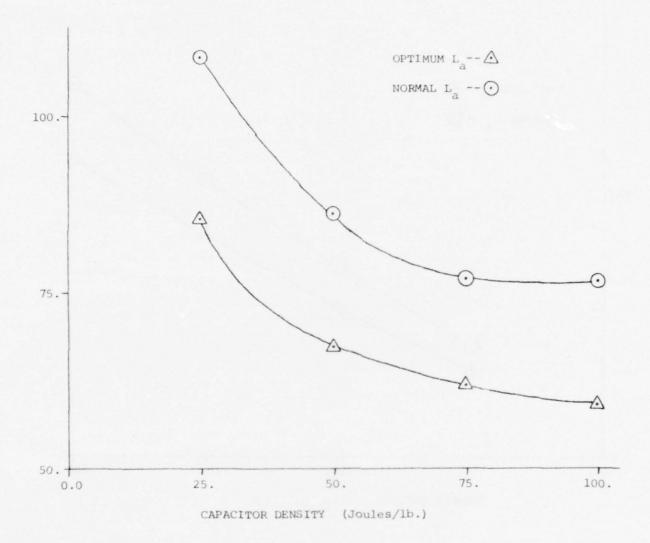


Figure 31. Filter weight vs. C energy density. Current density = 100 cir. mile/amp, all other variables are the same as in the example run.

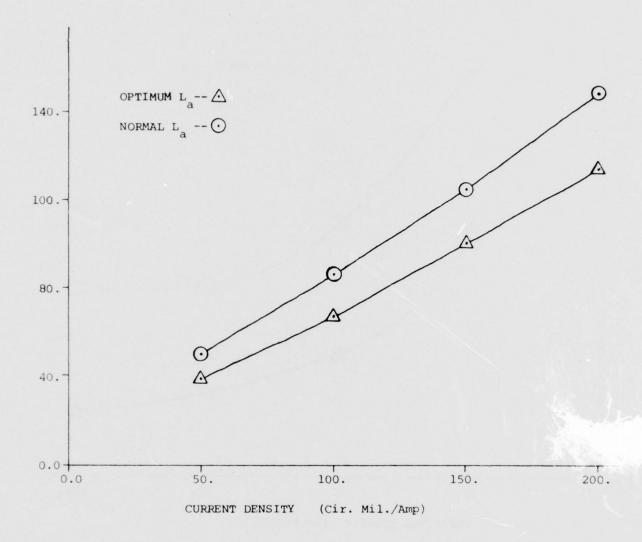


Figure 32. Filter weight vs. $L_{\rm o}$ current density. All other variables are the same as in the example run.

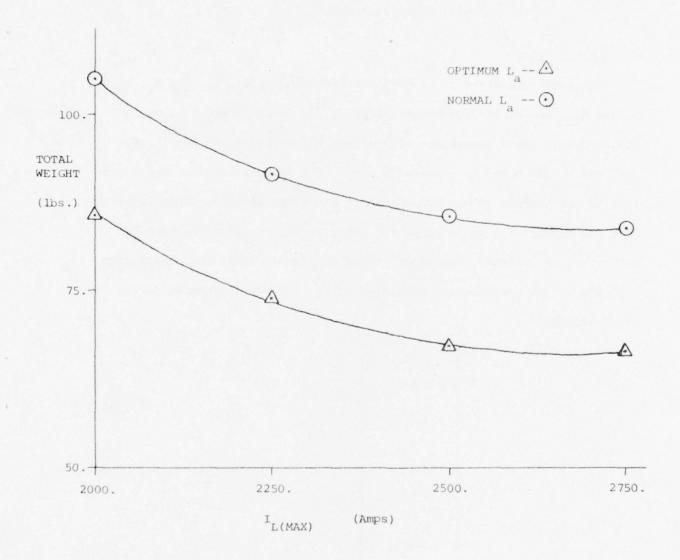


Figure 33. Filter weight vs. maximum allowable short circuit current. Current density = 100 cir. mils/amp, all other variables are the same as in the example run.

6. SENSITIVITY ANALYSIS

6.1 Introduction

Since the values of the alternator inductances, L_a , L_f , L_d , M_a , M_f , M_d and M_{fd} , are subject to numerical error, it is of interest to see how errors in these parameters will affect the calculations for I_f , β , μ , V and W. As noted in Sections 1 and 2, the calculations for the uncontrolled and controlled rectifier bridges are quite similar. This implies that the effect of a given parameter error should be about the same for both types of systems. Therefore it was decided to limit the sensitivity analysis to the uncontrolled rectifier case. For convenience we define the following,

$$\underline{f(x,y)} = R.H.S. \text{ of}$$

$$(44.)$$

$$(45.)$$

$$(46.)$$

$$(47.)$$

$$(48.)$$

Theoretically, this analysis could be performed by either of two methods:

- 1. Use (102.) to find $\frac{\partial \underline{x}}{\partial \underline{y}}$ and solve for $\Delta \underline{x}$ for a given $\Delta \underline{y}$, i.e., $\Delta \underline{x} = \frac{\partial \underline{x}}{\partial \underline{y}} \Delta \underline{y}$. This will be referred to as the <u>differential</u> method.
- 2. Simply replace \underline{y} by \underline{y} + $\Delta \underline{y}$ and use the Newton Raphson method to find the resulting \underline{x} + $\Delta \underline{x}$. This will be referred to as the <u>deliberate</u> error method.

The differential method is certainly the more elegant of the two, so this was investigated first. Unfortunately this approach depends on solving sets of simultaneous equations that have ill-conditioned coefficient matrices. Two algorithms were used for solving these equations, but both failed due to excessive round-off errors. Therefore it was necessary to resort to the deliberate error method. This second approach worked satisfactorily even though it is rather inefficient in terms of computation time. Both methods will be discussed for completeness, even though the first did not produce satisfactory results.

6.2 Differential Method

One usually does not bother to describe methods that do not work, but this analysis is interesting from a conceptual standpoint, so it is included for that reason. It is also possible that the problems with this method may eventually be solved, even though it was unsuccessful in this present research.

Taking the partial derivative of (102.) produces an equation of the form,

$$\frac{\partial \underline{f}(\underline{x},\underline{y})}{\partial y_{i}} = [C] \frac{\partial \underline{x}}{\partial y_{i}} + \underline{r} = \underline{0}$$
 (103.)

where [C] is a (5x5) coefficient matrix, and \underline{r} is a (5x1) vector.

$$\frac{\partial \mathbf{x}}{\partial \mathbf{y_i}} = - [c]^{-1} \underline{\mathbf{r}}$$
 (104.)

which is the ith column of $\frac{\partial \underline{x}}{\partial \underline{y}}$, a (5x7) matrix. Therefore it is conceptually possible to use (104.) for all seven elements of \underline{y} to find $\frac{\partial \underline{x}}{\partial \underline{y}}$. $\Delta \underline{x}$ for a given $\Delta \underline{y}$ is then,

$$\Delta \underline{\mathbf{x}} = \frac{\partial \underline{\mathbf{x}}}{\partial \underline{\mathbf{y}}} \Delta \underline{\mathbf{y}} \tag{105.}$$

Unfortunately, the [C] matrices indicated by (103.) are very ill conditioned in this application, and this prevented finding a solution for $\frac{\partial \mathbf{x}}{\partial \mathbf{y}}$. Two methods of solution were attempted, the first being the DGELG double precision subroutine from the IBM Scientific Subroutine Package and the second being a Shipley-Coleman inversion algorithm to find $[C]^{-1}$. Both of these programsuse pivoting for size, but they were still incapable of finding the correct solution. Therefore this approach was abandoned in favor of the deliberate error method.

6.3 Deliberate Error Method

In this method a given error, $^\Delta\!y_i$, is added to y_i and the resulting $\underline{x} + \Delta\underline{x}$ is calculated by the equations described in section 1. The terms of \underline{y} are not independent however, since mutual inductance terms are present, and this must be accounted for in the analysis. Therefore, the approach used in this particular study was to assume that the following terms can be varied independently of one another: L_a , L_f , L_d , k_{aa} , k_{af} , k_{ad} , and k_{fd} , where the last four terms are the coefficients of coupling, i.e.,

$$k_{aa} = \frac{M_a}{L_a}, \quad k_{af} = \frac{M_f}{\sqrt{L_a L_f}}, \quad k_{ad} = \frac{M_d}{\sqrt{L_a L_d}}, \quad k_{fd} = \frac{M_{fd}}{\sqrt{L_f L_d}}$$
 (106.)

The independent and dependent parameters are listed as follows:

Independent	Dependent
L _a	Ma, Mf, M
$^{\mathrm{L}}\mathrm{_{f}}$	M _f , M _{fd}
$^{\mathrm{L}}\mathrm{_{d}}$	M _d , M _{fd}
k _{aa}	$_{\rm a}^{\rm M}$
k _{af}	M _f
k _{ad}	M _d
k _{fd}	M _{fd}

For example, a 10% increase in L_a implies (new value = 1.1 L_a),

$$M_a = 1.1 k_{aa} L_a$$
, $M_f = k_{af} \sqrt{1.1 L_a L_f}$, $M_d = k_{ad} \sqrt{1.1 L_a L_d}$,

whereas a 10% increase in k_{af} implies (new value = 1.1 k_{af}),

$$M_{af} = 1.1 k_{af} \sqrt{L_a L_f}$$

The effect of these errors will be described in the next section on numerical results.

6.4 Numerical Results

The following paragraphs discuss the effects of varying each of the machine inductances, i.e., the effect of a deliberate error. Note that since the algorithm used in Section 1 depends upon the approximation given by (41.), it is necessary to restrict the parameter variations to the range where (41.) is valid. It is assumed that (41.) is satisfied as long as the following condition is met:

 ΔL_a : Results are shown in Figures 34 and 35. These figures indicate that all of the \underline{x} variables are quite sensitive with respect to ΔL_a .

 ΔL_f : Results are shown in Figures 36 and 37. It is noted that β , μ , V and W do not vary with respect to L_f . The reason for this is that the algorithm automatically adjusts I_f to compensate for any L_f changes, so that the M_fI_f flux linkages remain constant (note that M_f is dependent on L_f .) Compare with the M_f results shown in Figures 42 and 43.

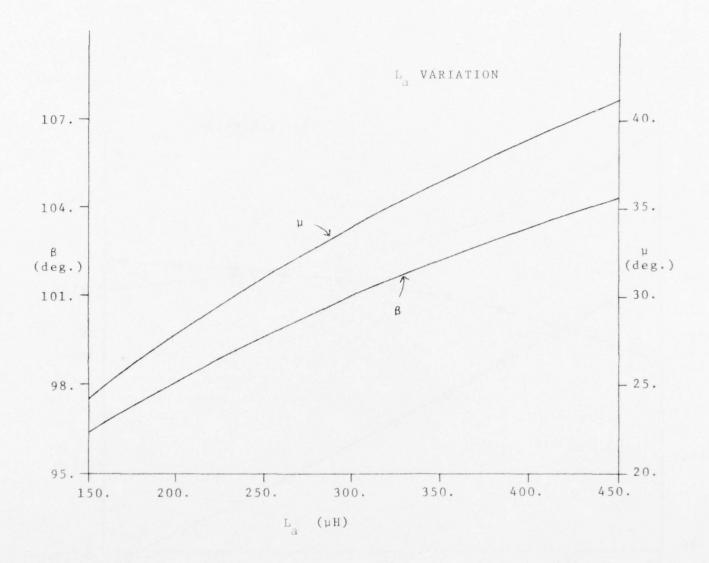


Figure 34. β and μ variation vs. $L_{\underline{a}}.$

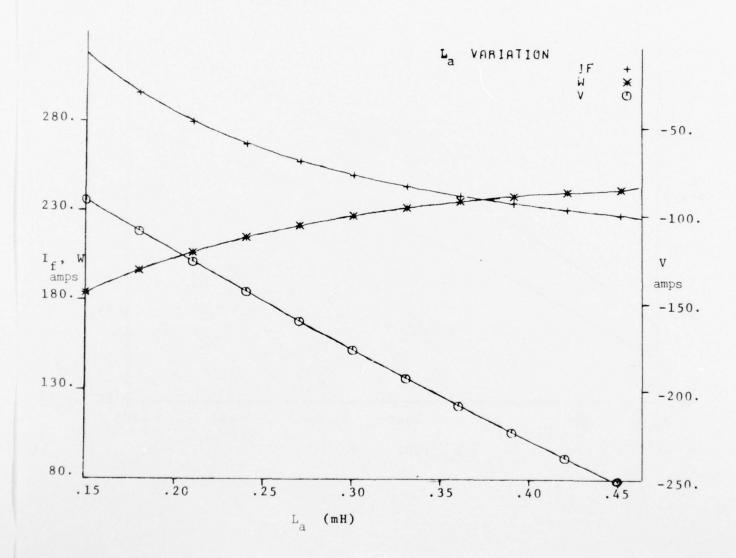


Figure 35. I_f , W and V variation vs. L_a .

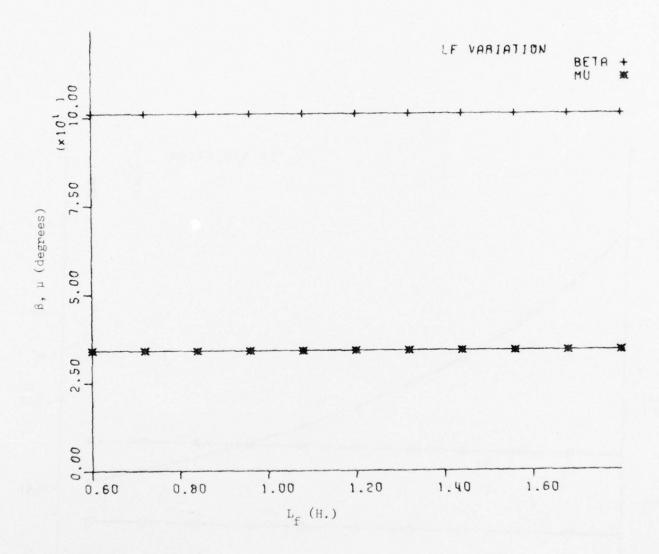


Figure 36. β and μ variation vs. $L_{\mbox{\scriptsize f}}.$

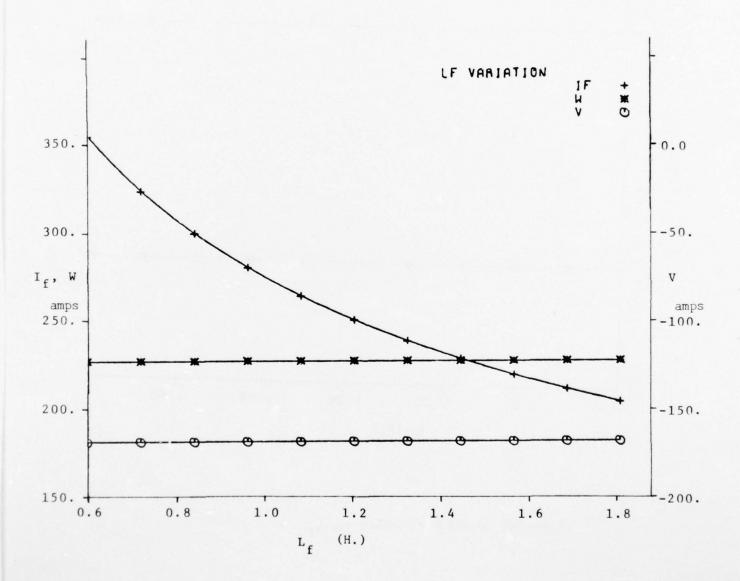


Figure 37. I_f , W and V variation vs. L_f .

 $\Delta L_{\underline{d}}$: Results are shown in Figures 38 and 39. These figures indicate that the calculations are completely insensitive to $L_{\underline{d}}$ variations. The reason for this stems from the previously mentioned approximation,

which is given by (41.) in Section 1. Once this approximation is made, ${\rm M}_{\odot}$ is replaced by ${\rm M}_{\odot}$ in all subsequent calculations. The value of ${\rm M}_{\odot}$ is,

$$M_{oo} = \frac{M_d^2}{Ld} = k_{ad}^2 L_a$$
 (108.)

The result of this is that $L_{\rm d}$ does not actually appear in (44.)-(51.), which are the equations used to find x.

 Δk_{aa} (ΔM_a): Results are shown in Figures 40 and 41. The figures indicate that μ is quite sensitive to ΔM_a variations, while I_f and β are less sensitive. W and V also vary considerably with respect to M_a .

 Δk_{af} (ΔM_f): Results are shown in Figures 42 and 43. For an explanation of these results, refer to the discussion for ΔL_f .

 Δk_{ad} (ΔM_d): Results are shown in Figures 44 and 45.

 $\Delta k_{
m fd}$ ($\Delta M_{
m fd}$): Results are shown in Figures 46 and 47. These figures indicate that the calculations are insensitive to $M_{
m fd}$ variations. The reason for this is much the same as for $L_{
m d}$, i.e., once the approximation (107.) is made, $M_{
m fd}$ does not appear in any of the subsequent equations.

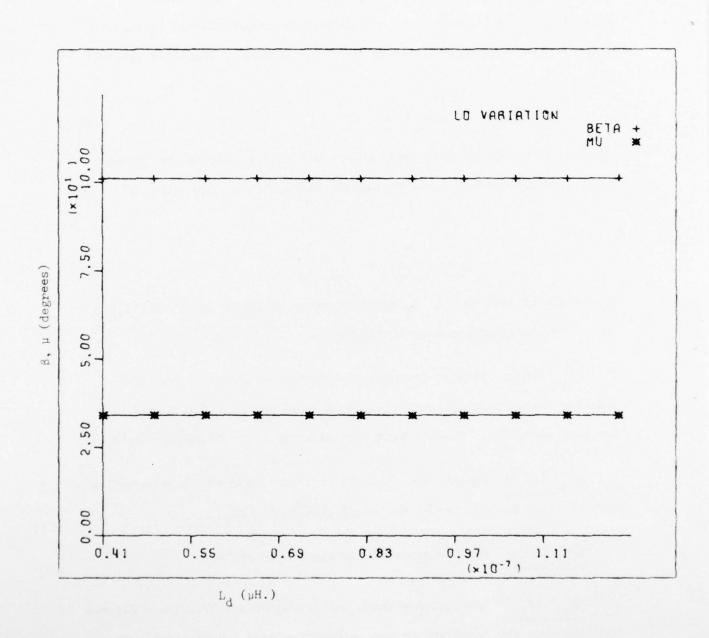


Figure 38. β and μ variation vs. $\boldsymbol{L}_{\mbox{\scriptsize d}}.$

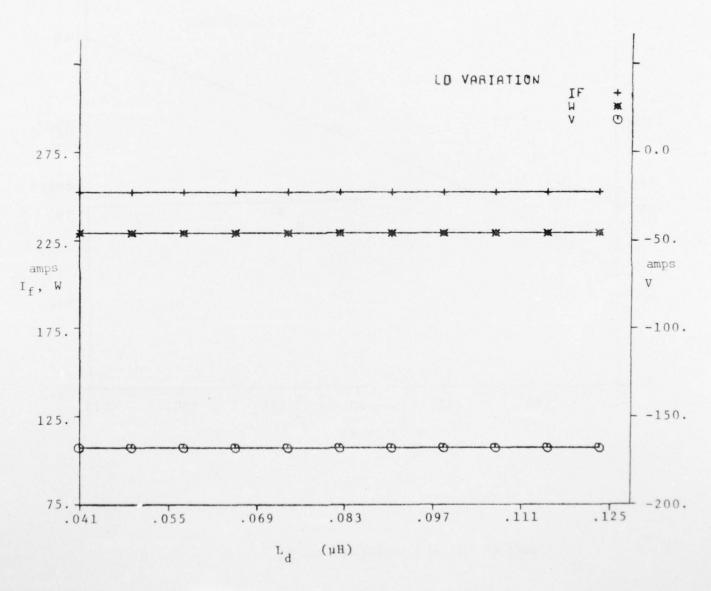


Figure 39. I_f , W and V variation vs. L_d .

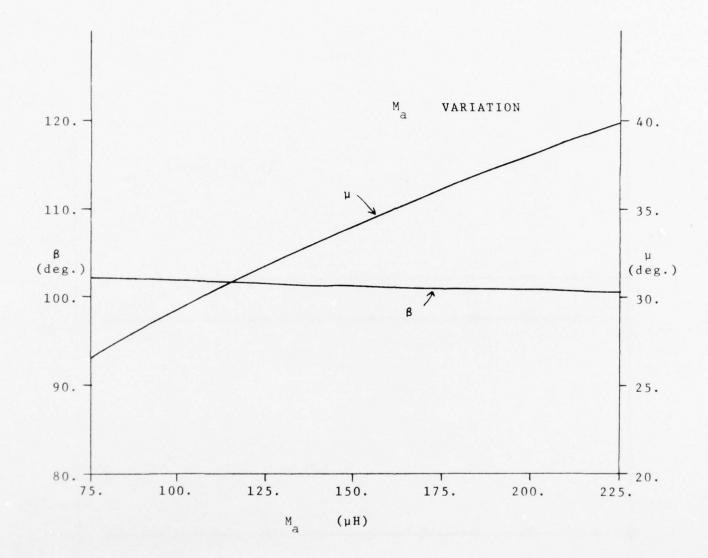


Figure 40. β and μ variations vs. ${\rm M}_{\rm a}.$

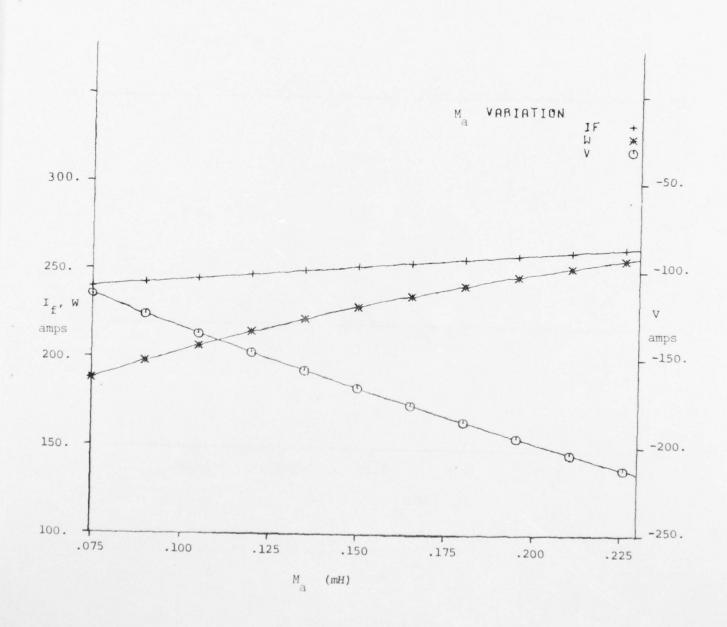


Figure 41. I_f , W and V variation vs. M_a .

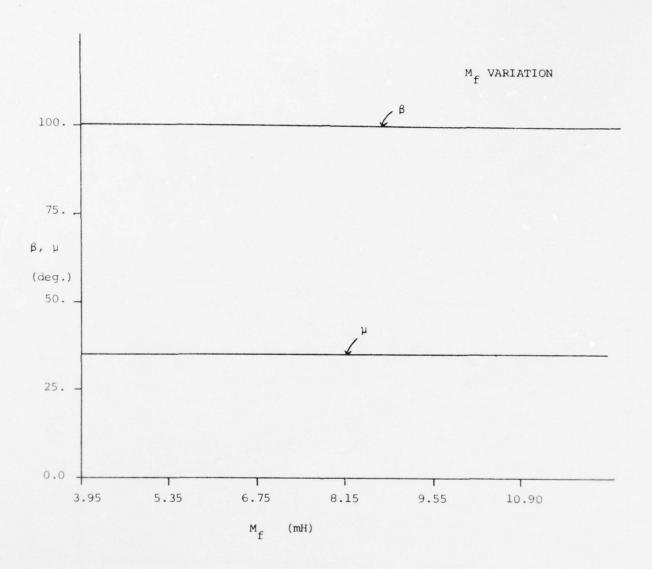
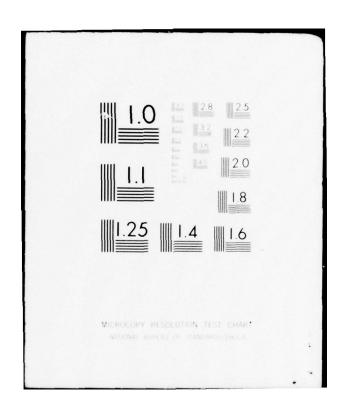


Figure 42. β and μ variation vs. M_{f} .



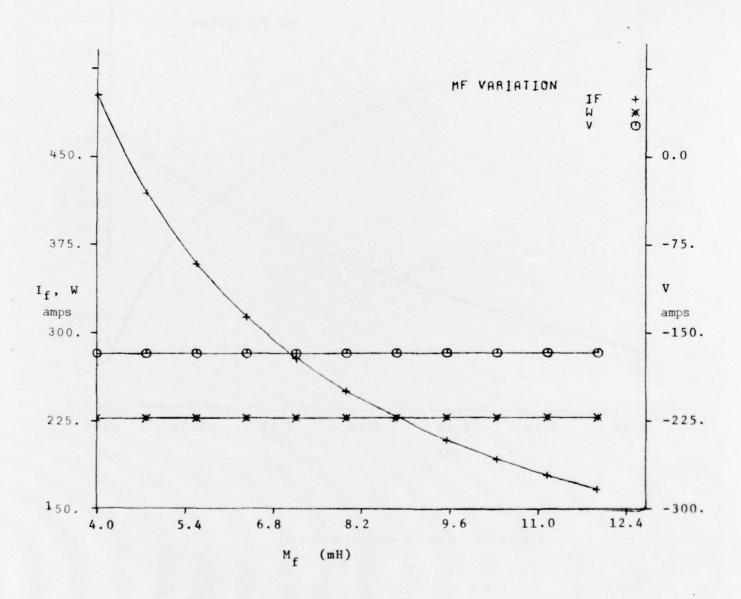


Figure 43. β and μ variation vs. M_f .

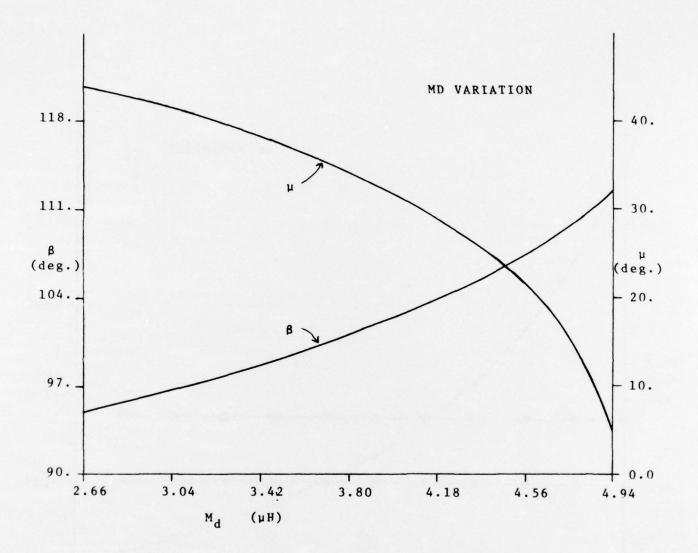


Figure 44. β and μ variation vs. $\mbox{M}_{\mbox{\scriptsize d}}.$

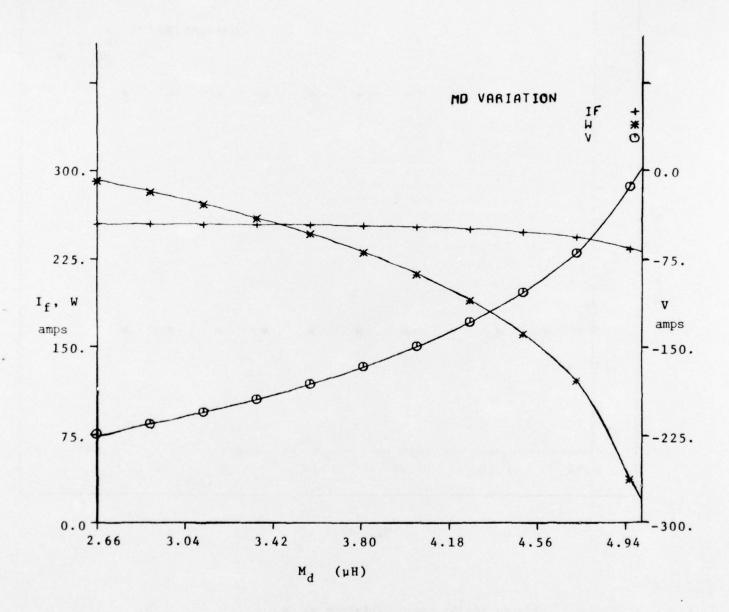
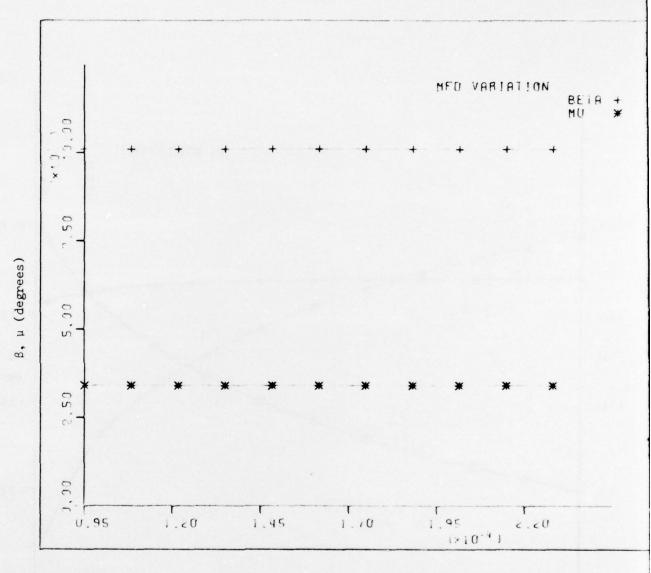


Figure 45. I_f , W and V variation vs. M_d .



M_{fd} (mH.)

Figure 46. β and μ variation vs. $M_{\mbox{fd}}$.

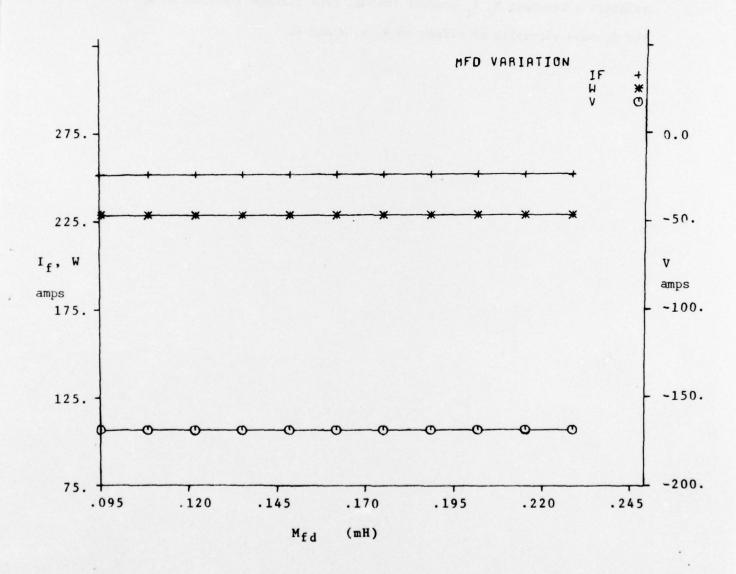


Figure 47. I_f , W and V variation vs. M_{fd} .

To summarize, it can be seen that I_f , β , μ , V and W as a group are most sensitive to errors in L_a , M_a and M_d . I_f is also quite sensitive to errors in L_f and M_f , but since the algorithm adjusts to maintain a constant M_f I_f product (mutual flux linkages) errors in L_f and M_f have virtually no effect on β , μ , V and W.

7. VOLTAGE REGULATOR AND CURRENT OVERLOAD PROTECTION CIRCUITS

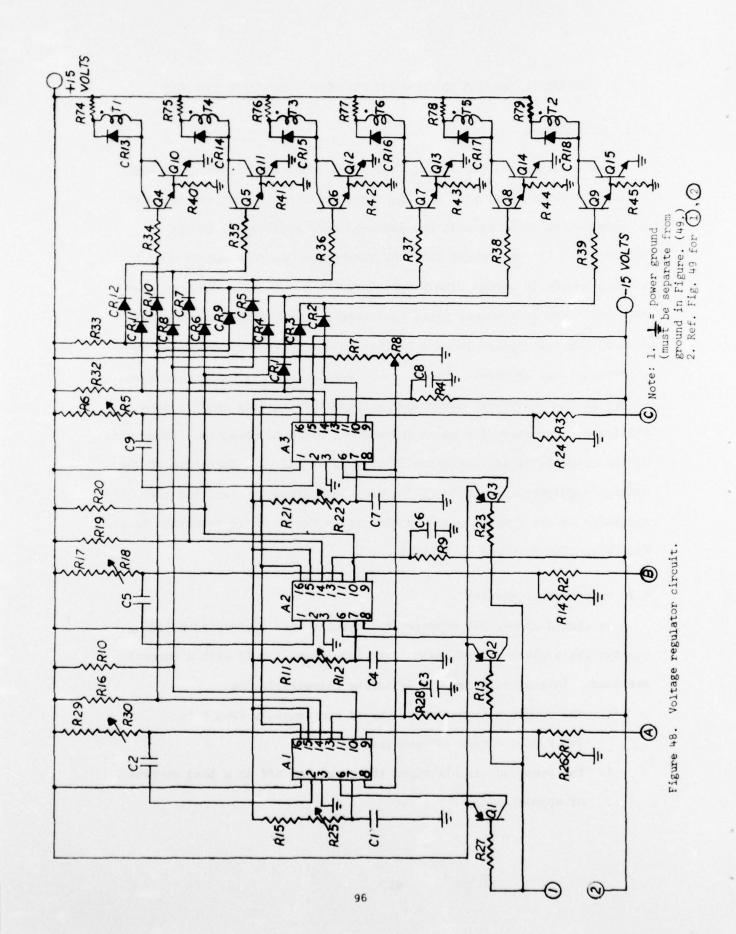
7.1 Introduction

The experimental portion of this study consisted of designing and building a phase controlled voltage regulator for eventual testing with an alternator. This circuit was designed and tested early in the project when it was thought that the alternator could be modelled by a voltage source in series with single inductance. Testing the regulator with this type of a source would have been a fairly simple matter, but such a test now appears to have limited value since a more detailed machine model was employed. Therefore it was decided to concentrate more effort on the analytical study and postpone this testing until a conventional alternator with known inductances could be obtained. Schematics of the complete design are shown in Figures 48 and 49. Operation of the voltage regulator circuit in Figure 48 is described in [23], and the operation of the current overload circuit in Figure 49 is described in [22]. The parts list is shown in Table I.

7.2 Experimental Results

As stated above, the experimental results were limited to building and testing a phase controlled voltage regulator circuit with a current overload. This circuit has the following characteristics:

- The output voltage can be varied continuously from 0 to 290 V.d.c. with a 100 ohm load.
- The overload circuit turns the regulator off at a load current of approximately 3.5 A.d.c.



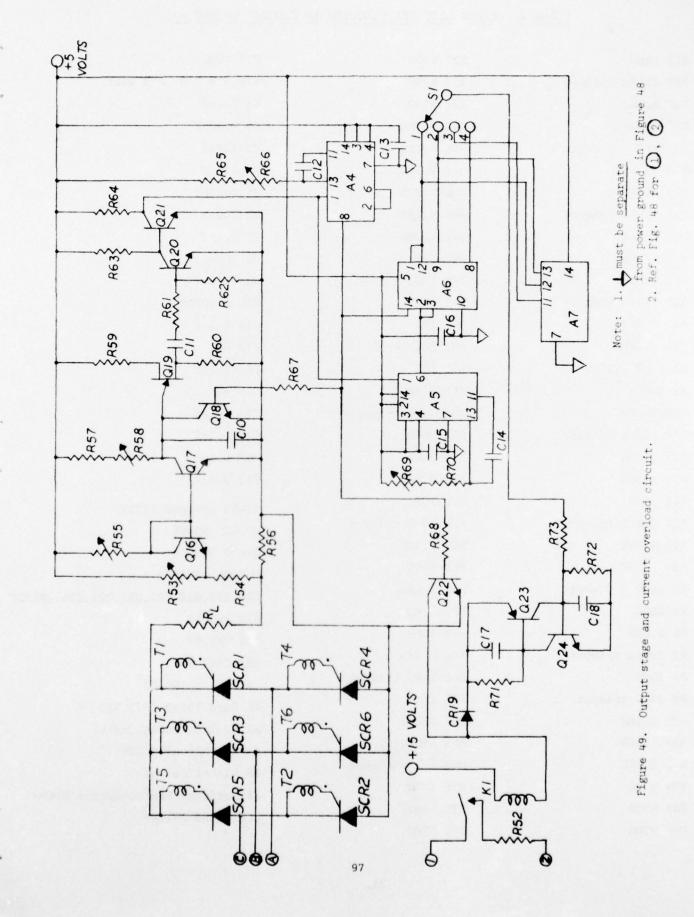


TABLE I. PARTS LIST FOR CIRCUITS IN FIGURES 48 AND 49

R15 10KΩ	R37 470Ω	R73 20KΩ
R25 250KΩ trimpot	R38 470Ω	R74-R79 30Ω - 1 watt
R27 4.7KΩ	R39 470Ω	C1 0.1µf
R26 3.76KΩ	R40 4.7KΩ	C2 0.05µf
R1 11K Ω - 2 watt	R41 4.7KΩ	C3 100µf
R28 330Ω	R42 4.7KΩ	C4 0.1µf
R29 5.6KΩ	R43 4.7KΩ	C5 0.05µf
R30 250KΩ trimpot	R44 4.7KΩ	C6 100µf
R16 1.5KΩ	R45 4.7KΩ	C7 0.1µf
R10 1.5KΩ	R46 10Ω	C8 100µf
R11 10KΩ	R47 10Ω	C9 0.05µf
R12 250KΩ trimpot	R48 10Ω	Cl0 0.001µf
R13 4.7KΩ	R49 10Ω	Cl1 0.1µf
R14 3.76KΩ	R50 10Ω	C12 2µf
R2 $11K\Omega$ - 2 watt	R51 10Ω	C13 0.1µf
R9 330Ω	R52 3.3KΩ	C14 4µf
R17 5.6KΩ	R53 20KΩ trimpot	C15 0.1µf
R18 250KΩ trimpot	R54 200Ω	C16 0.1µf
R19 1.5KΩ	R55 20KΩ	C17 0.1µf
R20 1.5KΩ	R56 0.04Ω	C18 0.1µf
R21 10KΩ	R57 10KΩ	T1-T6 Sprague 11Z12
R22 250KΩ trimpot	R58 20KΩ trimpot	Q1-Q3 2N3906
R23 4.7KΩ	R59 2.0KΩ	Q4-Q9 2N3904
R24 3.76ΚΩ	R60 630Ω	Q10-Q15 2N2222
R3 $11K\Omega$ - 2 watt	R61 1.1KΩ	Q16,Q17,Q18,Q20,Q21,Q22,Q24 2N2222
R4 330Ω	R62 10ΚΩ	Q19 2N2646
R6 5.6KΩ	R63 10ΚΩ	Q23 2N2907
R5 250KΩ trimpot	R64 2.2KΩ	CR1-CR12 1N914
R7 10KΩ	R65 10KΩ trimpot	CR13-CR18 1N4001
R8 10KΩ trimpot	R66 15KΩ	K1 Reed Relay SPST N/O
R31 1.5KΩ	R67 330KΩ	A1-A3 Telefunken UAA145
R32 1.5KΩ	R68 330KΩ	A4-A5 Fairchild 9601
R33 1.5ΚΩ	R69 10KΩ trimpot	A6 Signetics 7493
R34 470Ω	R70 15KΩ	A7 National Semiconductor N7408
R35 470Ω	R71 10KΩ	SCR1-SCRG 2N1849
R36 470Ω	R72 47KΩ	JOHN PORKO ZNIO45

 No misfiring problems were observed once the final design was complete.

Certain waveforms of interest are shown in Figures 50 through 53.



Figure 50. AC output voltage across the load for a delay angle of 15°. (Scale = 15°/div.)

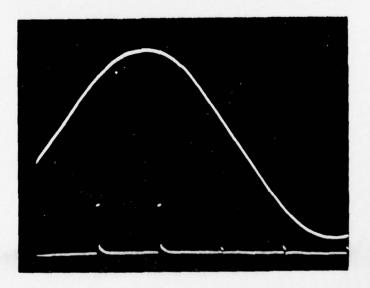


Figure 51. (Top) Line to neutral input voltage (Bottom) Thyristor firing pulses for a delay angle of 15°. (Note: 0° delay angle corresponds to 30° on the line to neutral voltage waveform. (Scale = 30°/div.)



Figure 52. (Top) Ramp voltage at pin 7 of the UAA145. (Bottom) Thyristor firing pulses for a delay angle of 15°. (Scale = 30°/div.)

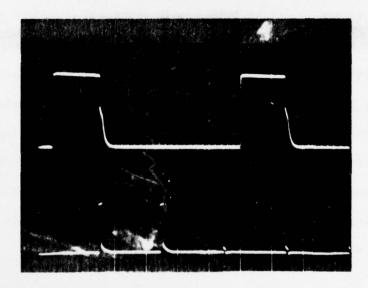


Figure 53. (Top) Pulse formation control signal at pin 11 of UAA145.

(Bottom) Thyristor firing pulses for a delay angle of 15°. (Scale = 30°/div.)

8. CONCLUSIONS

This study indicates that it is possible to utilize L_a to help perform some of the functions normally assigned to the L_{OO}^{C} output filter. This implies that a smaller filter can be used, thus decreasing the weight of the L_O and C_O components. For the 10 MVA/5kV example alternator with a controlled rectifier bridge it was shown that an increase in L_a from 0.3 mH. to 0.72 mH decreases the filter weight by about 17 lbs., a 22% reduction. This example also indicated 0.72 mH. to be an optimum value, i.e., filter weight increased for $L_a > 0.72$ mH. Naturally, this savings may be offset by an increase in alternator weight due to the larger L_a . Therefore any final weight optimization study should consider the alternator and filter as a combined system.

In the course of developing the filter weight minimization program it was necessary to derive both steady state and transient models for the alternator and rectifier bridge. Because of the large amounts of information provided by these models, it appears they may be useful for simulating the system during the design stage. Once experimental data becomes available for comparison, these models may be refined as necessary in order to accurately predict the various winding currents, commutation angles, etc. It is stressed that this experimental verification is necessary, and plans have been made to proceed with this for a system with a conventional alternator.

9. RECOMMENDATIONS

This study indicates that if L_a is increased up to a certain optimum point, it is possible to significantly reduce the size of the output filter. Information of this type should be brought to the attention of machine designers, but it may or may not influence the design of future alternators due to the many other factors which govern the size of L_a . Ultimately the alternator and filter should be considered together in future weight minimization studies.

Perhaps the most pressing need at this point is to obtain some experimental data to compare with the predicted results. Eventually this must be done using a superconducting alternator; however, it is unlikely that such a machine will be available for this purpose for quite some time. In the interim, it is proposed that tests should be conducted on a conventional alternator-rectifier system in order to evaluate the models.

10. REFERENCES

- H. H. Woodson, Z. J. J. Stekly, and E. Halas, "A Study of Alternators with Superconducting Field Windings: I Analysis," IEEE
 Trans. on Power Apparatus and Systems, vol. PAS-95, No. 3, pp.
 264-274, March 1966.
- Z. J. J. Stekly, H. H. Woodson, A. M. Hatch, L. O. Hoppie, and E. Halas, "A Study of Alternators with Superconducting Field Windings: II - Experiment," IEEE Trans. on Power Apparatus and Systems, vol. PAS-95, No. 3, pp. 274-280, March 1966.
- P. Thullen, J. C. Dudley, D. L. Greene, J. L. Smith, Jr., and H. H. Woodson, "An Experimental Alternator with a Superconducting Rotating Field Winding," IEEE Trans. on Power Apparatus and Systems, vol. PAS-90, No. 2, pp. 611-619, March-April 1971.
- 4. H. H. Woodson, J. L. Smith, Jr., P. Thullen, and J. L. Kirtley, "The Application of Superconductors in the Field Windings of Large Synchronous Machines," IEEE Trans. on Power Apparatus and Systems, vol. PAS-90, No. 2, pp. 620-627, March-April 1971.
- J. L. Kirtley, Jr., "Basic Formulas for Air-Core Synchronous Machines," IEEE PES Winter Power Meeting, Paper No. 71 CP 155-PWR, New York, New York, January 1971.
- J. L. Kirtley, Jr., "Per Unit Reactances of Superconducting Synchronous Machinery," IEEE Trans. on Power Apparatus and Systems, vol. PAS-92, No. 4, pp. 1316-1320, July-August 1973.
- 7. T. H. Einstein, "Generalized Representation of Generator Excitation Power Requirements," IEEE Trans. Power Apparatus and Systems, vol. PAS-91, No. 5, pp. 1840-1847, September-October 1972.

- 8. T. H. Einstein, "System Performance Characteristics of Superconducting Alternators for Electric Utility Power Generation," IEEE Trans. Power Apparatus and Systems, vol. PAS-94, No. 2, pp. 310-319, March-April 1975.
- M. Furuyama and J. L. Kirtley, Jr., "Transient Stability of Superconducting Alternators," IEEE Trans. on Power Apparatus and Systems, vol. PAS-94, No. 2, pp. 320-328, March-April 1975.
- 10. J. L. Smith, "Superconductors in Large Synchronous Machines," Final Report for EPRI-EEI research project RP-92, Electric Power Research Institute, Palo Alto, California, June 1975.
- 11. J. L. Kirtley, Jr., and M. Furuyama, "A Design Concept for Large Superconducting Alternators," IEEE Trans. Power Apparatus and Systems, vol. PAS-94, No. 4, pp. 1264-1269, July-August 1975.
- 12. J. L. Smith, Jr., P. Thullen, "Steady-State Electrical Tests on the MIT-EPRI 3 MVA Superconducting Generator," IEEE Trans. on Power Apparatus and Systems, vol. PAS-95, No. 3, pp. 887-893, May-June 1975.
- 13. J. L. McCabria, R. D. Blaugher, and J. H. Parker, Jr., "Superconducting Generator Development," NAECON '75 Record, pp. 261-271, Dayton, Ohio, June 1975.
- 14. A. E. King, C. C. Kouba, J. L. McCabria, and L. D. Smith, "High

 Power Study Superconducting Generators," Final Report AFAPL-TR-76-37,

 USAF Aero Propulsion Laboratory, Wright-Patterson AFB, Ohio, March 1976.
- 15. W. J. Shilling, "Exciter Armature Reaction and Excitation Requirements in a Brushless Rotating Rectifier Aircraft Alternator," AIEE Trans.

 Applications and Industry, vol. 79, Pt. 2, pp. 394-402, 1960.

- 16. J. Stepina, "Calculation of the R.M.S. Value of the Ampere-Turns Per Unit of Rotor Periphery in the Synchronous Machine Under Rectifier Load," ACTA TECHNICA GSAV, No. 3, pp. 255-280, 1964.
- 17. P. W. Franklin, "Theory of the Three Phase Salient Pole Type Generator with Bridge Rectified Output Part I," IEEE Trans.

 Power Apparatus and Systems, vol. PAS-72, No. 5, pp. 1960-1967, September-October 1972.
- 18. P. W. Franklin, "Theory of the Three Phase Salient Pole Type Generator with Bridge Rectified Output - Part II," IEEE Trans. Power Apparatus and Systems, vol. PAS-72, No. 5, pp. 1968-1975, September-October 1972.
- 19. W. J. Bonwick and V. H. Jones, "Performance of a Synchronous Generator with a Bridge Rectifier," Proceedings of IEE, Vol. 119, No. 9, pp. 1338-1342, September 1972.
- 20. W. J. Bonwick and V. H. Jones, "Rectifier-Loaded Synchronous Generators with Damper Windings," Proceedings of IEE, Vol. 120, No. 6, pp. 659-666, June 1973.
- 21. P. K. Dash, G. S. Hope and O. P. Malik, "Digital Simulation of a Synchronous Generator Operating with Thyristor Bridge," presented at the 1977 IEEE PES Winter Meeting (Paper No. A77-194-4), New York, New York, February 1977.
- 22. T. A. Stuart, "Overload Protection and Filtering Requirements for Phase Controlled Voltage Regulators," ASEE-USAF Summer Faculty Research Program Report (sponsored by Auburn University), Wright-Patterson AFB, Ohio, August 15, 1975.

- 23. "Phase Control Integrated Circuit," (Application Note), AEG-Telefunken Corporation, Heilbronn, West Germany.
- 24. F. W. Gutzwiller, G. H. Bacon, E. E. Von Zastrow, and R. R. Rottier, "Rectifier Components Guide," General Electric Company, Auburn, New York, 1962.
- 25. C. C. Damstra and T. Stoop, "A Three Phase Resonant Inverter Circuit for HVDC Valve," Proceedings of the 1977 IEEE/IAS International Semiconductor Power Converter Conference, pp. 164-171, Lake Buena Vista, Florida, March 1977.
- 26. J. Hak, Eisenlose Drosselspule, Leipzig-Kohler-Verlag, 1938.
- 27. G. W. Stagg and A. H. El-Abiad, "Computer Methods in Power System Analysis," McGraw-Hill, New York, New York, 1968.

11. RESEARCH PUBLICATIONS

- T. A. Stuart and M. W. Tripp, "Predicted Characteristics of the Superconducting Alternator with Rectified Load," NAECON '77 Conference Proceedings, Dayton, Ohio, May 1977.
- T. A. Stuart and M. W. Tripp, "Calculation of Rotor Currents for the Rectified Superconducting Alternator," to be published as a short paper by the <u>Proceedings of the IEEE</u> (accepted February 1977).
- 3. T. A. Stuart and M. W. Tripp, "A Steady State Analysis of the Superconducting Alternator with Rectified Output," accepted for the July 1977 issue of <u>IEEE Trans. on Aerospace and Electronic</u> Systems.
- 4. M. W. Tripp, "An Improved Model for Predicting the Output Characteristics of the Superconducting Alternator with Rectified Load," Masters Thesis, Department of Electrical Engineering, The University of Toledo, Toledo, Ohio, May 1977.

APPENDIX I: GLOSSARY OF TERMS

A, B, C = constants defined by (49.), (50.) and (51.)

a = thickness of L

C = output filter capacitor

D_c = energy density of C_o

D = density of aluminum

f = fill-in factor for L

f, = break frequency of output filter

 F_{w} = cross sectional area of one winding of L_{o}

 i_a , i_b , i_c = line currents

 $i_d^{},\ i_q^{}$ = currents in the equivalent direct and quadrature windings used to represent the damper shield

I_f = average field current

i = time varying component of field current

ik = commutation current

i_LF = load current with short circuit across load

ikF = commutation current with short circuit across load

 i_{fo} , i_{do} , i_{qo} = field and damper currents at θ = $\beta + \mu - \pi/3$

 K_q , K_f , K_d = constants defined by (15.) and (18.)

k = coefficient of coupling between armature phase windings

k_{ad} = coefficient of coupling between armature and equivalent damper windings

k_{af} = coefficient of coupling be ween field and armature

k_{fd} = coefficient of coupling between field and equivalent direct axis damper windings

k₁ = specified harmonic attenuation factor of output filter

 k_2 , k_3 = constants defined just below (97.) I, = load current L = self inductance of each armature winding L_d = self inductance of the direct and quadrature axis windings L_f = self inductance of the field winding L = output filter inductor M = magnitude of mutual inductance between armature windings M_d = magnitude of mutual inductance between damper and armature windings M_f = magnitude mutual inductance between field and armature windings M_{fd} = mutual inductance between field and direct axis damper windings M_{\odot} , M_{\odot} = constants defined by (33.) and (34.) N = number of turns for L R = resistance of one armature winding R = resistance of inductor, L v_f, v_d, v_g = voltages across rotor windings v_{ab} , v_{bc} , v_{ca} = phase to phase armature voltages v = instantaneous rectifier output voltage V_{r.} = average output voltage V = variable defined by (21.) W = variable defined by (20.) β = angle at which commutation starts

 $\Delta_{\rm o}$ = constant defined by (36.)

 Λ_f , Λ_d = constants defined by (36.)

 λ_a , λ_b , λ_c , λ_f , λ_d , λ_q = flux linkages

 θ = time angle

 μ = commutation angle

ω = electrical angular velocity

- (L _a + M _a)	√3 K _f sin (ωt)	√3 K _d sin (wt)	$\sqrt{3}$ K cos (wt)	2 (La + Ma)	~~ ~~	-/3 K _{f w} cos (wt)	-/3 K _{d w cos (wt)}	/3 K w sin (wt)	-2R
$\sqrt{3}M_{\rm f}\cos\left(\omega t+\frac{\pi}{6}\right)$ $\sqrt{3}$ $M_{\rm d}\cos\left(\omega t+\frac{\pi}{6}\right)$ - $\sqrt{3}M_{\rm d}\sin\left(\omega t+\frac{\pi}{6}\right)$	0	0	1	√3 M _d cos (wt)	√3 M _{d ω cos (ωt+π/6)}	0	0	0	-/3 M _d w cos (wt) /3 M _d w sin (wt)
$\frac{\pi}{6}$) $\sqrt{3} M_{d} \cos (\omega t + \frac{1}{6})$	0	1	0	√3 M _d sin (ωt)	sin ($\omega t + \pi/6$) $\sqrt{3}$ M_d w sin ($\omega t + \pi/6$) $\sqrt{3}$ M_d w cos ($\omega t + \pi/6$)	0	0	0	
$(L_o + 2L_a + 2M_a)$ $\sqrt{3}M_f \cos(\omega t +$	$\sqrt{3} K_{f} \cos (\omega t + \frac{\pi}{6})$ 1	$\sqrt{3} \text{ K}_{d} \cos (\omega t + \frac{\pi}{6})$ 0	$-\sqrt{3} \text{ K}_{q} \sin (\omega t + \frac{\pi}{6})$ 0	+ M _a) $\sqrt{3}$ M _f sin (wt)	$-(R_{\rm p} + 2R_{\rm a}) \sqrt{3} M_{\rm f} \omega \sin(\omega t + \pi/6) \sqrt{3}$	$\sqrt{3} K_{\rm f} \omega \sin (\omega t + \pi/6)$ 0	√3 K _d w sin (wt+π/6) 0	√3 K _q w cos (wt+π/6) 0	R -/3 Mf w cos (wt)
(L, + 0, -		$[A] = \begin{vmatrix} A_{11} & A_{12} \\ A_{23} & A_{23} \end{vmatrix} = \sqrt{3} K_d$		(W + T) -	B. B.	=	[21 822] (3 K	√3 K	

APPENDIX III: MAIN PROGRAMS

The following programs are listed in alphabetical order. All subroutines except GELG and ARCSIN are listed in APPENDIX IV. It should be noted that the notation in the programs occasionally differs from that in the text:

Text	Program
La	Lo
Ma	^L ab

- 1. CONT: Finds the solution for the controlled rectifier bridge case.
- 2. MACH2: Finds the value of L_a which produces the minimum value of the 6th harmonic of v_a .
- 3. MAST: Finds the minimum filter weight for a given set of specifications
- 4. PLTDAT: General purpose program that includes various simulations for both the controlled and uncontrolled rectifier bridge.
- 5. SENSI3: Sensitivity analysis program.
- 6. TABLE: Determines the harmonics of v_o and $i_{f(rms)}$ for various values of L_a .
- 7. TESTR2: Calling program for fault current simulation.
- 8. UNCONT: Finds the solution for the uncontrolled rectifier bridge case.

```
MAIN PLOTTER PROGRAM
C
      DIMENSION FD(5),F(5,1),FF(5,5),MUS(50),RMSIF(50),
     1XRMS(50), ALIF(21), TRETA(21), TMU(21), FF1(4,4), F1(4,1),
     1FD1(4), ILS(50), BETAS(50), IFS(50), APIL(50), APBETA(50),
     1APMU(50),APIF(50),AHAR6(50),AHAR12(50),AHAR18(50),
     1AHAR24(50);AHAR30(50);APRMS(50);HAR6(50);HAR12(50);
     1HAR18(50),HAR24(50),HAR30(50),AL0(21),XHAR6(21),XHAR12(50),
     1XHAR18(21),XHAR24(21),XHAR30(21),AIQ(60),AID(60),AIF(60),
     1AIK(60), THETA(60)
      REAL*4 MO, MOO, MU, IF, IL, K1, LD, LF, MF, MFD, LAB, LO, MD, KQ,
     1NN1,NP2,OMEGA,LA,MUP,MUF,KFO,KAB,KOD,ILS,IFS,MUS,KF,KD
      INPUT MACHINE PARAMETERS
C
      WRITE (7,50)
50
      FORMAT('0',2X,' THIS IS THE DATA FOR THE PHASE CONTROLLED
     1 BRIDGE RECTIFIER')
      LF=0.12E 01
      LD=0.82E-07
      MF=0.79E-02
      MD=0.38E-05
      MFD=0.19E-03
      LAB=0.15E-03
      L0=0.3E-03
C
      LO=LA AND LAB=MA
      K1=1.0
      VL=6760.0
      IL=1420.0
      OMEGA=2513.27
      FREQ=400.0
      KF=(MF*LD-MD*MFD)/(LF*LD-(MFD)**2)
      KD=(MD*LF-MF*MFD)/(LF*LD-(MFD)**2)
      KQ=MD/LD
      MOO=MD**2/LD
      MO=MOO
      DELTAF=MO+MOO
      DELTAO=(1.333*(LO+LAB))-DELTAF
      DIL=1420.0/15.0
      KFO=MF/SQRT(LF*LO)
      KAB=LAB/LO
      KOD=MD/SQRT(LO*LD)
      DL0=0.0
      IL=1420.0
      KKK=0
      MF=KFO*SQRT(LF*LO)
      LAB=KAB*LO
      MD=KOD*SQRT(LO*LD)
      MOO=MD**2/LD
      00M=0M
      DELTAF=MO+MOO
      DELTAO=(1.3333*(LO+LAB))-DELTAF
      KF=(MF*LD-MD*MFD)/(LF*LD-(MFD)**2)
      CALL NEWTON(MU, BETA, IF, W, V, FREQ, DELTAO, IL, VL, MOO, K1,
     1MF, MO, OMEGA, DELTAF, ZETA)
      IL=0.0
      IF=1.1*IF
      DO 100 LLL=1,17
      KKK=0
```

CALL PHACON(IF, MF, BETA, MO, W, V, IL, MU, DELTAO, OMEGA, VL, MOO) APIL(LLL)=IL APRETA(LLL)=BETA*180.0/3.1416 APMU(LLL)=MU*180.0/3.1416 CALL FS(MU, BETA, OMEGA, IL, IF, MO, DELTAO, MF, W, V, LO, LAB, 1DELTAF, LLL, AHAR6, AHAR12, AHAR18, AHAR24, AHAR30) CALL RMS(BETA, LLL, MU, APRMS, IL, DELTAO, MF, MO, W, V, MOO, IF, 1KF, DELTAF) IL=IL+DIL 100 CONTINUE WRITE(7,300)LO, IF 300 FORMAT('0',5X,'L0=',E10.3,5X,'IF=',E10.3) WRITE(7,203) FORMAT('0',5X,'IL, IFRMS, 6TH, 12TH, 18TH, BETA, MU') 203 DO 201 KK=1,17 WRITE(7,202)APIL(KK), APRMS(KK), AHAR6(KK), AHAR12(KK), 1AHAR18(KK), APBETA(KK), APMU(KK) 201 CONTINUE FORMAT(' ',2X,F7,1,2X,F7,3,2X,E10,3,2X,E10,3,2X, 202 1E10.3,2X,F7.1,2X,F5.2) STOP END

MACH2

```
DIMENSION FD(5), F(5,1), FF(5,5), MUS(50), RMSIF(50),
     1XRMS(50),ALIF(21),TBETA(21),TMU(21),FF1(4,4),F1(4,1),
     1FD1(4), ILS(50), BETAS(50), IFS(50), APIL(50), APBETA(50),
     1APMU(50), APIF(50), AHAR6(50), AHAR12(50), AHAR18(50),
     1AHAR24(50), AHAR30(50), APRMS(50), HAR6(50), HAR12(50),
     1HAR18(50), HAR24(50), HAR30(50), ALO(21), XHAR6(21), XHAR12(50),
     1XHAR18(21),XHAR24(21),XHAR30(21),AIQ(60),AID(60),AIF(60),
     1AIK(60), THETA(60)
      REAL*4 MO, MOO, MU, IF, IL, K1, LD, LF, MF, MFD, LAB, LO, MD, KQ,
     1NN1,NP2,OMEGA,LA,MUP,MUF,KF0,KAB,KOD,ILS,IFS,MUS,KF,KD
      INPUT MACHINE PARAMETERS
C
      LF=0.12E 01
      LD=0.82E-07
      MF=0.79E-02
      MD=0.38E-05
      MFD=0.19E-03
      LAB=0.15E-03
      L0=0.3E-03
C
      LO=LA AND LAB=MA
      K1=1.0
      VL=6760.0
      IL=1420.0
      OMEGA=2513.27
      FREQ=400.0
      KF=(MF*LD-MD*MFD)/(LF*LD-(MFD)**2)
      KD=(MD*LF-MF*MFD)/(LF*LD-(MFD)**2)
      KQ=MD/LD
      M00=MD**2/LD
      MO=MOO
      DELTAF=MO+MOO
      DELTAO=(1.333*(LO+LAB))-DELTAF
      KFO=MF/SQRT(LF*LO)
      KAB=LAB/LO
      KOD=MD/SQRT(LO*LD)
      DL0=0.0
      H6M=9999.0
      DO 200 L=1,21
      LO=LO+DLO
      KKK=0
      MF=KF0*SQRT(LF*L0)
      LAB=KAB*LO
      MD=KOD*SQRT(LO*LD)
      MOO=MD**2/LD
      MO=MOO
      DELTAF=MO+MOO
      DELTAO=(1.3333*(LO+LAB))-DELTAF
      KF=(MF*LD-MD*MFD)/(LF*LD-(MFD)**2)
      CALL NEWTON (MU, BETA, IF, W, V, FREQ, DEL TAO, IL, VL, MOO, K1,
     1MF, MO, DMEGA, DELTAF, ZETA)
      DL0=0.03E-03
       IF=1.1*IF
      CALL PHACON(IF, MF, BETA, MO, W, V, IL, MU, DELTAO, OMEGA, VL, MOO)
      CALL FS(MU, BETA, OMEGA, IL, IF, MO, DELTAO, MF, W, V, LO, LAB,
     1DELTAF, L, AHAR6, AHAR12, AHAR18, AHAR24, AHAR30)
      CALL RMS(BETA, L, MU, APRMS, IL, DELTAO, MF, MO, W, V, MOO, IF,
     1KF, DELTAF)
      WRITE(7,302)L0,AHAR6(L),APRMS(L)
```

```
302
      FORMAT('0',2X,'LA = ',E10.3,5X,'6 TH HARMONIC OF VO = ',
     1E10.3,5X,'IF RMS = ',E10.3
      IF (H6M.LT.AHAR6(L)) GD TO 200
      H6M=AHAR6(L)
      BLA=LO
       BAPRMS=APRMS(L)
200
      CONTINUE
      WRITE(7,301)
      FORMAT('0',5X,'THIS IS THE OPTIMUM ARMATURE INDUCTANCE')
301
      WRITE(7,300)BLA, H6M, BAPRMS
      FORMAT('0',2X,'BEST LA =',E10.3,5X,'PEAK 6TH HARM. OF VO =',
300
     1E10.3,1X, 'PEAK IF RMS=',E10.3)
      LO=BLA
      MF=KFO*SQRT(LF*LO)
      LAB=KAB*LO
      MD=KOD*SQRT(LO*LD)
      LAB=KAB*LO
      MD=KOD*SQRT(LO*LD)
      MOO=MD*MD/LD
      MO=MO0
      DELTAF=MO+MOO
      DELTAO=(1.3333*(LO+LAB))-DELTAF
      KF=(MF*LD-MD*MFD)/(LF*LD-MFD*MFD)
      RETURN
      END
```

```
MASTER OPTOMIZATION OF L-C FILTER DESIGN
C
      REAL*4 K1,K2,ILFMAX,IF,MU,LA,LAB,LF,LD,MD,MF,MFD,
     1 IL, MO, LWT, LEN, N1, LO
21
      CONTINUE
      WRITE(7,1)
      WRITE(7,104)
      FORMAT('0',5X,'ALL INPUTS HAVE FORMAT = F7.2 UNLESS
104
     1 OTHERWISE SPECIFIED')
      FORMAT('0',1X,'WRITE THE FOLLOWING PARAMETERS FOR THE FILTER')
1
      WRITE(7,2)
      FORMAT('0',1X,'CAP. ENERGY DENSITY (JOULES/LB.) =')
100
      FORMAT(F7.2)
         FORMAT('0',5X,'FORMAT=12')
103
101
      FORMAT(12)
      READ(5,100)DC
      WRITE (7,4)
      FORMAT('0',1X,'CURRENT DENSITY FOR L WIRE (CIR MIL/AMP) =')
4
      READ(5,100)CMA
      WRITE (7,6)
      FORMAT('0',1X,'MAX. RMS VALUE OF 6TH HARM. OF VO (VOLTS) =')
6
      READ(5,100)V2
      WRITE(7,7)
      FORMAT('0',1X,'ALLOWABLE PEAK FAULT CURRENT (AMPS) =')
7
      READ(5,100) ILFMAX
      IL=1420.0
      VL=6760.0
      LF=1.2
      LD=0.82E-07
      MFD=0.19E-03
      OMEGA=2513.27
      DO 50 IZ=1,2
      IZ=1 IS FOR LA NORMAL
C
C
      IZ=2 IS OR LA OPTIMUM
      IF(IZ,EQ.2) GO TO 51
      IF=275.0
      BETA=2.12
      MU=0.307
      LA=0.300E-03
      LAB=0.15E-03
C
      LAB=MA
      MD=0.38E-05
      MF=0.79E-02
      W=144.0
      V=-138.0
      DELTA0=0.248E-03
      MO=0.176E-03
      V1=0.120E 04
      WRITE (7,53)LA
      FORMAT('0',2X,'THE FOLLOWING VALUES ARE BASED ON NORMAL
53
     1LA =',E10.3,2X,'H.')
      GO TO 52
51
       CONTINUE
      IL=1420.0
      IF=239.0
      BETA=2.28
      MU=0.604
      LA=0.720E-03
```

```
LAB=0.360E-03
C
      LAB=MA
      MD=0.589E-05
      MF=0.122E-01
      W=164.0
      V=-340.0
      DELTA0=0.595E-03
      M0=0.423E-03
      V1=620.0
      WRITE (7,54)LA
      FORMAT('0',2X,'THE FOLLOWING VALUES ARE BASED ON
54
     10PTIMUM LA =',E10.3,2X,'H.')
52
      WRITE(7,300) IF, BETA, MU
      FORMAT(' ',2X,'IF=',E10.3,5X,'BETA=',E10.3,5X,'MU=',E10.3)
300
      WRITE(7,305)IL, VL, V1
305
      FORMAT(' ',2X,'IL=',E10.3,5X,'VL=',E10.3,5X,'V1=',E10.3)
      K1=V2/V1
C
      FIND CONDUCTOR AREA IN CIR MILS & SQ. CM.
      CM=CMA*IL
      A16=(1+K1)/(K1*36*DMEGA**2)
       AM=CM*5.07E-10
       FW=AM
       F=0.7
       DW=5937.8
       A2=(VL*FW)**2*(K1+1)/(DC*51,1E-07*K1*36*(OMEGA**2)*F*F)
       A3=3*3.1416*F*DW
       A=(5*A2/(3*A3))**0.125
       N=A**2*F/FW
       LO=(25.5E-07)*((F/FW)**2)*(A)**5
      CO=A16/LO
         RES=N*3*3.1416*A*(2.83E-08)/FW
      WRITE(7,55)LO,CO,RES
      FORMAT('0',1X,'OPT, VALUES BEFORE FAULT TEST
55
     1 ARE LO=',E10.3,1X,'H., CO=',E10.3,1X,'FD.',1X,'RES=',E10.3)
          RES=N*3*3.1416*A*(2.83E-08)/FW
  15
      CALL FAULT2(IF, BETA, MU, LA, LAB, LF, LD, MD, MF, MFD, W, V, IL,
     10MEGA, DELTAO, MO, VL, LO, ILFMAX, RES)
      WRITE(7,345)IL
      FORMAT(' ',2X, 'MAX LOAD CURRENT FROM FAULT =',E10.3)
345
      IF(IL.LT.ILFMAX) GO TO 14
      K=K+1
      L0=L0*1.1
      CO=A16/LO
       A=((L0*(FW/F)**2)/25.5E-07)**0.2
       N=(A**2)*F/FW
      IF(K.GT.100) GO TO 14
      IL=1420.0
      IF(K.GT.2) GO TO 15
      WRITE(7,16)
      FORMAT('0',1X,'FAULT CURRENT TOO LARGE, LO INCREASED')
16
      GO TO 15
      CONTINUE
14
       LWT=A3*A**3
       CWT=A2/(A**5)
      WT=LWT+CWT
      WRITE(7,17)LO,CO,IL,RES
```

```
17
      FORMAT('0',1X,'L0=',E10.3,5X,'C0=',E10.3,5X,'ILF=',E10.3,1X,'
       RES=',E10.3)
      WRITE(7,18)LWT,CWT,WT
18
      FORMAT('0',1X,'LWT=',E10.3,5X,'CWT=',E10.3,5X,'TOTAL WT =',E10.3)
      RAD=2*A
      WRITE(7,19)N,RAD,A
19
      FORMAT('0',1X,'NO. TURNS =',14,5X,'L RADIUS =',
     1E10.3, 'M', 5X, 'L LENGTH =', E10.3, 'M')
50
      CONTINUE
      WRITE(7,20)
20
      FORMAT('0',1X,'WRITE "0" TO END, OR "1" FOR ANOTHER RUN')
      WRITE(7,103)
      READ(5,101)KEY
      IF(KEY.GT.0) GO TO 21
      STOP
      END
```

```
MAIN PLOTTER PROGRAM
C
      DIMENSION FD(5), F(5,1), FF(5,5), MUS(50), RMSIF(50),
     1XRMS(50),ALIF(21),TBETA(21),TMU(21),FF1(4,4),F1(4,1),
     1FD1(4), ILS(50), BETAS(50), IFS(50), APIL(50), APBETA(50),
     1APMU(50), APIF(50), AHAR6(50), AHAR12(50), AHAR18(50),
     1AHAR24(50),AHAR30(50),APRMS(50),HAR6(50),HAR12(50),
     1HAR18(50), HAR24(50), HAR30(50), ALO(21), XHAR6(21), XHAR12(50),
     1XHAR18(21),XHAR24(21),XHAR30(21),AIQ(60),AID(60),AIF(60),
     1AIK(60), THETA(60)
      REAL*4 MO, MOO, MU, IF, IL, K1, LD, LF, MF, MFD, LAB, LO, MD, KQ,
     1NN1,NP2,OMEGA,LA,MUP,MUF,KFO,KAB,KOD,ILS,IFS,MUS,KF,KD
      INPUT MACHINE PARAMETERS
C
      LF=0.12E 01
      LD=0.82E-07
      MF=0.79E-02
      MD=0.38E-05
      MFD=0.19E-03
      LAB=0.15E-03
      L0=0.3E-03
      LO=LA AND
C
                  LAB=MA
      K1=1.0
      VL=6760.0
      IL=1420.0
      OMEGA=2513.27
      FREQ=400.0
      KF=(MF*LD-MD*MFD)/(LF*LD-(MFD)**2)
      KD = (MD \times LF - MF \times MFD) / (LF \times LD - (MFD) \times \times 2)
      KQ=MD/LD
      M00=MD**2/LD
      MO=MOO
      DELTAF=MO+MOO
      DELTAO=(1.333*(LO+LAB))-DELTAF
      DIL=2130.0/50.0
      CALL NEWTON (MU, BETA, IF, W, V, FREQ, DELTAO, IL, VL, MOO, K1,
     1MF, MO, OMEGA, DELTAF, ZETA)
      CALL LITLI(DELTAO, MF, IF, BETA, MO, W,
     1MOO,V,IL,DELTAF,MU,AID,AIQ,AIF,AIK,THETA,KQ,KF,KD)
      KF0=MF/SQRT(LF*L0)
      KAB=LAB/LO
      KOD=MD/SQRT(LO*LD)
      DL0=0.0
      IL=1420.0
      DO 200 L=1,21
      LO=LO+DLO
      KKK=0
      MF=KFO*SQRT(LF*LO)
      LAB=KAB*LO
      MD=KOD*SQRT(LO*LD)
      MOO=MD**2/LD
      MO=MOO
      DELTAF=MO+MOO
      DELTAO=(1.3333*(LO+LAB))-DELTAF
      KF=(MF*LD-MD*MFD)/(LF*LD-(MFD)**2)
      CALL NEWTON(MU, BETA, IF, W, V, FREQ, DELTAO, IL, VL, MOO, K1,
     1MF, MO, OMEGA, DELTAF, ZETA)
      IF=1.1*IF
      CALL PHACON(IF, MF, BETA, MO, W, V, IL, MU, DELTAO, OMEGA, VL, MOO)
```

```
ALO(L)=LO
      CALL FS(MU, BETA, OMEGA, IL, IF, MO, DELTAO, MF, W, V, LO, LAB,
     1DELTAF, L, XHAR6, XHAR12, XHAR18, XHAR24, XHAR30)
      CALL RMS(BETA, L, MU, XRMS, IL, DELTAO, MF, MO, W, V, MOO, IF,
     1KF, DELTAF)
      ALIF(L)=IF
      TBETA(L)=BETA*180./3.1416
      TMU(L)=MU*180./3.1416
      DL0=0.03E-03
200
      CONTINUE
      WRITE(7,201)
      DO 202 L=1,21
      WRITE(7,203)ALO(L),XRMS(L),XHAR6(L),XHAR12(L),XHAR18(L),
     1TBETA(L), TMU(L)
202
      CONTINUE
      FORMAT(' ',5X,'L0',10X,'IF',10X,'6TH',10X,'12TH',10X,'18TH',
201
     112X, 'BETA', 12X, 'MU')
      FORMAT(' ',1X,7E13.4)
203
      L0=0.3E-03
      LAB=0.15E-03
      MD=0.38E-05
      MOO=MD*MD/LD
      M0=M00
      MF=0.79E-02
      KF=(MF*LD-MD*MFD)/(LF*LD-MFD*MFD)
      DELTAF=MO+MOO
      DELTAO=(1.3333*(LO+LAB))-DELTAF
      IL=0.0
      WRITE(7,2800)
      DO 100 LLL=1,50
      KKK=0
      CALL NEWTON (MU, BETA, IF, W, V, FREQ, DELTAO, IL, VL, MOO, K1,
     1MF, MO, DMEGA, DELTAF, ZETA)
      ILS(LLL)=IL
      BETAS(LLL)=BETA*180.0/3.1416
      MUS(LLL)=MU*180.0/3.1416
      IFS(LLL)=IF
      FORMAT(' ',4X,'IL',8X,'BETA',7X,'MU',8X,'IF')
2800
      FORMAT('0',2X,F7.1,4X,F6.2,4X,F6.3,4X,F6.1,4X,F6.1,4X,F6.1)
2801
      CALL FS(MU, BETA, OMEGA, IL, IF, MO, DELTAO, MF, W, V, LO, LAB,
     1DELTAF, LLL, HAR6, HAR12, HAR18, HAR24, HAR30)
      CALL RMS(BETA, LLL, MU, RMSIF, IL, DELTAO, MF, MO, W, V, MOO, IF,
     1KF, DELTAF)
      IF=1.1*IF
      CALL PHACON(IF, MF, BETA, MO, W, V, IL, MU, DELTAO, OMEGA, VL, MOO)
      APIL(LLL)=IL
      APBETA(LLL)=BETA
      APMU(LLL)=MU
      APIF(LLL)=IF
      CALL FS(MU, BETA, OMEGA, IL, IF, MO, DELTAO, MF, W, V, LO, LAB,
     1DELTAF, LLL, AHAR6, AHAR12, AHAR18, AHAR24, AHAR30)
      CALL RMS(BETA, LLL, MU, APRMS, IL, DELTAO, MF, MO, W, V, MOO, IF,
     1KF, DELTAF)
      IL=IL+DIL
      IF(LLL.EQ.1) IL=35.0
100
      CONTINUE
      DO 101 LLL=1,50
```

```
WRITE(7,2801)ILS(LLL), BETAS(LLL), MUS(LLL), IFS(LLL)
101
      CONTINUE
      DO 102 LLL=1,50
      WRITE(7,2802)LLL, HAR6(LLL), HAR12(LLL), HAR18(LLL), HAR24(LLL),
     1HAR30(LLL)
      FORMAT(' ',1X,13,5E13.4)
2802
102
      CONTINUE
      DO 103 LLL=1,50
      WRITE(7,2803)LLL, RMSIF(LLL)
2803
      FORMAT(' ',1X,14,E20.5)
103
      CONTINUE
      DO 104 L=1,50
      WRITE(7,2802)L, AHAR6(L), AHAR12(L), AHAR18(L), AHAR24(L), AHAR30(L)
 104
      CONTINUE
      DO 105 L=1,50
      WRITE(7,2803)L, APRMS(L)
105
      CONTINUE
      WRITE(7,110)
      FORMAT('0',1X,'IL, BETA, MU, IF -- WITH PHASE CONT')
110
      DO 106 L=1,50
      WRITE(7,107)APIL(L),APBETA(L),APMU(L),APIF(L)
107
      FORMAT('0',1X,4E13.4)
106
      CONTINUE
      STOP
      END
```

```
C
      TEST PROGRAM FOR NEWTON SENSITIVITY ANALYSIS
      DIMENSION FD(5),F(5,1),FF(5,5),AIF(11),ABETA(11),AMU(11),
     1AW(11),AV(11),A1(11),AMO(11),AMOO(11),ALAMD(11)
      REAL*4 MO, MOO, MU, IF, IL, K1, LD, LF, MF, MFD, LAB, LO, MD, KQ, ILFMAX,
     1LA,KFO,KAB,KOD,KF,KD,IK,MA,IFT,IQ,LAMQ,LAMD,ILO,ILC,IKO,IKC
      DO 34 I1=1,7
      LF=0.12E 01
      LD=0.82E-07
      MF=0.79E-02
      MD=0.38E-05
      MFD=0.19E-03
      LAB=0.15E-03
      L0=0.3E-03
C
      LO=LA AND LAB=MA
      CAF=MF/SQRT(LO*LF)
      CAB=LAB/LO
      CAD=MD/SQRT(LO*LD)
      CFD=MFD/SQRT(LF*LD)
      DO 35 I2=1,11
      IF(I1.GT.6) GO TO 36
      IF(I1.GT.5) GO TO 37
      IF(I1.GT.4) GO TO 38
      IF(I1.GT.3) GO TO 39
      IF(I1.GT.2) GO TO 40
      IF(I1.GT.1) GO TO 41
      LF=0.6+0.12*(I2-1)
      MF=CAF*SQRT(LO*LF)
      MFD=CFD*SQRT(LF*LD)
      A1(I2)=LF
      GO TO 42
       LD=0.41E-07+(0.082E-07)*(12-1)
41
      MD=CAD*SQRT(LO*LD)
      MFD=CFD*SQRT(LF*LD)
      A1(I2)=LD
      GO TO 42
      MF=0.395E-02+(0.079E-02)*(12-1)
40
      A1(I2)=MF
      GO TO 42
39
      MFD=0.095E-03+(0.019E-03)*(12-1)
      A1(12)=MFD
      GO TO 42
      MD=0.19E-05+(0.038E-05)*(12-1)
38
      A1(I2)=MD
      GO TO 42
37
      LAB=0.075E-03+(0.015E-03)*(12-1)
      A1(12)=LAB
      GO TO 42
      LO=0.15E-03+(0.03E-03)*(12-1)
36
      MF=CAF*SQRT(LO*LF)
      MD=CAD*SQRT(LO*LD)
      LAB=CAB*LO
      A1(12)=L0
      CONTINUE
42
      K1=1.0
      VL=6760.0
      IL=1420.0
      OMEGA=2513.27
```

```
FREQ=400.0
KF=(MF*LD-MD*MFD)/(LF*LD-MFD*MFD)
KD=(MD*LF-MF*MFD)/(LF*LD-MFD*MFD)
KQ=MD/LD
M00=MD**2/LD
 AM00(12)=M00
AMO(I2)=KF*MF+KD*MD
 ALAMD(12)=AMO(12)-MOO
MO=MOO
 DELTAF=MO+MOO
DELTAO=(1.3333*(LO+LAB))-DELTAF
 CONTINUE
CALL NEW3ON(MU, BETA, IF, W, V, FREQ, DELTAO, IL, VL, MOO, K1,
1MF, MO, OMEGA, DELTAF, ZETA, K)
IF(K.LT.200) GD TD 80
AIF(12)=0.0
ABETA(12)=0.0
AMU(12)=0.0
AW(12)=0.0
AU(12)=0.0
GO TO 35
CONTINUE
AIF(I2)=IF
ABETA(12)=BETA
AMU(I2)=MU
AW(12)=W
AU(12)=V
CONTINUE
IF(I1.GT.6) GO TO 46
IF(I1.GT.5) GO TO 47
IF(I1.GT.4) GO TO 48
IF(I1.GT.3) GO TO 49
IF(I1.GT.2) GO TO 50
IF(I1.GT.1) GO TO 51
WRITE(7,100)
FORMAT('0',5X,'LF VARIATION')
GO TO 52
 WRITE(7,101)
FORMAT('0',5X,'LD VARIATION')
GO TO 52
WRITE(7,102)
FORMAT('0',5X,'MF VARIATION')
GO TO 52
WRITE(7,103)
FORMAT('0',5X,'MFD VARIATION')
GO TO 52
WRITE(7,104)
FORMAT('0',5X,'MD VARIATION')
GO TO 52
WRITE(7,105)
FORMAT('0',5X,'LAB VARIATION')
GO TO 52
WRITE(7,106)
FORMAT('0',5X,'LO VARIATION')
CONTINUE
WRITE(7,120)
FORMAT('0',7X, 'PARAMETER'8X, 'IF',11X, 'BETA',11X, 'MU',
```

0

1

2

)3

14

15

16

30

2

```
113X,'W',13X,'V',11X,'MOO',12X,'MO',11X,'LAMD')
DD 55 L=1,11
WRITE(7,110)A1(L),AIF(L),ABETA(L),AMU(L),AW(L),AV(L),
1AMOO(L),AMO(L),ALAMD(L)
FORMAT(' ',2X,9E14.4)
CONTINUE
CONTINUE
STOP
END
```

C

C

```
PROGRAM TABLE.FOR
MAIN PLOTTER PROGRAM
DIMENSION FD(5), F(5,1), FF(5,5), MUS(50), RMSIF(50),
1XRMS(50), ALIF(21), TBETA(21), TMU(21), FF1(4,4), F1(4,1),
1FD1(4), ILS(50), BETAS(50), IFS(50), APIL(50), APRETA(50),
1APMU(50), APIF(50), AHAR6(50), AHAR12(50), AHAR18(50),
1AHAR24(50), AHAR30(50), APRMS(50), HAR6(50), HAR12(50),
1HAR18(50), HAR24(50), HAR30(50), ALO(21), XHAR6(21), XHAR12(50),
1XHAR18(21),XHAR24(21),XHAR30(21),AIQ(60),AID(60),AIF(60),
1AIK(60), THETA(60)
REAL*4 MO, MOO, MU, IF, IL, K1, LD, LF, MF, MFD, LAB, LO, MD, KQ,
1NN1,NP2,OMEGA,LA,MUP,MUF,KFO,KAB,KOD,ILS,IFS,MUS,KF,KD
 INPUT MACHINE PARAMETERS
LF=0.12E 01
LD=0.82E-07
MF=0.79E-02
MD=0.38E-05
MFD=0.19E-03
LAB=0.15E-03
L0=0.3E-03
K1=1.0
VL=6760.0
IL=1420.0
OMEGA=2513.27
FREQ=400.0
KF=(MF*LD-MD*MFD)/(LF*LD-(MFD)**2)
KD=(MD*LF-MF*MFD)/(LF*LD-(MFD)**2)
KQ=MD/LD
M00=MD**2/LD
M0=M00
DELTAF=MO+MOO
DELTAO=(1.333*(LO+LAB))-DELTAF
DIL=1420.0/15.0
KFO=MF/SQRT(LF*LO)
KAB=LAB/LO
KOD=MD/SQRT(LO*LD)
DL0=0.0
DO 200 L=1,21
IL=1420.0
LO=LO+DLO
KKK=0
MF=KFO*SQRT(LF*LO)
LAB=KAB*LO
MD=KOD*SQRT(LO*LD)
MOO=MD**2/LD
MO=MOO
DELTAF=MO+MOO
DELTAO=(1.3333*(LO+LAB))-DELTAF
KF=(MF*LD-MD*MFD)/(LF*LD-(MFD)**2)
CALL NEWTON (MU, BETA, IF, W, V, FREQ, DELTAO, IL, VL, MOO, K1,
1MF, MO, OMEGA : DEL TAF, ZETA)
DL0=0.03E-03
IL=0.0
IF=1.1*IF
DO 100 LLL=1,17
KKK=0
CALL PHACON(IF, MF, BETA, MO, W, V, IL, MU, DELTAO, OMEGA, VL, MOO)
```

```
APIL(LLL)=IL
      APBETA(LLL)=BETA*180.0/3.1416
      AFMU(LLL)=MU*180.0/3.1416
      CALL FS(MU, BETA, OMEGA, IL, IF, MO, DELTAO, MF, W, V, LO, LAB,
     1DELTAF, LLL, AHAR6, AHAR12, AHAR18, AHAR24, AHAR30)
      CALL RMS(BETA, LLL, MU, APRMS, IL, DELTAO, MF, MO, W, V, MOO, IF,
     1KF, DELTAF)
      IL=IL+DIL
100
      CONTINUE
      WRITE(7,300)L0,IF
300
      FORMAT('0',5X,'L0=',E10.3,5X,'IF=',E10.3)
      WRITE(7,203)
      FORMAT('0',5X,'IL, IFRMS, 6TH, 12TH, 18TH, BETA, MU')
203
      DO 201 KK=1,17
       WRITE(7,202)APIL(KK), APRMS(KK), AHAR6(KK), AHAR12(KK),
     1AHAR18(KK), APBETA(KK), APMU(KK)
201
      CONTINUE
      CONTINUE
FORMAT(' ',2X,F7.1,2X,F7.3,2X,E10.3,2X,E10.3,2X,
200
202
     1E10.3,2X,F7.1,2X,F5.2)
      STOP
      END
```

```
TEST PROGRAM FOR FAULT
C
      DIMENSION FD(5,1),F(5,1),FF(5,5),A(4,4),B(5,5),RH(5,1),CIL(300),
     1CIK(300), CWT(300)
      REAL*4 MO, MOO, MU, IF, IL, K1, LD, LF, MF, MFD, LAB, LO, MD, KQ, ILFMAX,
     1LA,KFO,KAB,KOD,KF,KD,IK,MA,IFT,IQ,LAMQ,LAMD,ILO,ILC,IKO,IKC
      LF=0.12E 01
      LD=0.82E-07
      MF=0.79E-02
      MD=0.38E-05
      MFD=0.19E-03
      LAB=0.15E-03
      L0=0.3E-03
      LA=LO
      ILFMAX=0.1E 06
      WRITE(7,200)
200
      FORMAT('0',2X,'TYPE THE VALUE OF RP DESIRED')
      READ(5,201)RP
201
      FORMAT(E20.10)
      K1=1.0
      VL=6760.0
      IL=1420.0
      OMEGA=2513.27
      FREQ=400.0
      KF=(MF*LD-MD*MFD)/(LF*LD-MFD*MFD)
      KD=(MD*LF-MF*MFD)/(LF*LD-MFD*MFD)
      KQ=MD/LD
      M00=MD**2/LD
      00M=0M
      DELTAF=MO+MOO
      DELTAO=(1.3333*(LO+LAB))-DELTAF
      CALL NEWTON (MU, BETA, IF, W, V, FREQ, DELTAO, IL, VL, MOO, K1,
     1MF,MO,DMEGA,FELTAF,ZETA)
500
      WRITE(7,299)
      FORMAT('0',1X, 'ENTER VALUE OF LO DESIRED---FORMAT E10.3')
299
      READ(5,298)LO
298
      FORMAT(E10.3)
      FORMAT(' ',1X,5E13.4)
10
      IL=1420.0
      CALL FAULT2(IF, BETA, MU, LA, LAB, LF, LD, MD, MF, MFD, W, V, IL,
     10MEGA, DELTAO, MO, VL, LO, ILFMAX, RP)
      WRITE(7,300)IL
      FORMAT('0',3X,'ILMAX FROM FAULT =',E10,3)
300
      WRITE (7,600)
      FORMAT('0',3X,'TYPE "O" TO END, OR "1" FOR ANOTHER RUN')
600
      READ(5,700)KEY
700
      FORMAT(I4)
      IF(KEY.GT.O) GO TO 500
      STOP
```

END

UNCONT

```
MAIN PLOTTER PROGRAM
C
      DIMENSION FD(5),F(5,1),FF(5,5),MUS(50),RMSIF(50),
     1XRMS(50),ALIF(21),TBETA(21),TMU(21),FF1(4,4),F1(4,1),
     1FD1(4), ILS(50), BETAS(50), IFS(50), APIL(50), APBETA(50),
     1APMU(50), APIF(50), AHAR6(50), AHAR12(50), AHAR18(50),
     1AHAR24(50), AHAR30(50), APRMS(50), HAR6(50), HAR12(50),
     1HAR18(50), HAR24(50), HAR30(50), ALO(21), XHAR6(21), XHAR12(50),
     1XHAR18(21),XHAR24(21),XHAR30(21),AIQ(60),AID(60),AIF(60),
     1AIK(60), THETA(60)
      REAL*4 MO,MOO,MU,IF,IL,K1,LD,LF,MF,MFD,LAB,LO,MD,KQ,
     1NN1,NP2,OMEGA,LA,MUF,MUF,KFO,KAB,KOD,ILS,IFS,MUS,KF,KD
C
      INPUT MACHINE PARAMETERS
      WRITE(7,50)
50
      FORMAT('0',2X,' THIS IS THE DATA FOR THE UNCONTROLLED
     1 BRIDGE RECTIFIER')
      LF=0.12E 01
      LD=0.82E-07
      MF=0.79E-02
      MD=0.38E-05
      MFD=0.19E-03
      LAB=0.15E-03
      L0=0.3E-03
C
      LO=LA AND
                 LAB=MA
      K1=1.0
      VL=6760.0
      IL=1420.0
      OMEGA=2513.27
      FREQ=400.0
      KF=(MF*LD-MD*MFD)/(LF*LD-(MFD)**2)
      KD=(MD*LF-MF*MFD)/(LF*LD-(MFD)**2)
      KQ=MD/LD
      MOO=MD**2/LD
      00M=0M
      DELTAF=MO+MOO
      DELTAO=(1.333*(LO+LAB))-DELTAF
      DIL=1420.0/15.0
      KFO=MF/SQRT(LF*LO)
      KAB=LAB/LO
      KOD=MD/SQRT(LO*LD)
      IIL 0=0.0
      IL=1420.0
      KKK=0
      MF=KFO*SQRT(LF*LO)
      LAB=KAB*LO
      MD=KOD*SQRT(LO*LD)
      MOO=MD**2/LD
      MO=MOO
      DELTAF=MO+MOO
      DELTAO=(1.3333*(LO+LAB))-DELTAF
      KF=(MF*LD-MD*MFD)/(LF*LD-(MFD)**2)
      IL=0.0
      DO 100 LLL=1,17
      KKK=0
      CALL NEWTON (MU, BETA, IF, W, V, FREQ, DELTAO, IL, VL, MOO, K1,
     1MF,MO,OMEGA,DELTAF,ZETA)
      APIL(LLL)=IL
```

AFIF(LLL)=IF APRETA(LLL)=BETA*180.0/3.1416 APMU(LLL)=MU*180.0/3.1416 CALL FS(MU, BETA, OMEGA, IL, IF, MO, DELTAO, MF, W, V, LO, LAB, 1DELTAF, LLL, AHAR6, AHAR12, AHAR18, AHAR24, AHAR30) CALL RMS(BETA, LLL, MU, APRMS, IL, DELTAO, MF, MO, W, V, MOO, IF, 1KF , DELTAF) IL=IL+DIL CONTINUE 100 WRITE(7,300)L0 FORMAT('0',5X,'L0=',E10,3) 300 WRITE (7,203) FORMAT('0',5X,'IL, IFRMS, 6TH, 12TH, 18TH, BETA, MU, IF') 203 DO 201 KK=1,17 WRITE(7,202)APIL(KK), APRMS(KK), AHAR6(KK), AHAR12(KK), 1AHAR18(KK), APBETA(KK), APMU(KK), APIF(KK) 201 CONTINUE 202 FORMAT(' ',2X,F7,1,2X,F7,3,2X,E10,3,2X,E10,3,2X, 1E10.3,2X,F7.1,2X,F5.2,3X,F6.2) STOP END

APPENDIX IV. SUBROUTINES

The following subroutines for the main programs of Appendix III are listed in alphabetical order. Subroutines GELG and ARSIN are not included. GELG is a program for solving simultaneous equations that is part of the IBM Scientific Subroutine Package. ARSIN is a series for the arcsin function. It should be noted that the notation in the programs occasionally varies from that in the text:

Text	Program
L _a	Lo
Ma	Lab

- 1. FS: Finds the harmonics of v.
- 2. FAULT2: Calculates the fault current.
- 3. JACOB: Calculates the Jacobian matrix for the uncontrolled rectifier bridge.
- 4. <u>JACOB4</u>: Calculates the Jacobian matrix for the controlled rectifier bridge.
- 5. LITLI: Calculates i_d , i_q , i_f and i_k vs. θ .
- 6. <u>NEWTON</u>: Newton-Raphson algorithm for the uncontrolled rectifier bridge.
- 7. NEW30N: Same as NEWTON except variable K is included in argument list to test for convergence. Used only with SENSI3.
- 8. PHACON: Newton-Raphson algorithm for the controlled rectifier bridge.

- 9. RHS: Calculates right hand side vector for NEWTON.
- 10. RHS4B4: Calculates right hand side vector for PHACON.
- 11. RMS: Find rms value of i_f .
- 12. TERMA: Performs repetitive calculation for FS.

```
SUBROUTINE FS(MU, BETA, OMEGA, IL, IF, MO, DELTAO, MF, W, V, LO, LAB,
1DELTAF, LLL, HAR6, HAR12, HAR18, HAR24, HAR30)
DIMENSION CN(5), HAR6(50), HAR12(50), HAR18(50), HAR24(50), HAR30(50)
REAL*4 MU, IL, IF, MO, MF, LO, LAB
A=-OMEGA*(1.732*IF*MF+2.865*M0*W)*1.91
B=2.865*DMEGA*MO*V*1.91
C=-2.865*OMEGA*IL*MO*1.91
DD=(DMEGA/DELTAO)*(1.5*MO-LO-LAB)
D=DD*(1.155*MF*IF+1.91*MO*W)*1.91
E=+1.91*MO*V*DD*1.91
F=0.955*IL*DELTAF*DD*1.91
DO 10 K=1,5
B1=BETA+MU-1.047
B2=B1+1.047
N=K*6
CALL TERMA(N,A,2.094,B2,AN1,BN1)
AN=AN1
BN=BN1
CALL TERMA(N,A,2,094,B1,AN1,BN1)
AN=AN-AN1
BN=BN-BN1
CALL TERMA(N, B, 0.524, B2, AN1, BN1)
AN=AN+AN1
BN=BN+BN1
CALL TERMA(N,B,0.524,B1,AN1,BN1)
 AN=AN-AN1
BN=BN-BN1
ANG=2.094-BETA-MU
CALL TERMA(N,C,ANG,B2,AN1,BN1)
AN=AN+AN1
 BN=BN+BN1
CALL TERMA(N,C,ANG,B1,AN1,BN1)
 AN=AN-AN1
 BN=BN-BN1
B1=BETA
B2=BETA+MU
CALL TERMA(N,D,O.O,B2,AN1,BN1)
AN=AN+AN1
BN=BN+BN1
CALL TERMA(N,D,O.O,B1,AN1,BN1)
AN=AN-AN1
BN=BN-BN1
CALL TERMA(N,E,1.571,B2,AN1,BN1)
AN=AN+AN1
BN=BN+BN1
CALL TERMA(N,E,1.571,B1,AN1,BN1)
AN=AN-AN1
BN=BN-BN1
ANG=-BETA-MU
CALL TERMA(N,F,ANG,B2,AN1,BN1)
AN=AN+AN1
BN=BN+BN1
CALL TERMA(N,F,ANG,B1,AN1,BN1)
AN=AN-AN1
BN=BN-BN1
CN(K)=SQRT(AN**2+BN**2)
```

10 CONTINUE HAR6(LLL)=CN(1) HAR12(LLL)=CN(2) HAR18(LLL)=CN(3) HAR24(LLL)=CN(4) HAR30(LLL)=CN(5) RETURN END

```
SUBROUTINE FAULT2(IF, BETA, MU, LA, LAB, LF, LD, MD, MF, MFD, W, V, IL,
     10MEGA, DELTAO, MO, VL, LO, ILFMAX, RP)
      ROTOR FLUX LINKAGES ASSUMED CONSTANT
C
      DIMENSION A(4,4),B(5,5),CIL(300),CIK(300),CWT(300),
     1ARH(4,1),BRH(5,1)
      REAL*4 LO,KD,KF,KQ,IK,IF,MU,LA,LAB,LF,LD,MD,MF,MFD,IL,IFT,
     1ID, IQ, LAMQ, LAMF, LAMD, ILO, ILC, IKO, IKC, MO, ILFMAX
      KK=0
      JJ=0
      SPECIFY INITIAL CONDITIONS FOR CONDUCTION PERIOD
      WT=BETA+MU-1.047
      L0=0.1
      KD=(MD*LF-MF*MFD)/(LF*LD-MFD*MFD)
      KF=(MF*LD-MD*MFD)/(LF*LD-MFD*MFD)
      KQ=MD/LD
      IFT=IF+1.732*KF*((3/3.1416)*(W+IL*
     1COS(BETA+MU))-(IL*COS(WT+0.524)))
      ID=(IFT-IF)*KD/KF
      IQ=1.732*KQ*((3/3.1416)*(V-IL*SIN(BETA+MU))
     1+IL*SIN(WT+0.524))
      F1=1/(LF*LD-MFD*MFD)
      LAMQ=-1.732*MD*IL*SIN(WT+0.524)+LD*IQ
      LAMF=1.732*IL*MF*COS(WT+0.524)+LF*IFT+MFD*ID
      LAMD=1.732*IL*MD*COS(WT+0.524)+MFD*IFT+LD*ID
      SF=F1*(LAMF*LD-LAMD*MFD)
      SD=F1*(LAMD*LF-LAMF*MFD)
      SQ=LAMQ/LD
      A(1,1)=L0+2*(LA+LAB)
      A(2,2)=1.0
      A(3,3)=1.0
      A(4,4)=1.0
      A(2,3)=0.0
      A(2,4)=0.0
      A(3,2)=0.0
      A(3,4)=0.0
      A(4,2)=0.0
      A(4,3)=0.0
      B(1,1)=L0+2*(LA+LAB)
      B(2,2)=1.0
      B(3,3)=1.0
      B(4,4)=1.0
      B(2,3)=0.0
      B(2,4)=0.0
      B(3,2)=0.0
      B(3,4)=0.0
      B(4,2)=0.0
      B(4,3)=0.0
      B(5,1)=-LA-LAB
      B(5,5)=2*(LA+LAB)
      B(1,5)=-LA-LAB
      GO INTO CONDUCTION DO LOOP
      DWT=3.1416/150
      DT=DWT/2513.3
      WT=WT+0.524
      JUMP=0
110
      WT=WT-1.047*JUMP
      JUMP=JUMP+1
```

```
IF(JUMP.GE.4) GO TO 99
      RA=0.0164
      DO 1 K=1,3000
      KEY=0
      ILO=IL
12
      KEY=KEY+1
      IF(KEY.GT.2) GO TO 71
C
      FIND DY/DX AT O
      A(1,2)=1.732*MF*COS(WT)
      A(1,3)=1.732*MD*COS(WT)
      A(1,4) = -1.732 * MD * SIN(WT)
      A(2,1)=1.732*KF*COS(WT)
      A(3,1)=+1.732*KD*COS(WT)
      A(4,1)=-1.732*KQ*SIN(WT)
      CONTINUE
71
      ARH(1,1)=-(RP+2*RA)*IL+1.732*MF*DMEGA*SIN(WT)*
     1IFT+1.732*MD*OMEGA*SIN(WT)*ID
     1+1.732*MD*OMEGA*COS(WT)*IQ
      ARH(2,1)=1.732*KF*DMEGA*SIN(WT)*IL
      ARH(3,1)=+1.732*KD*OMEGA*SIN(WT)*IL
      ARH(4,1)=1.732*KQ*OMEGA*COS(WT)*IL
      ARH(1,1)=(ARH(1,1)-A(1,2)*ARH(2,1)-A(1,3)*ARH(3,1)
     1-A(1,4)*ARH(4,1))/(A(1,1)-A(1,2)*A(2,1)
     1-A(1,3)*A(3,1)-A(1,4)*A(4,1))
      ARH(2,1)=ARH(2,1)-A(2,1)*ARH(1,1)
      ARH(3,1)=ARH(3,1)-A(3,1)*ARH(1,1)
      ARH(4,1) = ARH(4,1) - A(4,1) * ARH(1,1)
      ARH(1,1)=DIL/DT AT 0
      IF(KEY.GT.1) GO TO 2
      WT=WT+DWT
      IL=IL+ARH(1,1)*DT
      ILC=IL
      DILDT=ARH(1,1)
      GO TO 3
      CONTINUE
2
      IL=ILO+((DILDT+ARH(1,1))*DT)/2
3
      CONTINUE
      IFT=SF-1.732*IL*COS(WT)*KF
      ID=SD-1.732*IL*COS(WT)*KD
      IQ=SQ+1.732*KQ*IL*SIN(WT)
      IF(KEY.LT.2) GO TO 12
      IF (ABS(IL-ILC).LE.1.0) GO TO 10
      ILC=IL
      IF(KEY.GT.50) GO TO 997
      GO TO 12
      CONTINUE
10
      KK=KK+1
      CIL(KK)=IL
      IF(IL.GT.ILFMAX) GO TO 997
      CIK(KK)=0.0
      IF(KK,GE,299) GO TO 997
301
      CONTINUE
      TEST FOR END OF CONDUCTION PERIOD
C
      UBCT=RA*IL+(LAB+LA)*ARH(1,1)-1.732*MF*SIN(WT-0.524)*ARH(2,1)
     1-1.732*OMEGA*COS(WT-0.524)*(MF*IFT+MD*ID)
     1-1.732*MD*SIN(WT-0.524)*ARH(3,1)-1.732*MD*COS(WT-0.524)*AFH(4,1)
     1+1.732*MD*OMEGA*SIN(WT-0.524)*IQ
```

```
FAULT IS PRESENT FOR 1 CONDUCTION PERIOD PLUS 1
C
C
      COMMUTATION PERIOD + 1 COMMUTATION PERIOD WHERE NEXT SCRS
C
      ARE BLANKED--PROGRAM ENDS WHEN PEAD IL IS PAST
      IF((JUMP.GE.2).AND.(IL.LT.CIL(KK-1))) GO TO 99
      IF(JUMP.GE.2) GO TO 1
      IF(VBCT.GT.O.O) GO TO 11
1
      CONTINUE
      WRITE(7,720)
720
      FORMAT(' ',5X,'CONDUCTION PERIOD DOES NOT END')
      GO TO 997
       CONTINUE
11
C
      CALCULATE COMMUTATION INTERVAL
      IK=0.0
      DO 26 K=1,200
      KEY=0
      ILO=IL
      IKO=IK
120
      KEY=KEY+1
      IF(KEY.GT.2) GO TO 70
C
      FIND DY/DX AT O
      B(1,2)=1.732*MF*COS(WT)
      B(1,3)=1.732*MD*COS(WT)
      B(1,4) = -1.732 * MD * SIN(WT)
      B(2,1)=1.732*KF*COS(WT)
      B(2,5)=1.732*KF*SIN(WT-0.524)
      B(3,1)=+1.732*KD*COS(WT)
      B(3,5)=+1.732*KD*SIN(WT-0.524)
      B(4,1)=-1.732*KQ*SIN(WT)
      B(4,5)=1.732*KQ*COS(WT-0.524)
      B(5,2)=1.732*MF*SIN(WT-0.524)
      B(5,3)=1.732*MD*SIN(WT-0.524)
      B(5,4)=1.732*MD*COS(WT-0.524)
70
      CONTINUE
      BRH(1,1)=-(RP+2*RA)*IL+RA*IK+1.732*MF*OMEGA*SIN(WT)
     1*IFT+1.732*MD*OMEGA*SIN(WT)*ID
     1+1.732*MD*OMEGA*COS(WT)*IQ
      BRH(2,1)=1.732*KF*OMEGA*(SIN(WT)*IL-IK*COS(WT-0.524))
      BRH(3,1)=+1.732*KD*OMEGA*(IL*SIN(WT)-IK*COS(WT-0.524))
      BRH(4,1)=1.732*KQ*DMEGA*(IL*COS(WT)+IK*SIN(WT-0.524))
      BRH(5,1)=RA*IL-2*RA*IK-1.732*MF*OMEGA*IFT*
     1COS(WT-0.524)-1.732*MD*OMEGA*ID*
     1COS(WT-0.524)+1.732*MD*OMEGA*IQ*
     15IN(WT-0.524)
      H=B(1,1)-B(1,2)*B(2,1)-B(1,3)*B(3,1)-B(1,4)*B(4,1)
      C=B(1,5)-B(1,2)*B(2,5)-B(1,3)*B(3,5)-B(1,4)*B(4,5)
      D=BRH(1,1)-B(1,2)*BRH(2,1)-B(1,3)*BRH(3,1)-B(1,4)*BRH(4,1)
      E=B(5,1)-B(5,2)*B(2,1)-B(5,3)*B(3,1)-B(5,4)*B(4,1)
      F=B(5,5)-B(2,5)*B(5,2)-B(5,3)*B(3,5)-B(5,4)*B(4,5)
      G=BRH(5,1)-B(5,2)*BRH(2,1)-B(5,3)*BRH(3,1)-B(5,4)*BRH(4,1)
      BRH(1,1)=(D*F-C*G)/(H*F-C*E)
      BRH(5,1)=(H*G-D*E)/(H*F-C*E)
      BRH(1,1)=DIL/DT, BRH(5,1)=DIK/DT
C
      IF(KEY.GT.1) GO TO 20
      WT=WT+DWT
      IL=IL+BRH(1,1)*DT
      IK=IK+BRH(5,1)*DT
      ILC=IL
```

```
IKC=IK
      DILDT=BRH(1,1)
      DIKDT=BRH(5,1)
      GO TO 30
      CONTINUE
20
      IL=ILO+((DILDT+BRH(1,1))*DT)/2
      IK=IKO+((DIKDT+BRH(5,1))*DT)/2
30
      CONTINUE
      IFT=SF-1.732*KF*(IL*COS(WT)+IK*SIN(WT-0.524))
      ID=SD-1.732*KD*(IL*COS(WT)+IK*SIN(WT-0.524))
      IQ=SQ+1.732*KQ*(IL*SIN(WT)-IK*COS(WT-0.524))
      IF(KEY.LT.2) GO TO 120
      IF((ABS(IL-ILC), LE.1.0), AND, (ABS(IK-IKC), LE.1.0)) GO TO 100
      ILC=IL
      IKC=IK
      IF(KEY.GT.50) GO TO 997
      GO TO 120
100
      CONTINUE
      KK=KK+1
      CIL(KK)=IL
      CIK(KK)=IK
300
      CONTINUE
      IF(IL.GT.ILFMAX) GO TO 997
      TEST FOR END OF COMMUTATION PERIOD
C
      IF(IK.GE.IL) GO TO 110
26
      CONTINUE
      WRITE (7,721)
      FORMAT(' ',5X,'COMMUTATION PERIOD DOES NOT END')
721
      GJ TO 997
99
      CONTINUE
      DUM=BETA+MU-1.047
997
      DO 86 K=1.KK
      DUM=DUM+DWT
      CWT(K)=DUM
      CONTINUE
86
      DO 144 L=1,KK
      WRITE(7,145)CIL(L),CIK(L),CWT(L)
C
      FORMAT(' ',2X,'IL=',E10.3,5X,'IK=',E10.3,5X,'WT=',E10.3)
145
      CONTINUE
144
      RETURN
      END
```

```
SUBROUTINE JACOB(MF, BETA, IF, W, V, IL, MO, MU, DELTAO, OMEGA, FF, A, B, C)
 DIMENSION FF(5,5)
 REAL*4 MO, MOO, MU, MF, IL, IF, K1, OMEGA
 PAIF=1.155*MF*SIN(BETA)
 PBIF=1.155*MF
 PABETA=1.155*IF*MF*COS(BETA)+1.91*MO*(W*COS(BETA)-V*SIN(BETA))
 PBBETA=-1.91*MO*IL*SIN(BETA+MU)
 PCBETA=-1.91*MO*IL*COS(BETA+MU)
 PAMU=-1.91*MO*IL*COS(MU)
 PWMU=0.0
 PVMU=0.0
 PBMU=-1.91*MO*IL*SIN(BETA+MU)
 PCMU=-1.91*MO*IL*COS(BETA+MU)
 PAW=1.91*MO*SIN(BETA)
 PBW=1.91*MO
 PAV=1.91*MO*COS(BETA)
 PCV=1.91*MO
 FF(1,1)=(COS(BETA+MU)-COS(BETA))*PAIF
1+0.25*(2*MU-SIN(2*(BETA+MU))+SIN(2*BETA))*PBIF
 FF(1,2)=(COS(BETA+MU)-COS(BETA))*PABETA
1-A*(SIN(BETA+MU)-SIN(BETA))-0.25*(2*MU
1-SIN(2*(BETA+MU))+SIN(2*BETA))*PBBETA
1+0.5*B*(-COS(2*(BETA+MU))+COS(2*BETA))
1+0.5*((SIN(BETA+MU))**2-(SIN(BETA))**2)
1*PCBETA+C*(SIN(BETA+MU)*COS(BETA+MU)-SIN(BETA)*COS(BETA))
 FF(1,3)=PAMU*(COS(BETA+MU)-COS(BETA))-A*SIN(BETA+MU)
1+0.25*(2*MU-SIN(2*(BETA+MU))+SIN(2*BETA))*
1PBMU+(B/2)*(1-COS(2*(BETA+MU)))+0.5*((SIN(BETA+MU))**2
1-(SIN(BETA))**2)*PCMU+C*(SIN(BETA+MU)*COS(BETA+MU))
 FF(1,4)=PAV*(COS(BETA+MU)-COS(BETA))+0.5*((SIN(BETA+MU))**2
1-(SIN(BETA))**2)*PCV
 FF(1,5)=DELTAO+PAW*(COS(BETA+MU)-COS(BETA))
1+0.25*(2*MU~SIN(2*(BETA+MU))+SIN(2*BETA))*PBW
 FF(2,1)=PAIF*(SIN(BETA)-SIN(BETA+MU))
1+0.5*((SIN(BETA+MU))**2-(SIN(BETA))**2)*PBIF
FF(2,2)=PABETA*(SIN(BETA)-SIN(BETA+MU))
1+A*(COS(BETA)-COS(BETA+MU))
1+0.5*((SIN(BETA+MU))**2-(SIN(BETA))**2)*PBBETA
1+B*(SIN(BETA+MU)*COS(BETA+MU)-SIN(BETA)*COS(BETA))
1+0.25*PCBETA*(2*MU+SIN(2*(BETA+MU))-SIN(2*BETA))
1+0.5*C*(COS(2*(BETA+MU))-COS(2*BETA))
 FF(2,3)=PAMU*(SIN(BETA)-SIN(BETA+MU))
1-A*COS(BETA+MU)+0.5*PBMU*((SIN(BETA+MU))**2
1-(SIN(BETA))**2)+B*(SIN(BETA+MU)*COS(BETA+MU))
1+0.25*PCMU*(2*MU+SIN(2*(BETA+MU))-SIN(2*BETA))
1+0.5*C*(1+COS(2*(BETA+MU)))
FF(2,4)=DELTAO+PAV*(SIN(BETA)-SIN(BETA+MU))
1+0.25*PCV*(2*MU+SIN(2*(BETA+MU))-SIN(2*BETA))
 FF(2,5)=PAW*(SIN(BETA)-SIN(BETA+MU))
1+0.5*PBW*((SIN(BETA+MU))**2-(SIN(BETA))**2)
FF(3,1)=(3.*OMEGA/3.1416)*(1.732*MF*SIN(BETA+MU))
FF(3,2)=(3,*0MEGA/3,1416)*((1,732*IF*MF*COS(BETA+MU))
1+((9.*MO/3.1416)*(W*COS(BETA+MU)-V*SIN(BETA+MU))))
FF(3,3)=(3,*OMEGA/3,1416)*((1,732*IF*MF*COS(BETA+MU))
1+((9.*MO/3.1416)*(W*COS(BETA+MU)-V*SIN(BETA+MU))))
FF(3,4)=27.*OMEGA*MO*COS(BETA+MU)/((3.1416)**2)
```

```
FF(3,5)=27.*OMEGA*MO*SIN(BETA+MU)/((3.1416)**2)
      FF(4,1)=MF*COS(BETA)/1.732
      FF(4,2)=(-IF*MF*SIN(BETA)/1.732)
     1+((3.*MO/3.1416)*(-W*SIN(BETA)-V*COS(BETA)))
      FF(4,3) = -3.*MO*IL*SIN(MU)/3.1416
      FF(4,4) = -3.*MO*SIN(BETA)/3.1416
      FF(4,5)=3.*MO*COS(BETA)/3.1416
      FF(5,1)=-4.*MF*COS(BETA+MU/2)*SIN(MU/2)/1.732
      FF(5,2)=(4.*IF*MF*SIN(BETA+MU/2)*SIN(MU/2)/1.732)
     1+((6.*MO/3.1416)*(W*(COS(BETA)-COS(BETA+MU))
      1-V*(SIN(BETA)-SIN(BETA+MU))))
      FF(5,3)=(-4,*IF*MF/1,732)*(-0,5*SIN(BETA+MU/2)*SIN(MU/2)
      1+0.5*COS(BETA+MU/2)*COS(MU/2))
     1+(6.*MO/3.1416)*(-W*COS(BETA+MU)+V*SIN(BETA+MU))
      1-6.*IL*MO*COS(MU)/3.1416
      FF(5,4)=6.*MO*(COS(BETA)-COS(BETA+MU))/3.1416
      FF(5,5)=6.*MO*(SIN(BETA)-SIN(BETA+MU))/3.1416
      DO 2 II=1,5
      FF(1,II)=FF(1,II)*1.0E 04
2
      CONTINUE
      DO 3 II=1,5
      FF(2,II)=FE(2,II)*1.0E 04
      CONTINUE
3
      DO 4 II=1,5
      FF(4, II)=FF(4, II) *1.0E 04
4
      CONTINUE
      DO 5 II=1,5
      FF(5, II)=FF(5, II)*1.0E 04
      CONTINUE
.5
      RETURN
      END
```

```
SUBROUTINE JACOB4(MF, BETA, IF, W, V, IL, MO, MU, DELTAO, OMEGA, FF,
1A,B,C)
 DIMENSION FF(4,4)
 REAL*4 MO, MOO, MU, MF, IL, IF, K1, DMEGA
 PAIF=1.155*MF*SIN(BETA)
 PBIF=1.155*MF
 PABETA=1.155*IF*MF*COS(BETA)+1.91*MO*(W*COS(BETA)-V*SIN(BETA))
 PBBETA=-1.91*MO*IL*SIN(BETA+MU)
 PCBETA=-1.91*MO*IL*COS(BETA+MU)
 PAMU=-1.91*MO*IL*COS(MU)
 PWMU=0.0
 PUMU=0.0
 PBMU=-1.91*MO*IL*SIN(BETA+MU)
 PCMU=-1.91*MO*IL*COS(BETA+MU)
 PAW=1.91*MO*SIN(BETA)
 PBN=1.91*MO
 PAV=1.91*MO*COS(BETA)
 FCU=1.91*MO
FF(1,1)=(COS(BETA+MU)-COS(BETA))*PABETA
1-A*(SIN(BETA+MU)-SIN(BETA))-0.25*(2.*MU
1-SIN(2.*(BETA+MU))+SIN(2.*BETA))*PBBETA
1+0.5*B*(-COS(2.*(BETA+MU))+COS(2.*BETA))
1+0.5*((SIN(BETA+MU))**2-(SIN(BETA))**2)
1*PCBETA+C*(SIN(BETA+MU)*COS(BETA+MU)-SIN(BETA)*COS(BETA))
FF(1,2)=PAMU*(COS(BETA+MU)-COS(BETA))-A*SIN(BETA+MU)
1+0,25*(2,*MU-SIN(2,*(BETA+MU))+SIN(2,*BETA))*
1PBMU+(B/2,)*(1-COS(2,*(BETA+MU)))+0.5*((SIN(BETA+MU))**2
1-(SIN(BETA))**2)*PCMU+C*(SIN(BETA+MU)*COS(BETA+MU))
FF(1,3)=PAV*(COS(BETA+MU)-COS(BETA))+0.5*((SIN(BETA+MU))**2
1-(SIN(BETA))**2)*PCV
FF(1,4)=DELTAO+PAW*(COS(BETA+MU)-COS(BETA))
1+0.25*(2.*MU-SIN(2.*(BETA+MU))+SIN(2.*BETA))*PBW
 FF(2,1)=PABETA*(SIN(BETA)-SIN(BETA+MU))
1+A*(COS(BETA)-COS(BETA+MU))
1+0.5*((SIN(BETA+MU))**2-(SIN(BETA))**2)*PBBETA
1+B*(SIN(BETA+MU)*COS(BETA+MU)-SIN(BETA)*COS(BETA))
1+0.25*PCBETA*(2.*MU+SIN(2.*(BETA+MU))-SIN(2.*BETA))
1+0.5*C*(COS(2.*(BETA+MU))-COS(2.*BETA))
FF(2,2)=PAMU*(SIN(BETA)-SIN(BETA+MU))
1-A*COS(BETA+MU)+0.5*PRMU*((SIN(BETA+MU))**2
1-(SIN(BETA))**2)+B*(SIN(BETA+MU)*COS(BETA+MU))
1+0.25*PCMU*(2.*MU+SIN(2.*(BETA+MU))-SIN(2.*BETA))
1+0.5*C*(1+COS(2.*(BETA+MU)))
FF(2,3)=DELTAO+PAV*(SIN(BETA)-SIN(BETA+MU))
1+0.25*PCV*(2.*MU+SIN(2.*(BETA+MU))-SIN(2.*BETA))
FF(2,4)=PAW*(SIN(BETA)-SIN(BETA+MU))
1+0.5*PBW*((SIN(BETA+MU))**2-(SIN(BETA))**2)
FF(3,1)=(3.*OMEGA/3.1416)*((1.732*IF*MF*COS(BETA+MU))
1+((9,*MO/3,1416)*(W*COS(BETA+MU)-V*SIN(BETA+MU))))
FF(3,2)=(3.*OMEGA/3.1416)*((1.732*IF*MF*COS(BETA+MU))
1+((9.*MO/3.1416)*(@*COS(BETA+MU)-V*SIN(BETA+MU))))
FF(3,3)=27.*OMEGA*MO*COS(BETA+MU)/((3.1416)**2)
FF(3,4)=27.*OMEGA*MO*SIN(BETA+MU)/((3.1416)**2)
FF(4,1)=(4.*IF*MF*SIN(BETA+MU/2.)*SIN(MU/2.)/1.732)
1+((6,*M0/3,1416)*(W*(COS(BETA)-COS(BETA+MU))
1-V*(SIN(BETA)-SIN(BETA+MU))))
FF(4,2)=(-4.*IF*MF/1.732)*(-0.5*SIN(BETA+MU/2.)*SIN(MU/2.)
```

1+0.5*COS(BETA+MU/2.)*COS(MU/2.)) 1+(6.*M0/3.1416)*(-W*COS(BETA+MU)+V*SIN(BETA+MU)) 1-6.*MO*COS(MU)*IL/3.1416 FF(4,3)=6.*MO*(COS(BETA)-COS(BETA+MU))/3.1416 FF(4,4)=6.*MO*(SIN(BETA)-SIN(BETA+MU))/3.1416 DO 2 II=1,4 FF(1,II)=FF(1,II)*1.0E 04 CONTINUE DO 3 II=1,4 FF(2, II)=FF(2, II) *1.0E 04 CONTINUE 3 DO 4 II = 1,4 FF(4, II)=FF(4, II) *1.0E 04 4 CONTINUE RETURN END

```
SUBROUTINE LITLI(DELTAO, MF, IF, BETA, MO, W,
     1MOO, V, IL, DELTAF, MU, AID, AIQ, AIF, AIK, THETA, KQ, KF, KD)
      DIMENSION AIF(60), AID(60), AIQ(60), AIK(60), THETA(60)
      REAL*4 MF, IF, MO, MOO, IL, MU, MD, KQ, KD, KF
      WRITE(7,10)KF,KQ,KD
10
      FORMAT(' ',1X,'KF =',E15.3,'KQ =',E15.3,'KD =',E15.3)
      WRITE (7,11) IL
      WRITE(7,12)BETA
      WRITE(7,13)MU
      WRITE(7,14) IF
      WRITE(7,15)V
      WRITE(7,16)W
      FORMAT(' ',1X,'IL =',F10.2)
11
      FORMAT(' ',1X,'BETA =',F10.3)
12
      FORMAT(' ',1X,'MU =',F10.3)
13
      FORMAT(' ',1X,'IF =',F10.3)
14
      FORMAT(' ', 1X, 'V =', F10.3)
15
      FORMAT(' ',1X,'W =',F10.3)
16
      WRITE(7,9)
      FORMAT(' ',9X,'THETA',9X,'IK',12X,'IQ',12X,'ID',12X,'IF')
      ANG=BETA+MU-1.0472
      DO 100 L=1,60
      X=ANG-BETA
      Y=ANG-(BETA+MU)
      Z=ANG-(BETA+1.0472)
      IF(X) 2,2,3
      IF(Y) 5,2,4
3
4
      IF(Z) 2,2,5
2
      AIK(L)=0.0
      GO TO 6
      AIK(L)=(1./DELTA0)*(1.155*MF*IF*(SIN(BETA)-SIN(ANG))
5
     1+1.91*MO*W*(SIN(BETA)-SIN(ANG))+1.91*MOO*V*(COS(BETA)
     1-COS(ANG))-0,955*IL*DELTAF*(SIN(MU)+SIN(ANG-BETA-MU)))
      AIQ(L)=1.732*KQ*(0.955*(V-IL*SIN(BETA+MU))
6
     1+(IL*SIN(ANG+0.524)-AIK(L)*COS(ANG)))
      AID(L)=1.732*KD*(0.955*(W+IL*COS(BETA+MU))
     1-(IL*CDS(ANG+0.524)+AIK(L)*SIN(ANG)))
      AIF(L)=AID(L)*KF/KD
      THETA(L)=ANG*180.0/3.1416
      AIK(L)=-AIK(L)
      ANG=ANG+0.01745
      WRITE(7,200)THETA(L),AIK(L),AIQ(L),AID(L),AIF(L)
      FORMAT(' ',1X,F14.2,4E14.3)
200
      CONTINUE
100
      RETURN
      END
```

```
SUBROUTINE NEWTON(MU, BETA, IF, W, V, FREG, DELTAO, IL, VL, MOO, K1,
     1MF, MO, OMEGA, DELTAF, ZETA)
      DIMENSION FD(5),F(5,1),FF(5,5)
      REAL*4 MO, MOO, MU, IF, IL, K1, MF
      SLIGHT ERROR FOR IL.NE.O BUT.LT.35
C
      KAT=0
      K=0
      IF(IL.GE.35.0) GO TO 50
      MU=0.0
      RETA=3.1416/2.
      IF=(1./(MF*1.732))*((4.17E-04)*VL-0.75*IL*DELTA0)
      W=0.0
      V=IL
      GO TO 51
      X=SQRT((18*FREQ*DELTAO*IL)/(4*VL+18*FREQ*DELTAO*IL))
50
      CALL ARCSIN(X)
      MU=2*X
      ZETA=SIN(MU/2)/(MU/2)
      A=-(((3.1416*DELTAO)/(6*(1-COS(MU))*MOO))+(1-K1)*SIN(MU)
     1+ZETA*K1*SIN(MU/2))/((1-K1)*COS(MU)+ZETA*K1*COS(MU/2))
      B=ATAN(A)
      IF (B.GE.O.) GO TO 2
      BETA=3.1416+B
      GO TO 3
      BETA = B
2
      IF=(1/(1.732*MF*SIN(BETA+MU)))*((VL/(6*FREQ))-(0.75*IL*DELTA0)-(
3
     14.5*IL*ZETA*K1*DELTAF*SIN(MU/2)/3.1416))
      W = IL*K1*(-COS(BETA+MU)+ZETA*COS(BETA+MU/2))
      V=IL*K1*(SIN(BETA+MU)-ZETA*SIN(BETA+MU/2))
       WRITE(7,510)
C
      FORMAT('0',5X,'****FRANKLIN SOLUTION********)
510
      WRITE(7,300)K, BETA, MU, IF, W, V
C
51
      CONTINUE
      DO 70 K=1,200
      KK=0
      A=1.155*IF*MF*SIN(BETA)+1.91*MO*(W*SIN(BETA)
     1+U*COS(BETA))-1.91*MO*IL*SIN(MU)
      B=1.155*IF*MF+1.91*MO*W+1.91*IL*MO*COS(BETA+MU)
      C=1.91*MO*(V-IL*SIN(BETA+MU))
      CALL RHS(IF, MF, BETA, MO, W, V, IL, MU, DELTAO, F, OMEGA, A, B, C, VL)
      WRITE(7,486)F(1,1),F(2,1),F(3,1),F(4,1),F(5,1)
C
486
      FORMAT (5E20.7)
      DO 71 L=1,5
      FD(L) = -F(L,1)
      Y=ABS(FD(L))
      IF(Y.GT.0.001) KK=1
71
       CONTINUE
      IF(KK.GE.1) GO TO 72
      GO TO 75
72
      CONTINUE
      CALL JACOB(MF, BETA, IF, W, V, IL, MO, MU, DELTAO, OMEGA, FF, A, B, C)
      IF (KAT.NE.O) GO TO 100
      KAT=1
100
      IEQN=5
      IVEC=1
      EPS=0.01
      K10=0
```

```
CALL GELG(FD, FF, IEQN, IVEC, EPS, K10)
      BETA=BETA+FD(2)
      MU=MU+FD(3)
      IF=IF+FD(1)
      V=V+FD(4)
      W=W+FD(5)
      WRITE(7,300)K, BETA, MU, IF, W, V
300
      FORMAT(' ',1X,14,3X,'BETA=',E14.7,3X,'MU=',E14.7,
     13X, 'IF=', E14.7, 3X, 'W=', E14.7, 3X, 'V=', E14.7)
      CONTINUE
70
      WRITE(7,78)
78
      FORMAT(' ',1X,'NEWTON-RHAPSON DOES NOT CONVERGE')
75
      CONTINUE
      IF(K.EQ.1) WRITE(7,500)
      FORMAT(' ',1X,'NEWTON DID NOT ITTERATE, K=1')
500
C
      FORMAT('0',2X,'********FINAL SOLUTION ********')
487
      WRITE(7,300)K,BETA,MU,IF,W,V
C
C
      WRITE(7,488)
      FORMAT('0',2X,'THIS IS THE RHS VECTOR FOR TEST')
488
      WRITE(7,489)F(1,1),F(2,1),F(3,1),F(4,1),F(5,1)
C
489
      FORMAT (5E20.7)
      RETURN
      END
```

```
SUBROUTINE NEWSON(MU, BETA, IF, W, V, FREQ, DELTAO, IL, VL, MOO, K1,
     1MF, MO, OMEGA, DELTAF, ZETA, K)
      DIMENSION FD(5),F(5,1),FF(5,5)
      REAL #4 MO, MOO, MU, IF, IL, K1, MF
      SLIGHT ERROR FOR IL.NE.O BUT.LT.35
C
      KAT=0
      IF(IL.GE.35.0) GO TO 50
      MU=0.0
      BETA=3.1416/2.
      IF=(1./(MF*1.732))*((4.17E-04)*VL-0.75*IL*DELTAO)
      W=0.0
      V=IL
      GO TO 51
50
      X=((4*3.1416*VL-9*OMEGA*IL*DELTAO)/(4*3.1416*VL
     1+9*OMEGA*IL*DELTAO))
      CALL ARCCOS(X)
      MU=X
      ZETA=SIN(MU/2)/(MU/2)
      A=-(((3.1416*DELTA0)/(6*(1-CDS(MU))*MOO))+(1-K1)*SIN(MU)
     1+ZETA*K1*SIN(MU/2))/((1-K1)*COS(MU)+ZETA*K1*COS(MU/2))
      B=ATAN(A)
      IF(B.GE.O.) GO TO 2
      BETA=3.1416+B
      GO TO 3
2
      BETA = B
      IF=(1/(1.732*MF*SIN(BETA+MU)))*((VL/(6*FREQ))-(0.75*IL*DELTA0)-(
3
     14.5*IL*ZETA*K1*DELTAF*SIN(MU/2)/3.1416))
      W = IL*K1*(-COS(BETA+MU)+ZETA*COS(BETA+MU/2))
      V=IL*K1*(SIN(BETA+MU)-ZETA*SIN(BETA+MU/2))
      CONTINUE
51
      DO 70 K=1,200
      KK=0
      A=1.155*IF*MF*SIN(BETA)+1.91*MO*(W*SIN(BETA)
     1+V*COS(BETA))-1.91*MO*IL*SIN(MU)
      B=1.155*IF*MF+1.91*MO*W+1.91*IL*MO*COS(BETA+MU)
      C=1.91*MO*(V-IL*SIN(BETA+MU))
      CALL RHS(IF, MF, BETA, MO, W, V, IL, MU, DELTAO, F, OMEGA, A, B, C, VL)
      WRITE(7,486)F(1,1),F(2,1),F(3,1),F(4,1),F(5,1)
C
486
      FORMAT (5E20.7)
      DO 71 L=1,5
      FD(L) = -F(L,1)
      Y=ABS(FD(L))
      IF(Y.GT.0.01) KK=1
71
       CONTINUE
      IF(KK.GE.1) GO TO 72
      GO TO 75
72
      CONTINUE
      CALL JACOB(MF, BETA, IF, W, V, IL, MO, MU, DELTAO, OMEGA, FF, A, B, C)
      IEQN=5
      IVEC=1
      EPS=0.01
      K10=0
      CALL GELG(FD, FF, IEQN, IVEC, EPS, K10)
      BETA=BETA+FD(2)
      MU=MU+FD(3)
      IF=IF+FD(1)
      V=V+FD(4)
```

W=W+FD(5) WRITE(7,300)K,BETA,MU,IF,W,V C 300 FORMAT(' ',1X,14,3X,'BETA=',E14.7,3X,'MU=',E14.7, 13X,'IF=',E14.7,3X,'W=',E14.7,3X,'V=',E14.7) 70 CONTINUE WRITE(7,78) FORMAT(' ',1X, 'NEWTON-RHAPSON DOES NOT CONVERGE') 78 75 CONTINUE IF(K.EQ.1) WRITE(7,500) FORMAT(' ',1X, 'NEWTON DID NOT ITTERATE, K=1') 500 WRITE(7,487) C FORMAT('0',2X,'********FINAL SOLUTION ********') 487 WRITE(7,300)K,BETA,MU,IF,W,V WRITE(7,488) 488 FORMAT('0',2X,'THIS IS THE RHS VECTOR FOR TEST') WRITE(7,489)F(1,1),F(2,1),F(3,1),F(4,1),F(5,1) C 489 FDRMAT (5E20.7) RETURN END

```
SUBROUTINE PHACON(IF, MF, BETA, MO, W, V, IL, MU, DELTAO, OMEGA, VL, MOO)
      REAL*4 IF, MF, MO, IL, MU, MOO, DMEGA
      DIMENSION FD1(4),F1(4,1),FF1(4,4)
      KAT=0
      BETA=BETA+(5.0*3.1416/180.0)
      DO 100 K=1,70
      KK=0
      A=1.155*IF*MF*SIN(BETA)+1.91*MO*(W*SIN(BETA)
     1+V*COS(BETA))-1.91*MO*IL*SIN(MU)
      B=1.155*IF*MF+1.91*MO*W+1.91*IL*MO*COS(BETA+MU)
      C=1.91*MO*(V-IL*SIN(BETA+MU))
      CALL RHS484(IF, MF, BETA, MO, W, V, IL, MU, DELTAO, F1, OMEGA, A, B, C, VL)
      DO 101 L=1,4
      FD1(L)=-F1(L,1)
      Y=ABS(FD1(L))
      IF (Y.GE.O.01) KK=1
       CONTINUE
101
      IF(KK.GE.1) GO TO 102
      GO TO 105
102
       CONTINUE
      CALL JACOB4(MF, BETA, IF, W, V, IL, MO, MU, DELTAO, OMEGA, FF1, A, B, C)
      IF(KAT.NE.O) GO TO 300
300
      KAT=1
      IEQN=4
      IVEC=1
      EPS=0.01
      K10=0
      CALL GELG(FD1,FF1, IEQN, IVEC, EPS, K10)
      BETA=BETA+FD1(1)
      MU=MU+FD1(2)
      V=V+FD1(3)
      W=W+FD1(4)
       CONTINUE
100
      WRITE(7,2000)
       FORMAT(' ',1X, 'NEWT-RAP DOESN T CONV FOR PHASE CONTROL')
2000
105
      IF(K.EQ.1) WRITE(7,305)
      FORMAT(' ',1X, 'PHACON DID NOT ITTERATE, K=1')
305
      RETURN
      END
```

```
SUBROUTINE RHS(IF, MF, BETA, MO, W, V, IL, MU, DELTAO, F, OMEGA, A, B, C, VL)
DIMENSION F(5,1)
REAL*4 MO, MU, MF, IL, IF, OMEGA
F(1,1)=DELTAO*W+A*(COS(BETA+MU)-COS(BETA))+(B/4.)*
1(2.*MU-SIN(2.*(BETA+MU))+SIN(2.*BETA))
1+(C/2.)*((SIN(BETA+MU))**2-(SIN(BETA))**2)
F(2,1)=DELTAO*V+A*(SIN(BETA)-SIN(BETA+MU))
1+(B/2.)*((SIN(BETA+MU))**2-(SIN(BETA))**2)
1+(C/4.)*(2.*MU+SIN(2.*(BETA+MU))-SIN(2.*BETA))
F(3,1)=-VL+0.955*DMEGA*(0.75*IL*DELTAO+1.732*IF*MF*
1SIN(BETA+MU)+2.865*MO*(W*SIN(BETA+MU)
1+V*COS(BETA+MU)))
F(4,1)=(0.5774*IF)*MF*COS(BETA)+(0.955*MO)
1*(W*COS(BETA)-V*SIN(BETA))+0.955*MO*COS(MU)*IL
F(5,1) = -DELTAO*IL-(2.3094*IF)*MF*COS(BETA+MU/2)
1*SIN(MU/2)+(1.91*MO)*(W*(SIN(BETA)
1-SIN(BETA+MU))+V*(COS(BETA)-COS(BETA+MU)))
1-1.91*MO*SIN(MU)*IL
F(1,1)=F(1,1)*1.0E 04
F(2,1)=F(2,1)*1.0E 04
F(4,1)=F(4,1)*1.0E 04
F(5,1)=F(5,1)*1.0E 04
RETURN
END
```

```
SUBROUTINE RHS484(IF, MF, BETA, MO, W, V, IL, MU, DELTAO, F, OMEGA,
1A, B, C, VL)
 DIMENSION F(4,1)
 REAL*4 MO, MU, MF, IL, IF, OMEGA
F(1,1)=DELTAO*W+A*(COS(BETA+MU)-COS(BETA))+(B/4.)*
1(2.*MU-SIN(2.*(BETA+MU))+SIN(2.*BETA))
1+(C/2.)*((SIN(BETA+MU))**2-(SIN(BETA))**2)
F(2,1)=DELTAO*V+A*(SIN(BETA)-SIN(BETA+MU))
1+(B/2.)*((SIN(BETA+MU))**2-(SIN(BETA))**2)
1+(C/4.)*(2.*MU+SIN(2.*(BETA+MU))-SIN(2.*BETA))
F(3,1)=-VL+0.955*DMEGA*(0.75*IL*DELTA0+1.732*IF*MF*
1SIN(BETA+MU)+2.865*MO*(W*SIN(BETA+MU)
1+V*COS(BETA+MU)))
F(4,1) = - DELTAO*IL - (2.309*IF) *MF*COS(BETA+MU/2.)
1*SIN(MU/2.)+(1.91*MO)*(W*(SIN(BETA)
1-SIN(BETA+MU))+V*(COS(BETA)-COS(BETA+MU)))
1-1.91*MO*SIN(MU)*IL
F(1,1)=F(1,1)*1.0E 04
 F(2,1)=F(2,1)*1.0E 04
F(4,1)=F(4,1)*1.0E 04
 RETURN
END
```

SUBROUTINE RMS(BETA, LLL, MU, RMSIF, IL, DELTAO, MF, MO, W, V, MOO, IF 1,KF,DELTAF) DIMENSION RMSIF(50) REAL*4 IK, IF, IL, MU, MF, MOO, MO, KF THETA=BETA+MU-(3.1416/3.) DTHETA=3.1416/300. SIF=0.0 DO 1 K=1,50 THETA=THETA+DTHETA IK=(1./DELTAO)*((2./1.732)*IF*MF*(SIN(BETA)-SIN(THETA))1+(6./3.1416)*(MO*W*(SIN(BETA)-SIN(THETA))+MOO*V*(COS(BETA) 1-COS(THETA)))-(3./3.1416)*IL*DELTAF*(SIN(MU)+SIN(THETA-1BETA-MU))) IF (THETA.LT.BETA) IK=0.0 SIF=(1.732*KF*((3./3.1416)*(W+IL*COS(BETA+MU))-(IL*COS(1THETA+3.1416/6.)+IK*SIN(THETA))))**2+SIF THETA=THETA+DTHETA CONTINUE RMSIF(LLL)=SQRT(SIF)/SQRT(50.) RETURN END

1

```
SUBROUTINE TERMA(N,Y,PHI,X,AN1,BN1)
AN1=Y*(SIN((N+1)*X)*COS(PHI)+COS((N+1)*X)*SIN(PHI))
1/(2*(N+1))
AN1=AN1+Y*(SIN((N-1)*X)*COS(PHI)-COS((N-1)*X)*SIN(PHI))
1/(2*(N-1))
BN1=Y*(-COS((N+1)*X)*COS(PHI)+SIN((N+1)*X)*SIN(PHI))
1/(2*(N+1))
BN1=BN1-Y*(COS((N-1)*X)*COS(PHI)+SIN((N-1)*X)*SIN(PHI))
1/(2*(N-1))
RETURN
END
```

APPENDIX V: DISTRIBUTION LIST

AFAPL/DOE/STINFO
WRIGHT-PATTERSON AFB OH 45433

AIR UNIVERSITY
MAXWELL AFB AL 36112

AFAPL/POD WRIGHT-PATTERSON AFB OH 45433

AFWL/SY-1/DR. A. GUENTHER KIRTLAND AFB NM 87117

USA MEROC/COMMANDING OFFICER ATTN: SMEFB-ES/MR. LARRY AMSTUTZ FT. BELVOIR, VIRGINIA 22060

BOEING COMPANY ATTN: ASSISTANT SECRETARY PO BOX 3999 SEATTLE, WASHINGTON 98124

GARRETT CORPORATION
AIRESEARCH MANUFACTURING COMPANY
ATTN: MR. LEON SCHIPPER
2525 WEST 190TH STREET
TORRANCE, CALIFORNIA 90509

GENERAL DYNAMICS CORPORATION ATTN: VICE PRESIDENT ONE ROCKFELLER PLAZA NEW YORK, NY 10020

GENERAL ELECTRIC COMPANY
AEROSPACE AND DEFENCE SALES AND SERVICE
3430 SOUTH DIXIE
DAYTON, OHIO 45439

GEORGIA TECH SCHOOL OF ELECTRICAL ENGINEERING ATTN: DR. DIMITRIUS PARIS 225 NORTH AVENUE, NW ATLANTA, GEORGIA 30332 HUGHES RESEARCH LABORATORIES ATTN: DR. M. A. LUTZ 3011 MALIBU CANYON ROAD MALIBU, CALIFORNIA 90265

LOS ALAMOS SCIENTIFIC LABORATORIES ATTN: DR. HENRY L. LAQUER PO BOX 1663 LOS ALAMOS, NM 87544

MAGNETIC CORPORATION OF AMERICA 67 ROGERS STREET CALBRIDGE, MASSACHUSETTS 02142

MAXWELL LABORATORIES, INC. ATTN: DR. ALAN KOLB 9244 BALBOA AVENUE SAN DIEGO, CALIFORNIA 92122

PURDUE UNIVERSITY
SCHOOL OF ELECTRICAL ENGINEERING
ATTN: PROF. DAVID B. MILLER
LAFAYETTE, INDIANA 47907

RCA
ATTN: MGR. MARKETING ADM.
MARNE HIGHWAY
MOORESTOWN, NEW JERSEY 08057

STANFORD RESEARCH INSTITUTE ATTN: DR. D. CUBICCIOTTI STANFORD, CALIFORNIA 94305

TECH-TRAN LIGHT
50 INDEL AVENUE
RANCOCAS, NEW JERSEY 08073

TRW, INC.
SYSTEMS GROUP
ONE SPACE PARK
REDONDO BEACH, CALIFORNIA 90278

UNITED AIRCRAFT CORPORATION
RESEARCH LABORATORIES
ATTN: MR. ARTHUR CHALFANT
400 MAIN STREET
EAST HARTFORD, CONNECTICUT 06108

UNITED AIRCARFT CORPORATION UNITED TECHNOLOGY CENTER SUNNYVALE, CALIFORNIA 94088

UNIVERSITY OF BUFFALO ATTN: DR. A. S. GILMORE 3435 MAIN STREET BUFFALO, NEW YORK 14214

UNIVERSITY OF MICHIGAN
ATTN: MR. KEN BURNS, RM 218
RESEARCH ADMINISTRATION NORTH CAMPUS
ANN ARBOR, MICHIGAN 48105

UNIVERSITY OF WASHINGTON
DEPT. OF AERONAUTICAL ENGINEERING
ATTN: PROF. A. HERZBERG
SEATTLE, WASHINGTON 98105

UNIVERSITY OF WISCONSIN INSTRUMENTATION SYSTEMS CENTER ATTN: DR. R. W. BOOM 1500 JOHNSON DRIVE MADISON, WISCONSIN 53705

WESTINGHOUSE ADVANCED TECHNOLOGY LABORATORIES ATTN: DR. D. MERGERIAN, MS 3714 PO BOX 1521 BALTIMORE, MARYLAND 21203 WESTINGHOUSE ELECTRIC CORPORATION ATTN: MR. L. H. POWERS 1306 FARR DRIVE DAYTON, OHIO 45404

LOCKHEED MISSLES AND SPACE CO. ATTN: TECHNICAL INFORMATION CENTER P.O. BOX 504 SUNNYVALE, CA 94088

DOUGLAS AIRCRAFT COMPANY W.B. YOPP 3855 LAKEWOOD BOULEVARD LONG BEACH, CALIFORNIA 90801

HUGHES AIRCRAFT COMPANY
ELECTROMAGNETIC ENGINEERING SECTION
COMPONENTS AND MATERIALS LABORATORIES
ATTN: JACK K. KISCH
CULVER CITY, CA

TELEDYNE MEC ATTN: MR. BEN SMITH 3165 PORTER DRIVE PALO ALTO, CA 94304

MASSACHUSETTS INSTITUTE OF TECHNOLOGY DEPARTMENT OF MECHANICAL ENGINEERING CRYOGENIC ENGINEERING LABORATORY ATTN: DR. JOSEPH L. SMITH, JR. CAMBRIDGE, MA 02139